A Model of the Religious Transition

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ABSTRACT

The religious transition is the decline of religiosity with rising levels of income. The empirical robustness of the transition has been demonstrated. It appears that the transition is driven by the substitution of scientific knowledge for religious beliefs, which characterizes the process of modern economic growth. This note models the substitution process. A Solow model with CES technology generates the transition path with endogenous growth and reveals a direct link between the substitution parameter and the estimated transition parameter.

Keywords: Religious Transition; Religiosity; Religious Beliefs; Solow Model

1. Introduction

The religious transition is the decline in religiosity that follows from rising levels of income. The process has been analyzed empirically in Paldam and Gundlach [1] and [2]. This note is an attempt to explain the empirical results in the context of a simple growth model.

A religion is a particular bundle of largely immaterial ideas and beliefs. It is almost constant, though the bundle is adjusted marginally in the long run. Religiosity is the intensity by which people use their religion. That is, religiosity is the importance of (any) religion in all aspects of life. Religiosity is much more variable than religious beliefs.

In Paldam and Gundlach [1], religiosity is measured as an $R$-variable that is the dominating factor in 14 polled items from the World Values Survey [3]. These items are chosen to span as many religious aspects as possible. The $R$-variable is reported to be robust to changes in the composition of countries and items in the sample. With this operationalization of religiosity, a strong transition path becomes visible both over time and across countries. The transition path from high to low religiosity can be described by the function $R = R(y)$, where income ($y$) is measured as (log) GDP per capita. The function is governed by the transition parameter, which is reported to be robust across alternative samples and specifications.

In low income countries, religiosity is roughly twice as high as in high income countries. While the empirical facts are strong and robust, the explanation of the facts is more debatable, especially as the demand for religion is both for consumption and as a factor of production. Some explanations have been sketched in Paldam and Gundlach [1]. A key factor in the explanations is substitution. In the process of development, religious beliefs are replaced by scientific knowledge as a factor of production and religious institutions are replaced by secular institutions as a provider of collective goods such as education, healthcare, and social security.

We develop a simple Solow growth model with CES-production technology to explain the religious transition as a substitution process. The model uses two factors of production: Religious beliefs and scientific knowledge. Endogenous economic growth is driven by a sufficiently high elasticity of substitution, where religious beliefs (and religious institutions) are replaced by scientific knowledge (and secular institutions). In this setting, the implicit factor share of religious beliefs falls with rising levels of income, even in the presence of a constant stock of religious beliefs. We interpret the observed decline of the empirical measure of religiosity $R$ as the declining factor share of religious beliefs and show that the empirical estimate of the implied transition parameter is related to the substitution parameter of the CES technology.

2. A Religious Solow Model with Endogenous Growth

We consider an economy that produces a single output good with two factor inputs. The factor inputs are non-standard: religious beliefs $B$ and scientific knowledge $Z$, rather than labor and capital. The two factor inputs represent alternative ways of decision making that lead to different levels of output. It is assumed that the stock of...
religious beliefs is constant, while the stock of scientific knowledge can be accumulated over time. The stock of religious beliefs is maintained by religious institutions and the stock of scientific knowledge is maintained by secular institutions, such that any substitution of a factor of production is assumed to represent a proportional substitution of the respective institution (and vice versa)\(^1\). Each factor input has diminishing returns and is substitutable. Population is constant and normalized to 1. There is no exogenous technological change.

Given these assumptions, the output of the economy at time \(t\) is produced according to a CES production function

\[
Y_t = F(Z_t, B) = A \left[ \delta Z_t^{\rho} + (1 - \delta) B^{\rho} \right]^{1/\rho}, \tag{1}
\]

where \(Y_t\) is real output, \(Z_t\) is the stock of accumulated scientific knowledge, \(B\) is the constant stock of religious beliefs, and \(A, \delta,\) and \(\rho\) are parameters of scale, distribution, and substitution, which are assumed to satisfy the standard assumptions \(A > 0, 0 < \delta < 1,\) and \(\rho \geq -1^2\).

The elasticity of substitution, \(\sigma\), is given by

\[
\sigma = 1/(1 + \rho). \tag{2}
\]

Dividing both sides of Equation (1) by \(B\) generates the intensive form as

\[
\bar{y}_t = f(z_t) = A \left[ \delta z_t^{\rho} + (1 - \delta) \right]^{1/\rho}, \tag{3}
\]

with \(\bar{y}_t = Y_t/B\) and \(z_t = Z_t/B\). A constant fraction of output \(s = \bar{y}/Y\) is saved and invested to generate new scientific knowledge. The stock of scientific knowledge depreciates with a constant rate \(d = D/Z\). The growth rate of the economy, \(\gamma_t\), is given by the difference between the rates of knowledge accumulation and depreciation as

\[
\gamma_t = s \cdot f(z)/z - d. \tag{4}
\]

As \(z\) goes to infinity, the first term of Equation (4) approaches a positive constant if the elasticity of substitution is larger than 1. As is well known\(^3\), the CES technology with \(\sigma > 1\) generates endogenous income growth if the parameters satisfy the inequality condition

\[
s \cdot A \delta^{1/\rho} > d. \tag{5}
\]

This is shown in Figure 1. Whenever the marginal product of scientific knowledge (more generally, the marginal product of the input that can be accumulated) asymptotically achieves some lower bound that is greater than zero and larger than the value of the rate of depreciation, there will be a positive long-run rate of growth. Exogenous technological progress is not needed in this model as the engine of growth as long as the elasticity of substitution between scientific knowledge and religious beliefs is high enough to guarantee that the two curves in Figure 1 do not cross.

This simple growth model captures an important aspect of the observed long-run religious transition. The CES production function allows for output in the presence of only one of the inputs\(^4\). With no scientific knowledge, there is no substitution and hence no long-run growth, but there will be output in the presence of religious beliefs, \(B > 0\). So the modeling framework is in line with the Malthusian stagnation and the dominance of religious beliefs before the Industrial Revolution and with the rise of scientific knowledge and modern economic growth thereafter.

3. The Path of Religiosity in the Religious Solow Model

Religiosity \(R\) is defined as the weight of religious beliefs in decision-making. In the religious Solow model, \(R\) is interpreted as the weight of \(B\) in the production process. This weight is represented by the factor share \(\pi_b\) of \(B\), hence \(R = \pi_b\).

In a CES specification, the factor shares are functions of the distribution parameter, the substitution parameter, and the values of the factor inputs. The factor shares of \(B\) and \(Z\) are given by:

\[
R = \pi_b = \frac{(1 - \delta) B^{-\rho}}{\delta Z^{-\rho} + (1 - \delta) B^{-\rho}} \quad \text{and} \quad \pi_z = \frac{\delta Z^{-\rho}}{\delta Z^{-\rho} + (1 - \delta) B^{-\rho}} \tag{6}
\]

![Figure 1. Endogenous growth with scientific knowledge accumulation and constant religious beliefs.](Image 322x100 to 525x246)
With scientific knowledge rising to infinity and constant religious beliefs, the factor share of scientific knowledge will approach 100% in the limit \((\pi_s \to 1)\) if \(-1 < \rho < 0\), i.e., if \(\sigma > 1\). By implication, the factor share of religious beliefs will approach zero in the limit \((R = \pi_y \to 0)\) with rising scientific knowledge.

Rising scientific knowledge implies rising income because the substitution of \(Z\) for \(B\) is the engine of growth in this model. The decline of \(R = \pi_y\) that is generated by this endogenous growth is interpreted as the path of religiosity in the religious Solow model.

The transition path starts at a high level of religiosity, \(R^T\), which is typical for a traditional society where \(Z\) is approximately equal to zero. For \(Z \to \infty\), the level of religiosity approaches the modern level \(R^M\), which is predicted to be zero by the present model but which might turn out to be a non-zero constant if some decisions in life will remain to be determined by religious beliefs, independent of the level of scientific knowledge accumulation\(^5\). Thus, the model predicts that the transition path looks like the path in Figure 1(b) in Paldam and Gundlach [1].


Endogenous growth generated by a CES technology with \(\sigma > 1\) has been considered empirically implausible because it implies long-run trends of factor shares. Traditional factor shares of capital and labor appear to be trendless around one third and two thirds of total factor income. However, our empirical measure of religiosity does have a long-run trend, which is in line with our interpretation of religiosity as a factor share in the context of a CES technology.

Our interpretation invites the question whether and how the parameters of the religious Solow model (1) can be related to the slope parameter of the regression models estimated in Paldam and Gundlach [1]. They are of the general form:

\[
R_i = \alpha + \lambda y_i + \varepsilon_i, \tag{7}
\]

where \(i\) is a country index, \(\alpha\) is a regression constant, \(\varepsilon\) is an error term, and \(\lambda\) is the transition parameter.

Klump and de la Grandville [6] show that the steady state factor share of a normalized CES production function depends on the saving-investment rate and other parameters, including the substitution parameter. The saving-investment rate can be proxied by the level of per capita income. Using our own notation with population normalized to 1, the result by Klump and de la Grandville [(6), p. 290] reads

\[
\pi_x = \delta \left[A s_y \right]^{\frac{\mu}{\rho}}. \tag{8}
\]

Assuming that \(\sigma > 1\) and hence \(-1 < \rho < 0\), Equation (9) predicts a positive relation between \(s_y\) and \(\pi_x\). Since \(\pi_x\) and \(\pi_y\) add up to one, there must be a negative relation between \(s_y\) and \(\pi_y\) for \(\sigma > 1\) and hence a negative \(\rho\). Using the level of income \(\tilde{y}\) as a proxy for \(s_y\) and taking logs, we find

\[
\ln \pi_y = c + (1/\rho) \ln \tilde{y}, \tag{9}
\]

where \(c = -(1/\rho) \ln A - \ln \delta\) is a constant. Comparing Equation (9) with the regression Equation (7), it turns out that the estimated transition parameter, \(\lambda\), can be interpreted as a proxy of the inverse of the substitution parameter, at least if the scaling of the variables is ignored:

\[
\lambda = 1/\rho. \tag{10}
\]

This conceptualization of the religious transition critically hinges on an elasticity of substitution that is larger than one. The more detailed discussion in Paldam and Gundlach (2012) of substitution processes on the supply side and the demand side motivate the hypothesis of a large elasticity of substitution between scientific knowledge and religious beliefs. Further research has to show whether this elasticity is in fact large enough to explain the observed decline in religiosity with the suggested model of the religious transition.

5. Concluding Remarks

We have made an effort to make the model of the religious transition as simple as possible and we trust that the reader will agree that the model follows from basic economic theory. It explains the religious transition as the outcome of an endogenous growth process that is driven by substitution, and it links the substitution parameter of the CES technology to the estimated transition parameter. As a model of long-run growth, it is also in line with the stagnation before the industrial revolution and the dynamics of growth thereafter.

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REFERENCES


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