

## **Structural and microstructural characteristics of B-doped PbTe semiconductor**

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***Abstract:** The main task of this paper was accurate determination of structural and microstructural parameters of B-doped PbTe semiconductor ("p" type). Four samples (undoped PbTe, and three doped with initial B contents: 1 %, 3 % and 8 %) were synthesized using the Bridgman method and analysed using X-ray powder diffraction (XRD) technique. Structural features were obtained using the Rietveld method and microstructural by diffraction-line broadening methods. Microstructural measurements contain both crystallite domain sizes and microstrain calculations obtained by the Warren-Averbach and the simplified integral-breadth methods.*

**Keywords:** B-doped PbTe semiconductor, the Rietveld method, microstructural measurements.

### **INTRODUCTION**

PbTe is a narrow-gap semiconductor. The research in doping of semiconductor materials and hereby modified properties is one of the most significant tasks of modern semiconductor physics. Great consideration is given to optical, photoelectric and magnetic features of  $A^{IV}B^{VI}$  compounds doped with some elements from the III group (B, Al, Ga, In, Tl). The most studied compounds, thus far, are In, Ga and Tl-doped  $A^{IV}B^{VI}$  compounds. B-doped PbTe is one serial semiconductor material, important in manufacturing of laser and detector infrared (IR) optoelectronics within wavelength from 1 to 40  $\mu\text{m}$ .

The scope of the paper is to give an answer with the reference to the issues of how and where B atoms have sited into PbTe structure. Rietveld refinement method was used for structural and crystallite domain-size as well as crystal lattice microstrain calculations for microstructural determinations. Both crystallite domain size and microstrain measurements were calculated towards obtaining the crystallographic direction distributions of B atoms.

The Warren-Averbach method and corresponding microstrain calculations were applied in diffraction-line broadening measurements for surface-weighted ( $\langle D \rangle_s$ ) and volume-weighted ( $\langle D \rangle_v$ ), crystallite domain sizes. The referred measurements were also done by applying “simplified” integral-breadth methods: 1) broadenings originated due to both crystallite domain sizes and microstrains, which correspond to the Cauchy function, 2) the Gauss function and 3) both broadenings originated due to crystallite domain sizes that correspond to the Cauchy function and microstrains that correspond to the Gauss function. The last one provides for an excellent theoretical basis and it is widely applied in various Rietveld analysis softwares intended to microstructural calculations.

## EXPERIMENT AND ANALYTICAL METHODS

B-doped PbTe samples were synthesized using the Bridgman method. Pb and Te were applied in an ingot form, of a normal 99.99 wt% purity. So derived samples were further powdered for XRD analyses. Four samples were synthesized in the Institute of Technical Sciences of the Serbian Academy of Sciences and Arts: undoped PbTe, PbTe doped with B (1 at.%, 3 at.% and 8 at.%). X-ray intensity measurements were carried out on a PHILIPS PW 1710 automated diffractometer. The powder diffraction data are given in Table 1. The FULLPROF software [2] was used for the Rietveld structure refinement and BREADTH [1] for the diffraction-line broadening measurements.

## RESULTS AND DISCUSSION

### Rietveld structure refinement

PbTe is cubic, space group  $Fm\bar{3}m$  with  $Z=4$ . Both Pb and Te atoms are in fixed positions at  $\frac{1}{2}\frac{1}{2}\frac{1}{2}$  and 000 respectively, and both atoms are in octahedral

coordination.

**Table 1.** Rietveld powder diffraction data for B-doped PbTe.

Sample characterization				
Name (chemical, mineral)	Lead telluride (altaite)			
Empirical formula	PbTe			
Source/preparation	synthetic			
Technique				
Radiation type, source	X-rays, Cu $\lambda$ value used 1.54060Å $K\alpha_1/1.54439 K\alpha_2$			
Monochromator	diffracted beam graphite monochromator			
Detector (film, scint. etc)	proportional			
Instrument description (type, slits)	vertical diffractometer divergence slit 1° receiving slit 0.1 mm soller slit 1°			
Instrumental profile breadth	0.10 °2 $\theta$	temp. (°C)	25 ± 1	
Specimen size	form/particle edge loaded powder/ <10 $\mu\text{m}$ particle size			
Range of 2 $\theta$	from 20 ° to 140 °2 $\theta$ , 4 s per step			
Specimen motion	none			

There were no other phases except PbTe during the treatments. Even the reflection displacements did not occur. Therefore, the conclusion is that B atoms haven't deranged the PbTe structure when sited in it. (200) reflection showed strong, while (220) and (222) reflection showed appreciably weaker preferred orientation effects in all sample. The observed (circles), calculated (continuous line) and difference powder diffraction profiles for all analysed samples are shown in Figure 1. The Rietveld agreement factors are presented in Table 2.

Table 2. Rietveld refinement agreement factors

	PbTe	PbTe+B (1%)	PbTe+B (3%)	PbTe+B (8%)
$R_{exp}$	11.4	10.7	11.3	10.5
$R_p$	13.3	12.7	14.2	12.4
$R_{wp}$	14.3	14.1	14.9	14.8
$R_B$	6.12	5.58	5.69	5.82
$R_F$	6.47	5.55	5.28	6.48
$GoF$	1.6	1.7	1.6	1.7

The unit-cell parameter of pure PbTe is in a good agreement with all B-doped

samples and literature data [4] as well. The isotropic displacement parameters of

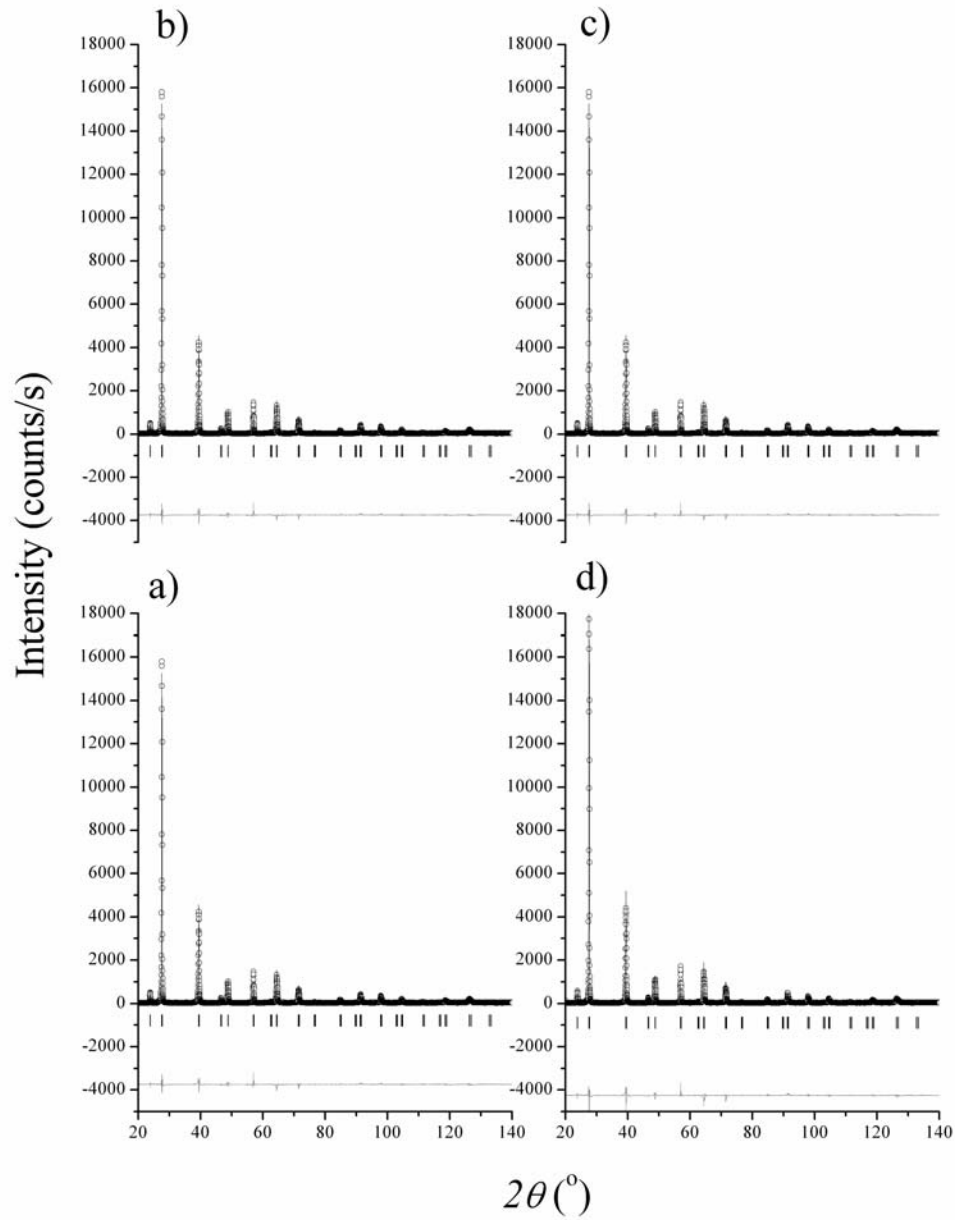


Figure 1. The observed (circles), calculated (continuous line) and difference powder diffraction profiles for: a) undoped PbTe, b) PbTe doped with B 1 at%, c) PbTe doped with B 3 at% and d) PbTe doped with B 8 at%.

Pb atoms have been observed to be larger than those of Te atoms, which can indicate thermal vibration increment of the Pb sublattice to that of the Te sublattice, especially in samples doped with 1 and 8 %. However, this is not an unusual phenomenon. Even in pure PbTe crystals, the relatively large anharmonic thermal vibrations of Pb lattice to that of the Te sublattice along the  $[hhh]$  direction were observed [3]. According to the same data these thermal vibrations of Pb atoms are enhanced by the alloying elements Ge or Sn and make a lattice unstable. Unit-cell and isotropic displacement parameters in comparison to the literature data [4] are given in Table 3.

Table 3. Rietveld refinement unit-cell and isotropic displacement parameters in comparison to the literature data.

	PbTe	<i>PbTe+B</i> (1%)	PbTe+B (3%)	PbTe+B (8%)	YASUTOSHI et al. (1987)
$B_{\text{iso}} \text{ Pb } (\text{\AA}^2)$	2.037(2)	2.661(1)	2.109(7)	2.648(1)	1.61(2)
$B_{\text{iso}} \text{ Te } (\text{\AA}^2)$	1.126(2)	1.319(2)	1.267(1)	1.426(6)	1.11(1)
$B_{\text{iso}} \text{ Pb}/B_{\text{iso}} \text{ Te}$	1.809	2.017	1.665	1.856	1.45
$a$ ( $\text{\AA}$ )	6.4603(2)	6.4605(2)	6.4601(7)	6.4605(2)	6.4541(9)
$V$ ( $\text{\AA}^3$ )	269.62(1)	269.65(2)	269.60(5)	269.65(1)	268.85

### Microstructural measurements

Microstructural parameter calculations were measured in crystallographic directions as follows:  $[h00]$ -(200), (400), (600);  $[hh0]$ -(220) (440);  $[hhh]$ -(111), (222), (333) (444);  $[hkk]$ -(311), (622)  $[h00]$  and  $[hh0]$  layers consist of both Pb and Te atoms while  $[hhh]$  and  $[hkk]$  layers consist of either Pb or Te atoms. So, the (311) layer consists entirely of Te atoms and the (622) one of Pb atoms. Likewise, (111) and (333) layers consist entirely of Te atoms; the (222) and (444) layers consist entirely of Pb atoms. Diffraction-line broadening measurements containing both crystallite domain sizes and microstrain parameters obtained by the Warren-Averbach and the simplified integral-breadth methods are given in Tables 4-7.

Table 4. Crystallite domain sizes obtained by the Warren-Averbach method.

		$D$ (Å)			
		$h\ 0\ 0$	$h\ h\ 0$	$h\ h\ h$	$h\ k\ k$
PbTe	$\langle D \rangle_s^*$	$480 \pm 36$	$357 \pm 29$	$466 \pm 64$	$163 \pm 82$
	$\langle D \rangle_v^{**}$	$484 \pm 14$	$443 \pm 19$	$484 \pm 27$	$315 \pm 113$
PbTe+B(1%)	$\langle D \rangle_s$	$498 \pm 43$	$428 \pm 38$	$476 \pm 46$	$312 \pm 25$
	$\langle D \rangle_v$	$543 \pm 20$	$482 \pm 20$	$546 \pm 24$	$421 \pm 20$
PbTe+B(3%)	$\langle D \rangle_s$	$417 \pm 46$	$339 \pm 30$	$394 \pm 63$	$235 \pm 18$
	$\langle D \rangle_v$	$406 \pm 17$	$362 \pm 14$	$407 \pm 26$	$314 \pm 14$
PbTe+B(8%)	$\langle D \rangle_s$	$554 \pm 38$	$430 \pm 54$	$448 \pm 51$	$330 \pm 41$
	$\langle D \rangle_v$	$583 \pm 16$	$536 \pm 36$	$545 \pm 46$	$479 \pm 38$

\* Surface-weighted domain size. \*\* Volume-weighted domain size.

Table 5. Microstrain parameters obtained by the Warren-Averbach method.

		$\langle \varepsilon^2 \rangle^{1/2} (10^{-3})$			
		$h\ 0\ 0$	$h\ h\ 0$	$h\ h\ h$	$h\ k\ k$
PbTe	$\langle \varepsilon^2 \rangle_{\langle D_s \rangle/2}^{1/2} *$	$0.89 \pm 0.03$	$0.99 \pm 0.05$	$0.66 \pm 0.05$	$0.72 \pm 0.02$
	$\langle \varepsilon^2 \rangle_{\langle D_v \rangle/2}^{1/2} **$	$0.88 \pm 0.02$	$0.89 \pm 0.04$	$0.68 \pm 0.05$	$0.75 \pm 0.02$
PbTe+B(1%)	$\langle \varepsilon^2 \rangle_{\langle D_s \rangle/2}^{1/2}$	$0.95 \pm 0.03$	$1.05 \pm 0.03$	$0.77 \pm 0.03$	$0.84 \pm 0.05$
	$\langle \varepsilon^2 \rangle_{\langle D_v \rangle/2}^{1/2}$	$0.91 \pm 0.02$	$0.94 \pm 0.03$	$0.72 \pm 0.03$	$0.73 \pm 0.04$
PbTe+B(3%)	$\langle \varepsilon^2 \rangle_{\langle D_s \rangle/2}^{1/2}$	$1.18 \pm 0.04$	$1.33 \pm 0.04$	$0.91 \pm 0.06$	$0.99 \pm 0.07$
	$\langle \varepsilon^2 \rangle_{\langle D_v \rangle/2}^{1/2}$	$1.19 \pm 0.04$	$1.29 \pm 0.04$	$0.89 \pm 0.06$	$0.86 \pm 0.06$
PbTe+B(8%)	$\langle \varepsilon^2 \rangle_{\langle D_s \rangle/2}^{1/2}$	$0.80 \pm 0.02$	$0.89 \pm 0.06$	$0.64 \pm 0.01$	$0.68 \pm 0.08$
	$\langle \varepsilon^2 \rangle_{\langle D_v \rangle/2}^{1/2}$	$0.78 \pm 0.02$	$0.80 \pm 0.05$	$0.53 \pm 0.01$	$0.56 \pm 0.07$

\* Root-mean-square microstrain (RMSM) averaged over the distance  $\langle D \rangle_s$ .

\*\* RMSM averaged over the distance  $\langle D \rangle_v$ .

Table 6. Crystallite domain sizes obtained by the simplified integral-breadth methods.

		$D$ (Å)			
		$h\ 0\ 0$	$h\ h\ 0$	$h\ h\ h$	$h\ k\ k$
PbTe	$\langle D_{C-C} \rangle^*$	524	491	467	271
	$\langle D_{C-G} \rangle^{**}$	454	446	446	323
	$\langle D_{G-G} \rangle^{***}$	451	443	443	319
PbTe+B(1%)	$\langle D_{C-C} \rangle$	652	619	569	454
	$\langle D_{C-G} \rangle$	523	509	463	421
	$\langle D_{G-G} \rangle$	506	493	460	420
PbTe+B(3%)	$\langle D_{C-C} \rangle$	469	441	403	317
	$\langle D_{C-G} \rangle$	384	374	366	311
	$\langle D_{G-G} \rangle$	375	368	361	311
PbTe +B(8%)	$\langle D_{C-C} \rangle$	672	638	617	502
	$\langle D_{C-G} \rangle$	562	551	539	479
	$\langle D_{G-G} \rangle$	555	544	538	478

Volume-averaged domain size from the simplified integral-breadth methods: \* Cauchy-Cauchy function, \*\* Cauchy-Gauss function, \*\*\* Gauss-Gauss function.

Microstrain parameters of both the Warren-Averbach and the simplified integral-breadth methods increase up to the sample doped with 3 %, to be followed by a rapid decrease in the sample doped with 8% of B. This trend is noticeable along each measured crystallographic direction. The referred phenomenon can be explained by B atoms, sited in PbTe structure, in two different manners. Besides, microstrain parameters in the directions, consisting of layers with homogeneous atoms, are much lower in comparison to the parameters with heterogeneous atoms. Taking into consideration all these facts, the basic assumption is that high microstrain values appear as the result of vacancy arrangements in the directions where the layers consist of heterogeneous atoms (Pb and Te). The point to be emphasised is that the values of the kind were measured in all samples, meaning they are not resulting from B atoms disposition. If so, such values

would not be measured in the sample doped with 8 %.

Table 7. Microstrain parameters obtained by the simplified integral-breadth methods.

		$\varepsilon (10^{-3})$			
		$h\ 0\ 0$	$h\ h\ 0$	$h\ h\ h$	$h\ k\ k$
PbTe	$\langle \varepsilon_{C-C} \rangle^*$	0.468	0.394	0.093	-
	$\langle \varepsilon_{C-G} \rangle^{**}$	0.648	0.656	0.122	-
	$\langle \varepsilon_{G-G} \rangle^{***}$	0.874	0.875	0.189	-
PbTe+B(1%)	$\langle \varepsilon_{C-C} \rangle$	0.793	0.768	0.543	0.268
	$\langle \varepsilon_{C-G} \rangle$	0.963	0.979	0.637	0.499
	$\langle \varepsilon_{G-G} \rangle$	1.210	1.240	0.873	0.674
PbTe+B(3%)	$\langle \varepsilon_{C-C} \rangle$	0.896	0.845	0.358	0.085
	$\langle \varepsilon_{C-G} \rangle$	1.120	1.150	0.546	0.304
	$\langle \varepsilon_{G-G} \rangle$	1.430	1.470	0.736	0.426
PbTe +B(8%)	$\langle \varepsilon_{C-C} \rangle$	0.551	0.508	0.320	0.152
	$\langle \varepsilon_{C-G} \rangle$	0.714	0.716	0.440	0.342
	$\langle \varepsilon_{G-G} \rangle$	0.921	0.929	0.612	0.469

Upper limit of microstrain from the simplified integral-breadth methods: \* Cauchy-Cauchy function, \*\* Cauchy-Gauss function, \*\*\* Gauss-Gauss function.

Generally, crystallite domain sizes both for the Warren-Averbach and the simplified integral-breadth methods show higher crystallinity degree in the samples doped with 1 and 8 % (these two samples have also the highest isotropic displacement parameters) and lower one in a pure sample and the sample doped with 3 %. Therefore, the crystallinity degree increases up to the sample doped with 1 % of B; aftermath it decreases in the sample doped with 3% of B, and increases again in the sample doped with 8% of B. Likewise, this trend may be noticed in microstrain parameter calculations, along each measured crystallographic direction. Graphic



illustrations of diffraction-line broadening measurements are shown in Figures 2 and 3.

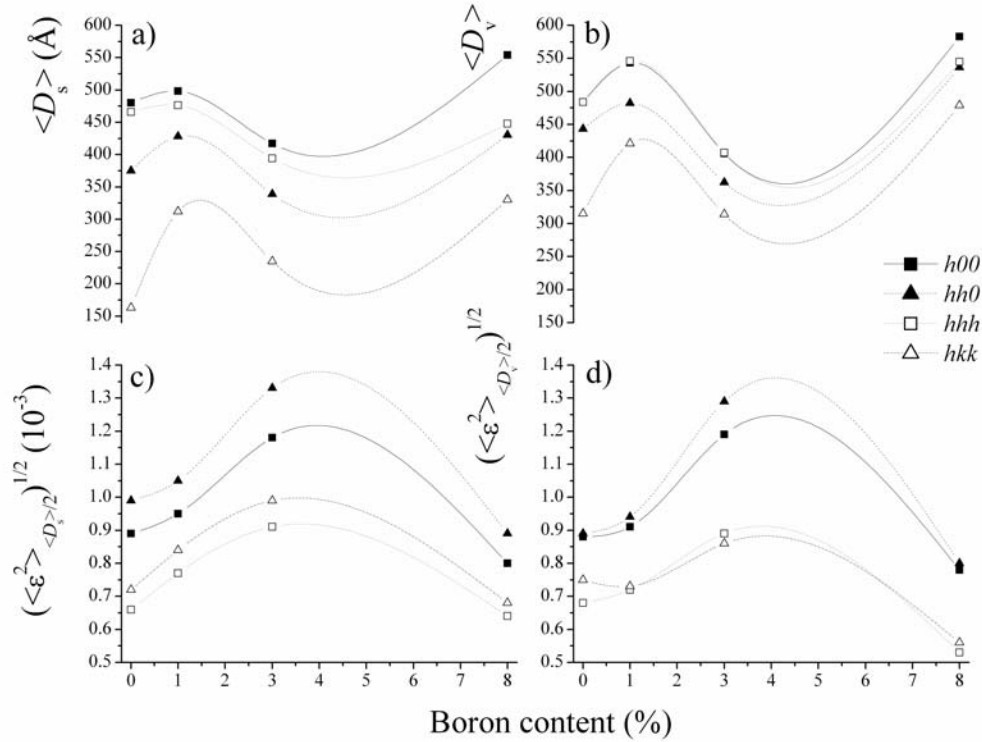


Figure 2. Graphic illustrations of crystallite: a) surface-weighted domain sizes, b) volume-weighted domain sizes, and c) RMSM averaged over the distance  $\langle D \rangle_s$ , d) RMSM averaged over the distance  $\langle D \rangle_v$  obtained by Warren-Averbach method.

## CONCLUSION

The achieved results of structural and microstructural measurements, par excellence unit-cell and microstrain parameters indicate that B atoms embedding did not generate disorder in PbTe-type structure. The disorder increases until the sample has been doped with 3 % and then rapidly falls down with the sample doped with 8 % of B. So, if contents of B atoms in the PbTe structure were limited they would be expelled as an

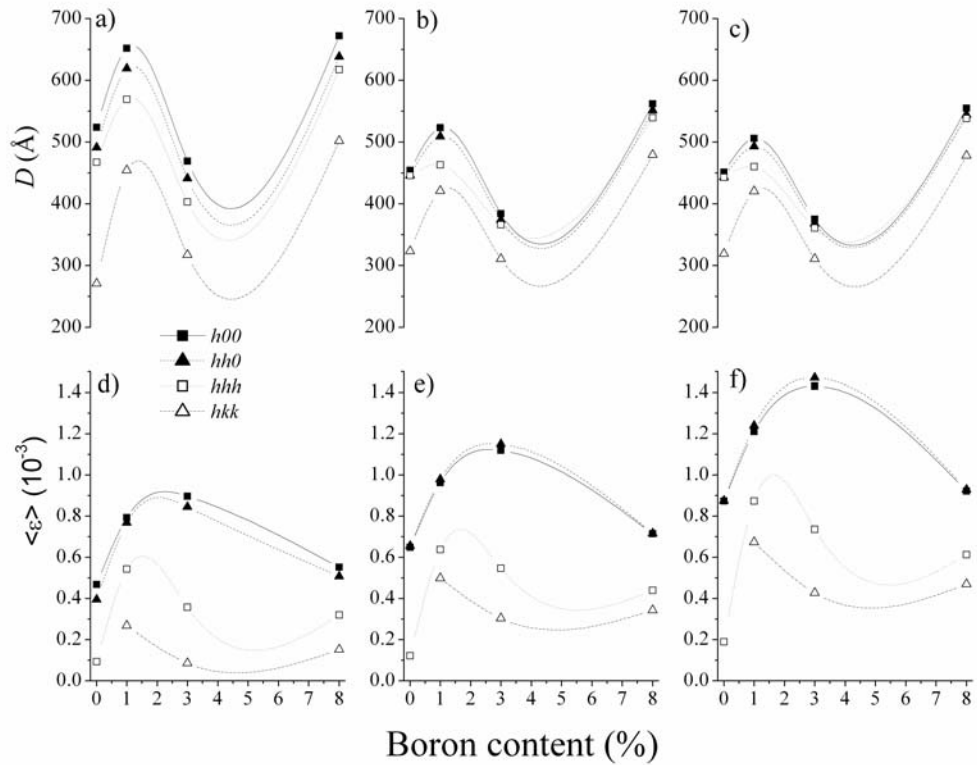


Figure 3. Graphic illustrations of volume-averaged domain sizes: a) Cauchy-Cauchy function, b) Cauchy-Gauss function, c) Gauss-Gauss function, and upper limit of microstrains: d) Cauchy-Cauchy function, e) Cauchy-Gauss function, f) Gauss-Gauss function obtained by the simplified integral-breadth methods.

extra phase in the sample doped with 8 %. Have B atoms occupied interstitial site-positions or filled-up vacancies or maybe both? Since these are real crystals, the crystal lattice defects are expected to appear. Schottky-type defects appear when atoms or ions are of approximate dimensions; consequently, the atom distribution in interstitial site-positions is difficult one. Frenkel-type defects consist of either interstitial atoms or ions and vacancies in a crystal lattice. Small cations and big anions are favoured for this type of defects. The foremost assumption is that B atoms, mostly already filled-up, formed vacancies in layers with the highest microstrain

parameters:  $[h00]$  and  $[hh0]$ . Since Pb and Te atoms are of approximate radii, Schottky-type defects are expected. This means B atoms sited unattended vacancies. Considering B atomic radius, which is in comparison to Pb and Te atoms very small one, a certain amount of B atoms must have sited interstitially into the structure. Higher values of isotropic displacement parameters of doped samples in comparison to the pure one can be explained in the manner that B atoms increased overall values of Pb and Te atoms. So, the crucial conclusion is that B atoms predominantly filled-up vacancies and, to less extent, degree sited into PbTe structure interstitially.

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