The Ratcheting Behaviour of Plain Carbon Steel Pressurized Piping Elbows Subjected to Simulated Seismic In-Plane Bending

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Abstract

In this paper, cyclic loading behavior of carbon steel pressurized piping elbows are described. Effects of internal pressure and bending moment amplitude on the ratcheting rate are investigated. The AF kinematic hardening model is used to predict the plastic behavior of the elbows. Material parameters and stress-strain data have been obtained from several stabilized cycles of specimens that are subjected to symmetric strain cycles. The results show that the maximum ratcheting strain occurred mainly in the hoop direction at flanks. Hoop strain ratcheting was found at intrados for individual specimen. Ratcheting strain rate increases with increase of the bending loading level at the constant internal pressure. The results show that the initial rate of ratcheting is large and then it decreases with the increasing cycles. The FE model predicts the hoop strain ratcheting rate to be near that found experimentally in all cases that $\frac{M}{M_i} \leq 1$.

Keywords

Pressure Pipe, Ratcheting, Carbon Steel, Nonlinear Kinematic Hardening Model, Cyclic Loading

1. Introduction

Piping systems, especially elbows are an important part of power plants components. When this components are cyclically loaded in the plastic regime, progressive plasctics deformation can occur by a combination of primary (steady) loading and secondary (cyclic) loading. This phenomenon is called as ratcheting and the accumulated plastic strain produced during above-mentioned cyclic deformation is called as ratcheting strain. The ratcheting

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is a phenomenon for the asymmetrical stress-controlled cycling and is important in designing above-mentioned structural components. Various models have been proposed for simulating cyclic and time independent behavior of materials such as Prager [1], Armstrong and Frederick [2], Ohno and Wang [3], Chaboche [4]-[6] plasticity models. Many efforts have been made to understand the ratcheting phenomena. Chen et al. [7]-[9] experimentally studied multiaxial ratcheting for pressurized low carbon steel elbows under reversed bending. It was shown that the maximum ratcheting strain occurred mainly in the hoop direction at flanks. Tasnim, et al. [10]-[12] simulated the plastic behavior of CS1026 and CS1020 carbon steels at cyclic loading. Zakavi et al. [13] studied the ratcheting behavior of the pressurized carbon steel (BS4360-43A) and stainless steel (304 L) straight pipe subjected to the seismic bending moment with the nonlinear combined hardening model using finite element code, ABAQUS. The finite element results were compared with those obtained from the experiments to evaluate the capability of the proposed AF model with isotropic/kinematic hardening rule to predict the cyclic loading behavior of the straight pipe. The results showed that the hoop-ratcheting strain predicted by FE analysis to be close to that found experimentally in all cases with \( M = MP^0.2 \leq 1 \). Otherwise, FE analysis gave overestimated values compared with the experimental data. The influences of mean stress and stress amplitude on ratcheting were evaluated using stress-controlled tests. Bari and Hassan [14]-[16] studied several kinematic hardening models for ratcheting prediction on steels. Koo and Lee [17] studied cyclic softening of the modified 9Cr-Mo steel at elevated temperatures. They showed that the cyclic softening behavior of the modified 9Cr-1Mo steel can invoke a ratcheting instability when the applied cyclic loads exceed a certain level of the ratchet loading condition. In this paper a finite element analysis with the nonlinear kinematic hardening model is used to evaluate ratcheting behavior of pressurized elbow subjected to dynamic bending moment. The results of this model are discussed for structures under various types of cyclic loads in references (Rahman, et al. [18]; Eslami, et al. [19]; Prager, [1]).

2. Materials and Methods

In this paper, a finite element code, ABAQUS, is used to study the ratcheting of carbon steel pressurized elbow subjected to cyclic bending loading. In the experimental tests [20], series of tests have been undertaken subjecting pressurized elbow specimens to rising amplitude dynamic (5 Hz, the resonant frequency) bending moments. Then, by conducting a series of finite element runs based on the nonlinear kinematic hardening model using the ABAQUS, the experimental tests are modeled and ratcheting data obtained. Then the two sets of results are compared with each other.

3. Nonlinear Kinematic Hardening Models

The kinematic hardening models are used to simulate the inelastic behavior of materials that are subjected to cyclic loading. The use of plasticity material models with isotropic type hardening is generally not recommended since they continue to harden during cyclic loading. The isotropic hardening model always predicts shakedown behavior, if creep is not considered [21]. The kinematic hardening plasticity models are proposed to model the inelastic behavior of materials that are subjected to repeated loading. For example, the Armstrong-Frederick [2] kinematic hardening model is suggested for the nonlinear strain hardening materials. Based on the Armstrong-Frederick nonlinear kinematic hardening rule, many constitutive models have been constructed to simulate the unaxial and multiaxial ratcheting of materials characterized by cyclic hardening or cyclic stable behaviors. The results of these models are discussed for structures under various types of cyclic loads in references.

The classical linear kinematic hardening rule and different nonlinear kinematic hardening models are available for the plastic analysis of structures. The nonlinear kinematic hardening model was first proposed by Armstrong and Frederick [2]. Nonlinearities are given as a recall term in the Prager rule. So that the transformation of yield surface in the stress space is different during loading and unloading. This is done by assuming different hardening modulus in loading and unloading conditions. The yield function for time independent plasticity, using the von-Mises yield criterion, is expressed as [22]:

\[
J_2 \sigma - X - k = 0
\]

where \( X \) is the back stress tensor, \( k \) the initial size of the yield surface, and denotes the von-Mises distance in the deviatoric stress space:
where $\sigma$ and $X$ are the stress and back stress tensors, and $\sigma'$ and $X'$ are the stress and back stress deviatoric tensors in the stress space, respectively. The nonlinearities are given as a recall term in the Prager rule:

$$
dX = \frac{2}{3} C d\varepsilon^p - \gamma X d\varepsilon^p
$$

where $d\varepsilon^p$ is the equivalent plastic strain rate, $C$ and $\gamma$ are two material dependent coefficients in the Armstrong–Frederick kinematic hardening model, and $\gamma = 0$ stands for the linear kinematic rule. The normality hypothesis and the consistency condition $df = 0$ lead to the expression for the plastic strain rate [22]:

$$
d\varepsilon^p = d \frac{\partial f}{\partial \sigma} = \frac{H(f)}{h} \left\{ \frac{\partial f}{\partial \sigma} : d\sigma \right\} \frac{\partial f}{\partial \sigma}
$$

where $H$ denotes the Heaviside step function: $H(f) = 0$ if $f < 0$, $H(f) = 1$ if $f \geq 0$ and the symbol $\langle \rangle$ denotes the MacCauley bracket, i.e., $\langle u \rangle = (u + |u|)/2$. The hardening modulus $h$ becomes:

$$
h = C - \frac{3}{2} \gamma X : \frac{\sigma' - X'}{k}
$$

In the case of tension-compression, the criterion and the equations of flow and hardening can be expressed in the form (Lemaitre and Chaboche, [22]):

$$
f = (\sigma - X) - k = 0
$$

$$
d\varepsilon^p = \frac{1}{h} \left\{ \frac{\sigma - X}{k} : d\sigma \right\} \frac{\sigma - X}{k} = d\sigma
$$

$$
dX = C d\varepsilon^p - \gamma X d\varepsilon^p
$$

$$
h = C - \gamma XSgn(\sigma - X)
$$

The evolution equation of hardening can be integrated analytically to give:

$$
X = \nu \frac{C}{\gamma} + \left( X_0 - \nu \frac{C}{\gamma} \right) \exp\left[ -\gamma (\varepsilon^p - \varepsilon^p_0) \right]
$$

where $\nu = \pm 1$ according to the direction of flow, and $\varepsilon^p_0$ and $X_0$ are the initial values, for example, at the beginning of each plastic flow.

### 4. Review of Experimental Set-up [20]

The experimental set-up for testing piping elbows under in-plane bending has been reported in reference [20]. The nominal pipe size was 2 inch NPS corresponding to an outside diameter of 60.3 mm. The component identification and relevant dimensions of the elbows are given in Table 1. For carbon steel (ASTM A106B) material,

<table>
<thead>
<tr>
<th>Component identification(^{\ast})</th>
<th>Thickness (mm), (schedule)</th>
<th>Bend Radius (mm)</th>
<th>Bend characteristic $H = tr^2/r^2$</th>
<th>Radius ratio $b = R/r$</th>
</tr>
</thead>
<tbody>
<tr>
<td>CLSI</td>
<td>3.91, (40)</td>
<td>76</td>
<td>0.37</td>
<td>2.7</td>
</tr>
<tr>
<td>CLXI</td>
<td>5.54, (80)</td>
<td>76</td>
<td>0.56</td>
<td>2.8</td>
</tr>
<tr>
<td>CSSI</td>
<td>3.91, (40)</td>
<td>51</td>
<td>0.25</td>
<td>1.8</td>
</tr>
<tr>
<td>CSXI</td>
<td>5.54, (80)</td>
<td>51</td>
<td>0.38</td>
<td>1.9</td>
</tr>
</tbody>
</table>

\(^{\ast}\)Components are labelled by a four-character coding: First character: C for carbon; Second character: L for long or S for short radius bends; Third character: S for standard weight or X for extra strong; Fourth character: I is used here to denote in-plane bending to differentiate from another programme concerned with out-of-plane loading.
specification and properties obtained by tensile tests data is given in Table 2. The parameters and section of the experimental results is shown in Figure 1. Pairs of 90° welding elbows [20] have, for symmetry, been tested simultaneously. The loading was applied in two stages. First, the test components were pressurized independently to their design pressure, calculated using the ASME Code formula. The internal pressure kept constant during testing. Next, the dynamic load to induce the cyclic bending was applied at the end nodes of the simulation model. It was specified as a sinusoidal force with a circular frequency. The frequency and design pressure of elbows is given in Table 3. Hoop strains at the crown reading from the gauges attached to the elbows at the crown positions (Figure 1).

5. Finite Element Arrangement

For all specimens the finite element code, ABAQUS, was used to study ratcheting behavior of pressurized elbows under simulated seismic bending moments. The elbows have a 1.50 m long pipework modeled by 28 elements. The most accurate element in the ABAQUS code for this type of structural system considering beam

![Figure 1. Elbow geometry, stress directions, angular coordinate and definition of important locations around the bend [20]). a = axial direction; h = hoop direction; ϕ = angular position around mid-circumference section containing E, C and I = 0° at C and positive towards E; C = crown positions (ϕ = 0°, 180°); E = extrados (ϕ = +90°); F = flank regions (defined by ϕ = ±45° about the crowns); I = intrados (ϕ = −90°).](image)

<table>
<thead>
<tr>
<th>Table 2. Material (Carbon steel) properties obtained by tensile tests.</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Material properties</strong></td>
</tr>
<tr>
<td>Young’s modulus</td>
</tr>
<tr>
<td>-----------------------</td>
</tr>
<tr>
<td>214 GPa</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Table 3. The frequency and design pressure.</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Component identification</strong></td>
</tr>
<tr>
<td>CLSI</td>
</tr>
<tr>
<td>CLXI</td>
</tr>
<tr>
<td>CSSI</td>
</tr>
<tr>
<td>CSXI</td>
</tr>
</tbody>
</table>
elements, pipe elements and elbow elements is the elbow element. Four types of elbow elements are available in the ABAQUS library, of which the two-noded element ELBOW31 was found to give the best results. ELBOW31 provides accurate predictions of the behavior of elbows under monotonic loading. In this paper, in order to predict the results, the tensile specimens were produced according with the materials properties that is given in Table 2.

The cyclic nonlinear constitutive model used in the FEM analyses in this study is derived from multiaxial formulations by Armstrong and Frederick. It is recommended that the model be calibrated with experimental data that is close to the expected strain range and loading history of the application. Stress-strain data is obtained from several stabilized cycles of specimens that are subjected to symmetric strain cycles. The material parameters $C$ and $\gamma$ determine the kinematic hardening component of the model. Three different ways of providing data for the kinematic hardening component of the mode can be given: using half-cycle test data, using single stabilized cycle, or test data obtained from several stabilized cycles. Stress-strain data can be obtained from several stabilized cycles of specimens that are subjected to symmetric strain cycles.

The calibration procedure consists of several cylindrical bar tests, one of which subjected to monotonic tension until necking and others were under symmetric strain-controlled experiments with different strains. During these calibration tests, the stress state must remain uniaxial.

From symmetric strain-controlled experiments, the equivalent plastic strain equals the summation of the absolute value of the change in longitudinal plastic strains:

$$\bar{\varepsilon}_p = \sum \Delta \varepsilon_{p(i)} = \sum |\Delta \varepsilon_i - \Delta \sigma_{exp} \cdot E|$$

where $\varepsilon_i$ total strain, $\sigma_{exp}$ is the measured stress and $E$ is the elastic modulus.

The equivalent back stress, $\bar{X}$, equals one-half of the difference in yield stress between the end of the tensile loading and first yield of the subsequent compressive loading.

These results, corresponding $(\bar{X}, \bar{\varepsilon}_p)$ data pairs may be plotted, and the kinematic hardening parameters, $C$ and $\gamma$, may be calculated by fitting Equation (10) to the data and selecting parameters minimize the sum of the square of the error between Equation (10) and the data.

For symmetric strain-controlled experiments, a typical curve with strain amplitude $\pm 0.75$ is shown in Figure 2. The results gained experimentally and from FE using nonlinear kinematic hardening model with $C = 2763.69$ Mpa, $\gamma = 17.66$ are detailed below.

![Figure 2. Typical cyclic loading curve with strain amplitude ±0.75 for carbon steel.](image-url)
6. Experimental and FE Results

Detailed results will be presented for four of the specimens tested (CLSI, CLXI, CSSI and CSXI) and summary results will be given for all tests conducted. Typical strain response in presence of ratcheting in FE results are shown in Figure 3.

All of the experimental ratcheting results from the tests and from FE analysis on specimens CSSI, CLSI, CLXI and CSXI are plotted in Figure 4 and Figure 5. Here, the strain for each cycle has been calculated as the average over the period of the test and plotted against M/M0.2. Figure 4 and Figure 5 show the data recorded for the crown surface.

The response of the specimens during these tests is illustrated in Figure 5(a). The dynamic bending moment experienced by the specimen has been plotted against the input displacement for each of the specimens CLSI, CLXI, CSSI and CSXI. In Table 4, the ratchet strains found experimentally over the test period and by FE
Table 4. Experimental and FE ratcheting data for specimen CSXI.

<table>
<thead>
<tr>
<th>Dynamic bending moment, $M$ (N·m)</th>
<th>$M/M_{cr}$</th>
<th>$M/M_t$</th>
<th>Experimental ratcheting data (µε/cycle)</th>
<th>FE analysis against moment levels (µε/cycle)</th>
</tr>
</thead>
<tbody>
<tr>
<td>4977</td>
<td>2.59</td>
<td>0.85</td>
<td>25</td>
<td>29.866</td>
</tr>
<tr>
<td>5727</td>
<td>2.74</td>
<td>0.98</td>
<td>50</td>
<td>58.1195</td>
</tr>
<tr>
<td>6068</td>
<td>2.79</td>
<td>1.05</td>
<td>450</td>
<td>1128.825</td>
</tr>
<tr>
<td>6136</td>
<td>2.88</td>
<td>1.06</td>
<td>750</td>
<td>1490.69</td>
</tr>
<tr>
<td>6409</td>
<td>2.94</td>
<td>1.09</td>
<td>1100</td>
<td>3850.6</td>
</tr>
<tr>
<td>6477</td>
<td>3.01</td>
<td>1.12</td>
<td>1500</td>
<td>4123.765</td>
</tr>
<tr>
<td>6613</td>
<td>3.06</td>
<td>1.14</td>
<td>2150</td>
<td>3340.5</td>
</tr>
<tr>
<td>6818</td>
<td>3.15</td>
<td>1.15</td>
<td>3100</td>
<td>3376.1145</td>
</tr>
<tr>
<td>6954</td>
<td>3.18</td>
<td>1.2</td>
<td>3700</td>
<td>4295.75</td>
</tr>
</tbody>
</table>

7. Results and Discussion

Results on four pairs of carbon, long and short radius piping elbows with two different thicknesses have been presented. The components were subjected to steady internal pressure and resonant, dynamic in-plane bending moments. The cyclic strain accumulation as a function of geometry and load level was assessed for all components. This paper, reviews the experimental observations and the FEA results of the structural ratcheting. Experimental and simulation results show that cyclic bending of elbows induces cyclic strain accumulation. Ratcheting has been found to be greater in the crown hoop direction than in the axial direction in all specimens, and increased rapidly once initiated. Ratcheting strains mainly occur in the circumferential direction. Such responses are imperative for understanding the ratcheting-fatigue failure mechanisms, and developing and validating simulation models for tubular structures. Despite that there are considerable advancements in cyclic plasticity.

Figure 5. (a) Experimental ratcheting data [20] and (b) FE analysis against moment levels for carbon steel.
models, they are still not robust enough to simulate the structural response when model parameters are determined from material response only.

Typical data obtained experimentally and from FE model for specimens CLSI to CSXI on the crown surface are shown in Figure 4 and Figure 5. For the carbon steel elbows, the onset of ratcheting did not start until moment levels of about $M/M_l = 1$. Complete set of data for specimens CSXI is presented in Table 4.

8. Conclusion

The important conclusion of this paper is to show the properties of nonlinear kinematic hardening model to predict the cyclic loading behavior of the structures. In this study, stress-strain data and material parameters have been obtained from several stabilized cycles of specimens that are subjected to symmetric strain cycles. Both experimental results and the FE analysis agree that ratcheting is influenced by the material stress-strain curve and load history. The rate of ratcheting depends significantly on the magnitude of the internal pressure, dynamic bending moment and material constants for nonlinear kinematic hardening model. The results show that the initial rate of ratcheting is large and then it decreases with the increasing cycles. The FE model predicts the hoop strain ratcheting rate to be near that found experimentally in all cases that $M/M_l \leq 1$. The ratcheting strains were found to be in general higher for the high thickness than for the low thickness elbows.

Acknowledgements

Late Appreciation is expressed to the technical staff of the Applied Mechanics Division of the Department of Mechanical Engineering at the University of Mohaghegh Ardabili (Iran) for their assistance with the work.

References


**Notation**

- \( t \) Pipe Thickness
- \( r \) Pipe mean radius
- \( E \) Young’s modulus
- \( M \) Applied dynamic moment
- \( M_y \) Yield strength
- \( M_{y,c} \) Elbow limit moment under out-of-plane bending
- \( s_m \) Allowable design stress intensity
- \( S_u \) Ultimate strength
- \( S_y \) Yield strength
- \( h = tR/r^2 \) Bend characteristic = \( tR/r^2 \)
- \( X \) Back stress tensor
- \( X' \) Back stress deviatoric tensor
- \( k \) Initial size of the yield surface
- \( C, \gamma \) Materials constants for kinematic hardening
- \( \varepsilon_p \) Plastic strain tensor
- \( \phi \) Angular position around the circumference of the bend (\( = 0' \) at the crown)
- \( f_n \) Test natural frequency
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