Residential Community Open-Up Strategy Based on Prim’s Algorithm and Neural Network Algorithm

Ximing Lv1,2, Ang Li3, Shunkai Zhang3, Jianbao Li3

1School of Mathematical Sciences, Inner Mongolia University, Hohhot, China
2School of Statistics and Mathematics, Inner Mongolia University of Finance and Economics, Hohhot, China
3School of Finance, Inner Mongolia University of Finance and Economics, Hohhot, China

Email: lvximing@vip.163.com

Abstract

“Open community” has aroused widespread concern and research. This paper focuses on the system analysis research of the problem that based on statistics including the regression equation fitting function and mathematical theory, combined with the actual effect of camera measurement method, Prim’s algorithm and neural network to “Open community” and the applicable conditions. Research results show that with the increasing number of roads within the district, the benefit time gradually increased, but each type of district capacity is different.

Keywords

Open Community, Regression Analysis, Prim’s Algorithm, Graph Theory, Neural Net-Work Algorithm

1. Introduction

Capillaries are reticular throughout the body, connecting arteries and veins. If the capillary is clogged, it will affect the blood flow and material exchange between arteries and veins. For urban traffic, “capillaries” are small roads that people are not interested in. If the “capillaries” blocked, then the “artery” and “vein” are no longer efficient [1]. How to solve the problem of traffic congestion by reasonable “open community” to improve the density of the road network is the focus of our study.

In order to study this huge problem, we decided to establish a mathematical model, and then empirical analysis. This requires us to establish a suitable index system, to evaluate the “open community” to control the role of road congestion.
After analysis, we established the following index evaluation system (Figure 1).

Road capacity, we can use a certain vehicle through a certain area of the minimum time to measure. The term “the benefit time” is defined as the time difference between a roadway around a residential area that permits traffic and does not allow traffic. The “the benefit time” is determined by the number of lanes and the speed, and the speed is related to the traffic density.

2. Data Acquisition and Analysis

2.1. Regional Analysis and Selection

As of September 11, 2016, there were 23 provinces, 4 municipalities, 2 special administrative regions and 5 autonomous regions in China. A total of 660 one, two, three-tier cities, each city car capacity and community structure is different, in order to study the problem in a better environment, select a suitable city is essential [2].

2.1.1. The Selection of Hohhot Region

Region selection reason:

1) Motor vehicle ownership is more appropriate, the majority of private cars, Hohhot, China can represent most of the city level, and there is great room for optimization.

2) This city is located in the plateau area. Roads are mostly straight; car congestion is almost free from geographical factors.

3) Residential area characterized as “Large mixed, small settlements”, forming a number of residential circle, conducive to the investigation and research.

Based on the above reasons, the selected research city is Hohhot, and the selected community is the representative district in this city.

2.1.2. The Selection of Residential Areas

According to the data obtained from the traffic management department of Hohhot, as shown in the blue area for most of the private car owner residential area, the figures (Figure 2) shown are the percentage of private car ownership in the area. In our data, we selected the smallest percentage (red five-pointed star “★” mark) area and representative area, as our research area and field observation area. Traffic flow around it can be approximated according to the following formula:

Traffic flow around the residential area = total traffic volume × The percentage.

Figure 1. The following index evaluation system.
2.2. Acquisition of Traffic Flow Data

2.2.1. The Average Hourly Traffic Data Acquisition
Through the “2011-2013 focus on environmental protection in key urban road traffic noise monitoring situation (2014)”, we found that the average hourly traffic volume in Hohhot was 2231 Vehicle/hour [3].

2.2.2. The Trend of the Daily Traffic Volume in Hohhot
Through the study of many authoritative data, we find that the trend of traffic flow in many cities is “double hump [4]” (Figure 3).

After a lot of data query, we found that there is a function similar to the “double hump”, through the modification and adjustment of this function, we get a “double-like hump” function (Figure 4).
In the follow-up analysis, the total traffic volume of the whole city in different time periods will be calculated by this function.

3. Preliminary Results

Through the analysis of the problem, we choose an algorithm in graph theory—Prim’s algorithm [5] [6] [7] to resolve this issue. It finds a subset of the edges that form a tree that includes every vertex, where the total weight of all the edges in the tree is minimized. The algorithm operates by building this tree one vertex at a time, from an arbitrary starting vertex, at each step adding the cheapest possible connection from the tree to another vertex. We believe that Prim’s algorithm can be a good solution to this problem.

In general, area around the crossroads can be formed well shape(Figure 5).

Assume the gate is at points A and D, so departure from $A_1$ and $A_2$ or $D_1$ and $D_2$ the departure traffic is the same. So this situation can be simplified into the following road network simulation map (Figure 6).

3.1.1. Traffic Velocity-Density Relation Model

In order to obtain the necessary data, we use the Traffic Engineering photogrammetry [8] [9] [10]. We were erected VCR in Wulanchabu East Road and the pedestrian bridge at University Road. Finally, select a number of private cars in the video, calculate the speed. Assuming constant speed, select one of the representative speed as the fitting data points in the speed value, in this selection, we assume that the vehicle travels at a constant speed and then uses the representative velocity as the velocity value in the fitted data points, Through the "double hump" function and the surrounding area traffic flow calculation formula, calculate the density of different time periods. A total of 24 groups were selected (Figure 7).

After obtaining the data, we are ready to use MATLAB software for regression

$$y = \left( \left( \frac{x}{4} - 3 \right)^2 + 0.5 \right) \times e^{\left( \frac{x}{4} - 3 \right)^2 + 0.1} \times 1000$$  (1)

In order to quantitatively express the relationship between density and velocity, we then carry out different degrees of regression analysis in order to find the function expression between the two.

### 3.1.2. Linear Regression Models

Its linear regression model is shown in Figure 8.

1) **Square regression equation**  
   Its square regression model is shown Figure 9.

2) **Cubic regression equation**  
   Its cubic regression model is shown in Figure 10.

3) **Neural Network Optimal Regression**  
   We use MATLAB software for neural network Levenberg-Marquardt [14] [15] [16] operation. Set Training 70%, Validation 15%, Text 15%, to obtain the optimal regression curve (Figure 11).

   Remnant analysis of neural network and raining, Validation, Text of the correlation coefficient are shown in Figure 12 and Figure 13.

   After several iterations, we find that the correlation coefficient is optimal when the high-order regression equation, but the correlation coefficient change from the second order is not particularly obvious, so we then use second-order regression equation as a function of speed and density relational expression.
Figure 8. The linear regression curve.

Figure 9. The square regression curve.

Figure 10. The cubic regression curve.

Figure 11. The neural network optimal regression curve.
3.1.3. Put Forward the Mathematical Model

According to the Prim’s algorithm and permutation and combination method, we simulate the driver’s route selection method:

1) In the node a wait, in front of the fork in the road 1, 2, ..., after selection into step 2.

2) After the observation, select the lowest traffic flow in the fork in the road,
to reach the next node, go to step 3.

3) The node is the end of the loop term to stop, if not the end, continue with step 1 cycle.

In the steady state, with the formula for calculating the profit time to get this set of formulas:

\[
\Delta T = \sum_i \left( T_i^1 - T_i^2 \right) = \sum_i \left( T_i^3 - T_i^4 \right) = \sum_i \left( T_i^5 - T_i^6 \right), \quad (i = 1, 2, 3 \ldots)
\]  

(2)

In which, \( T_i^1 \) is the commuting time required before opening section Yi, \( T_i^2 \) is the commuting time required after opening section Yi, \( T_i^3 \) is the length of the before opening section Yi/the speed of the Vehicle on the road before opening section Yi, \( T_i^4 \) is the length of the after opening section Yi/the speed of the vehicle on the road after opening section Yi, \( T_i^5 \) is the length of the before opening section Yi/the traffic density of the before opening section Yi, \( T_i^6 \) is the length of the after opening section Yi/the traffic density of the after opening section Yi.

3.2. Simple Model Simulation

3.2.1. Single-Lane Community

By simulating the simplest cell structure, we can obtain the following road network simulation map (Figure 14).

Let AB segment be \( n_1 \) lane, BD segment be \( n_2 \) lane, CD is \( n_3 \) lane, AC segment is \( n_4 \) lane.

According to the driver routing method, we can assume that in the case of stability, AE and AC road traffic density is the same. Let this traffic density be \( \rho \), And traffic flow density caused by traffic flow in other directions is denoted by \( \rho_e, \rho_s, \rho_w \). After opening the cell, the density of each section is

The ratio of traffic density between AE and AC links is \( 1:1 \)

\[
AE = \rho, \quad AC = \rho
\]

(3)

When the vehicle arrives at point E, the traffic density of EF and EB sections is equal. The ratio of traffic density between EB and AE is \( (1 + n_1):1 \):

\[
EB = \frac{\rho \times 1}{1 + n_1}, \quad EF = \frac{\rho \times 1}{1 + n_2}
\]

(4)

When the vehicle arrives at point B, the traffic density of EB and BD is \( n_1:n_2 \):

\[
BD = \frac{\rho \times n_1}{(1 + n_1) \times n_2}
\]

(5)
When the vehicle arrives at the point F, the traffic density of the FD section comes from the traffic density of the EF section and the CF section:

$$\rho_{FD} = \frac{\rho_{EF} \times n_1}{n_3} + \frac{\rho_{CF}}{n_3}$$  \hspace{1cm} (6)

When the vehicle arrives at point C, the ratio of the traffic flow density of CF road segment to the traffic flow density of AC link is $n_3 : n_4$:

$$\rho_{CF} = \frac{\rho \times n_4}{n_3}$$  \hspace{1cm} (7)

Before the “Open community”, the density (Figure 15) of each link is:

$$AB = \rho_1, \hspace{0.5cm} AC = \rho_1, \hspace{0.5cm} BD = \frac{\rho \times n_1}{n_2}, \hspace{0.5cm} CD = \frac{\rho \times n_4}{n_3}$$  \hspace{1cm} (8)

Let $\Delta T$ be the time gain after opening the cell:

$$\Delta T = \left\{ \begin{array}{l}
\frac{n_1}{n_1 + 1} \left[ \frac{Y_1}{f(\rho + \rho_1)} - \frac{Y_1}{f(\rho + \rho_1)} \right] + \frac{2 \times Y_2}{f\left(\rho + \frac{\rho_1}{n_3} + \rho_1\right)} \\
\frac{2 \times Y_2}{f\left(\rho + \frac{\rho_1}{n_3} \times n_2\right)} + \frac{1}{n_1 + 1} \left[ \frac{2 \times Y_2}{f\left(\rho + \frac{\rho_1}{n_3} + \rho_1\right)} - \frac{2 \times Y_2}{f\left(\rho + \frac{1}{n_1}\right)} \right] \\
\frac{Y_1}{f\left(\rho + \frac{\rho_1}{n_3} + \rho_1\right)} - \frac{Y_1}{f\left(\rho + \frac{\rho_1}{n_3} + \rho_1\right)} + \frac{n_4}{n_1 + n_4} \left[ \frac{Y_1}{f\left(\rho + \frac{\rho_1}{n_3} + \rho_1\right)} - \frac{Y_1}{f\left(\rho + \frac{\rho_1}{n_3} + \rho_1\right)} \right] \end{array} \right\}$$  \hspace{1cm} (9)

3.2.2. T-Shaped Road District

By modeling a slightly more complex cell structure, we can obtain the following plot road network simulation.

Let $AB$ segment be $n_1$ lane, $BD$ segment be $n_2$ lane, $CD$ is $n_3$ lane, $AC$ segment is $n_4$ lane (Figure 16).

The ratio of traffic density between $AE$ and $AC$ links is $1:1$

![Figure 15. Open community net.](image_url)
Figure 16. T-shaped road district.

\[ AE = \rho, \ AC = \rho \]  \hspace{1cm} (10)

When the vehicle arrives at point \( E \), the traffic density of \( EB \) and \( EO \) sections is equal. The ratio of traffic density between \( EB \) and \( AE \) is \( 1 : \left(1 + n_1\right) \):

\[ EB = \frac{\rho \times 1}{1 + n_1}, \ OE = \frac{\rho}{1 + n_1} \]  \hspace{1cm} (11)

When the vehicle arrives at point \( B \), the traffic density of \( EB \) and \( BD \) is \( n_1 : n_2 \):

\[ BG = \frac{n_1 \times \rho}{\left(1 + n_1\right) \times n_2} \]  \hspace{1cm} (12)

The traffic density of the \( CF \) link is determined by the \( AC \) link:

\[ CF = \frac{\rho \times n_1}{n_3} \]  \hspace{1cm} (13)

When the vehicle arrives at point \( O \), the traffic density of \( EO \) is divided into \( OG \) and \( OF \):

\[ OG = \frac{1 \times \rho}{2 \times n_1 + 2}, \ FO = \frac{1 \times \rho}{2 \times n_1 + 2} \]  \hspace{1cm} (14)

The traffic density of the \( GD \) section is gathered by the traffic density of the \( OG \) link and the \( BG \) link:

\[ GD = \frac{\left[\frac{\rho \times n_1}{1 + n_1} + \frac{1 \times \rho}{2 \times n_1 + 2}\right]}{n_2} \]  \hspace{1cm} (15)

\( FG \) road traffic flow density from the \( OF \) section and the \( CF \) section of the traffic flow density from the pool, then:

\[ FD = \frac{\left[\frac{1 \times \rho}{2 \times n_1} + n_1 \times \rho\right]}{n_3} \]  \hspace{1cm} (16)

Before the “Open community”, the density (Figure 15) of each link is:

\[ AB = \rho, \ BD = \frac{n_1 \times \rho}{n_2}, \ CD = \frac{\rho \times n_1}{n_3}, \ AC = \rho \]  \hspace{1cm} (17)

Let \( \Delta T \) be the time gain after opening the cell:
Through the empirical analysis of the study, we come to the following conclusions as Table 1.

Next, the evaluation system is used to test the traffic flow of the residential vehicles: the traffic volume density and the cell type are regulated under the premise of controlling the number of lanes around the cells.

After selecting the mean (175) and maximum (325) in the series data, we found that the same time, the yield time with the number of lanes in the district continues to lengthen. When only the density changes, the experiment chooses the peak data 325, the single-lane cell and the T-shaped road plot gain time is negative, which reflects the two communities on the morning and evening peak

Table 1. The benefit time of a single lane.

<table>
<thead>
<tr>
<th>Traffic density</th>
<th>The benefit time of a single lane</th>
<th>T-section of the benefits of time</th>
</tr>
</thead>
<tbody>
<tr>
<td>170</td>
<td>1.9222</td>
<td>2.6883</td>
</tr>
<tr>
<td>325</td>
<td>−50.33305</td>
<td>−17.1311</td>
</tr>
</tbody>
</table>
traffic capacity is limited. Community open only play a role in slowing traffic congestion, rather than cure.

4. Further Study

4.1. Actual Cell Simulation

4.1.1 Cross Road Community
This area is a selected area of the old district and the structure is relatively simple. The main road is a one-way street and the main road network structure marked in the map. The area around the road is a two-way street. Now we make an analysis of a problem about whether the area is conducive to ease the surrounding road congestion (Figure 17).

Figure 17. The cross-road actual cell.
Figure 18. The cross-road map.

Through the analysis of the actual map, we get the following road network simulation (Figure 18).

We set the $AB$ segment for the $n_1$ lane, $BD$ segment for the $n_2$ lane, $CD$ for the $n_3$ lane, $AC$ segment for the $n_4$ lane and 1 Lane inside the cell.

After the opening of the district:

According to the principles of the road drivers, the vehicle at $A$ point into the network. $AE$ and $AF$ sections is the same road density so the $AE = \rho$ and $AF = \rho$.

At $E$ point because of the density of the $EB$ segment and the $EO$ section, the density ratio of the two sections is $n_1 : 1$. Then,

$$EB = \frac{\rho}{n_1 + 1}, \quad EO = \frac{\rho}{n_1 + 1} \quad (19)$$

At $F$ point because of the density of the $FC$ segment and the $FO$ section, the density ratio of the two sections is $n_4 : 1$. Then,

$$FC = \frac{\rho}{n_4 + 1}, \quad FO = \frac{\rho}{n_4 + 1} \quad (20)$$

At $O$ point because the density of the $OH$ section and the $OG$ section is the same, the density ratio of the two sections is $1 : 1$ and the traffic volume is the sum of the $EO$ and $FO$ sections. Then,

The traffic flow density of $BH$ and $CG$ sections is fully inherited in $EB$ segment and $FC$ segment. Then,

$$OH = \frac{\rho + \rho}{2(n_1 + 1)}, \quad OG = \frac{\rho + \rho}{2(n_4 + 1)} \quad (21)$$

$HD$ and $GD$ sections of traffic flow density were inherited with $BH$ sections and $OH$ sections with $CG$ sections and $OG$ sections. Then,

$$GD = \frac{\rho \times n_4 + \rho \times n_4 + \rho}{2n_4 + 1}, \quad HD = \frac{\rho \times n_1 + \rho \times n_4 + \rho}{2n_2 + 1} \quad (22)$$

Before the district is not open, the density of each section:

$$AB = \rho, \quad BD = \frac{\rho \times n_1}{n_2}, \quad CD = \frac{\rho \times n_3}{n_3}, \quad AC = \rho \quad (23)$$

Final return time:
\[
\Delta T = \left(\frac{n_4}{n_1+n_1}\right) \times \left\{ \frac{\gamma_1}{f\left(D + D_n\right)} + \frac{\gamma_2}{f\left(D \times \frac{n_1}{n_2} + D_i\right)} - \frac{n_4}{n_1+n_1+1} \times \left[ \frac{\gamma_2}{f\left(D + D_n\right)} + \frac{\gamma_1}{f\left(D \times \frac{n_1}{n_2+1} + D_i\right)} \right] \right\}
- \frac{1}{n_1+n_1} \times \left[ \frac{\gamma_1}{f\left(D \times \frac{n_1}{n_2+1} + D_i\right)} + \frac{\gamma_2}{f\left(D \times \frac{n_1}{n_2+1} + D_i\right)} \right] - \frac{1}{n_2+n_1+1} \times \left[ \frac{\lambda_1}{f\left(D \times \frac{n_1}{n_2+1} + D_i\right)} + \frac{\lambda_2}{f\left(D \times \frac{n_1}{n_2+1} + D_i\right)} \right]
\] (24)

Through the calculation of the data, we come to the conclusion as Table 2:

We carried out the following inspection of the district traffic through the evaluation system:

We control the number of lines around the area and cell types as well as the traffic flow density adjustment. As a result, we find that the gain time synchronization increases with the increase of density. However, any cell has its upper limit capacity combined with the actual. So it cannot increase the density of traffic flow.

4.1.2. Park Type District

This area is within the selected region of a new park area (Figure 19). Garden-style design makes the complex structure of the district. Now, we make an analysis of this problem about more complex. The main road is a one-way street. The main road network structure marked in the map and the area around the road is a two-way street.

We will simplify the interior of this area (Figure 20).

Through the calculation of the data, we come to the conclusion as Table 3.

Through the analysis of Park Road District, we found that it is the same as the “cross road”. Through the study of the reasons, we find that the park road network structure is almost the same as the “cross road” community after the geometric transformation. This proves the universality of the “cross road” community.

5. Results

The State Council of the People’s Republic of China issued the Opinions on Further Strengthening the Management of Urban Planning and Construction, The issue of community Open community has become the focus of attention.

Table 2. The benefit time of cross section.

<table>
<thead>
<tr>
<th>Data Sheet</th>
<th>135</th>
<th>142</th>
<th>170</th>
<th>225</th>
<th>325</th>
</tr>
</thead>
<tbody>
<tr>
<td>Traffic density</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Cross section of the benefit time</td>
<td>3.2172</td>
<td>3.4178</td>
<td>3.9979</td>
<td>7.2684</td>
<td>26.1015</td>
</tr>
</tbody>
</table>
Some people disagree with the Open community of the community, taking into account their own security problems. After the opening of the community, with the passage of vehicles increased in the area, people’s travel security is not guaranteed, and into the area of mixed personnel, for people’s property security is also a great danger. Therefore, in the construction should pay attention to the construction of security measures and internal road construction in parallel to address people’s concerns.

After the open area, we can find: with the increasing number of roads within the district, the benefit time gradually increased, but each type of district capacity is different. For the urban planning department, it is possible to increase the road capacity within the area to be built, and the more roads in the area, the stronger the capacity of the area. For the district, has been built for transformation, the internal road construction should be appropriately reduced, not suitable for building too many roads. Because of its internal road structure is fixed, so
we must fully consider the choice of road width factors.

6. Conclusions

Through the establishment of the traffic velocity-density relation model, we can see that the one-way and the T-shaped roads have lower bearing capacity. For the simple structure of the internal road area, it cannot make too much traffic flow through, otherwise it will lead to cell blockage. Therefore, it is necessary to control the traffic volume in the district for traffic management. In the daily traffic peak hours, we must set traffic flow access restrictions to prevent excessive traffic flow.

Acknowledgements

This research was carried out with support of National Natural Science Foundation of People’s Republic of China (project 71261017 and 71661025).

References


