Nanoparticle Transportation and Brownian Diffusion in Planar Jet Flow via Large Eddy Simulation

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ABSTRACT
The nanoparticle transportation and Brownian diffusion in planar jet flow is simulated via large eddy simulation in this work. To thoroughly compare the Brownian diffusion with different particle size, we computed three particle diameter $d_p = 1$ nm, 10 nm and 50 nm in one simulation process simultaneously. The numerical results showed that at the flow developing stage, the particle mass concentration pattern develops as the flow vorticity develops. The distribution is nearly uniform at the lower reaches of the nozzle exit. When the jet flow is developing on, vortexes always carry the particle from upstream to downstream, from the central axis region to the outer mixing layer of jet. At the front of the jet flow, particles distribute more homogeneously for they have more residence time to diffuse from higher concentration region to the lower concentration region. The time averaged particle concentration distribution patterns are similar to Gaussian distribution form. The maximum concentration contributed by diffusion is present at the mixing layer near the nozzle exit. The farther away from the nozzle exit in the cross-stream direction, the smaller the concentration is. The maximum concentration contributed by diffusion is several orders smaller than that contributed by flow convection.

Keywords: Large Eddy Simulation; Planar Jet Flow; Nanoparticle Evolution; Diffusion

1. Introduction
Our surroundings are filled with thousand kinds of ultrafine particles. Mechanism of the motion of these nano-sized particles is of interest for decades [1-6], and ultrafine particles suspended in fluid have lots of application. When the particle diameter is in the order of nanometer, the Brownian diffusion instead of the inertial force is the dominant factor of the particle deposition [7]. However, the transport and deposition of nanoparticles in turbulent planar jet flow has not been examined in detail.

2. Model and Equation
The flow we concerned here is an incompressible planar jet flow containing relative high concentration nano-scale particles ($d_p = 1$ nm, 10 nm and 50 nm, assuming to be solid, spherical, and non-interacting in this work). The width of nozzle, $D$, is 5 mm. The inlet velocity at the nozzle, $U_0$, is 6 m/s. The computational domain is $x \times y = 20D \times 20D$ (as shown in Figure 1). The turbulence fluctuation intensity of the main inlet flow is given to be 5%. Time step size $\Delta t$ is set to be $2 \times 10^{-5}$ s. The fluid is isothermal at temperature of $T = 288$ K.

The planar jet flow, as a turbulent flow, can be characterized by a wide range of eddies, so the control equations here are solved by the LES (Large Eddy Simulation). After filtering by the length and time scales, the mass and momentum equations are as follows,

$$\frac{\partial \bar{\rho}}{\partial t} + \frac{\partial \rho \bar{u}_i}{\partial x_j} = - \frac{1}{\rho} \frac{\partial p}{\partial x_i} + \frac{\partial^2 \bar{\rho}}{\partial x_i \partial x_j} - \frac{\partial \tau_{ij}}{\partial x_j} \quad (1)$$

where $\bar{\rho}$ and $\bar{p}$ are the filtered velocity and pressure.

Methods which can be used in representing nanoparticle fields in fluid-particle systems include Lagrangian methods [8,9], moment methods [10,11], and sectional methods [12]. The equation employed here to describe the nanoparticle mass transfer is,

$$\frac{\partial Q}{\partial t} + \frac{\partial (\pi_i Q)}{\partial x_j} = D_P \frac{\partial^2 Q}{\partial x_i \partial x_j} + S_Q \quad (2)$$

where $Q$ is the species mass fraction, $S_Q$ is the source term, $D_P$ is the diffusivity and defined as [13];
Figure 1. Illustrate of the planar jet flow domain.

\[ D_p = \frac{kT C_{slip}}{3\pi \mu d_p} \]  (3)

where \( k = 13.8 \times 10^{-23} \text{ J/K} \) is the Boltzmann constant, \( T \) is the temperature, \( d_p \) is the particle diameter, and \( C_{slip} \) is the Cunningham slip correction factor.

\[ C_{slip} = 1 + \frac{\lambda}{d_p} \left( 2.514 + 0.8 \exp \left( -0.55 \frac{d_p}{\lambda} \right) \right) \]  (4)

Here, \( \lambda \) is the mean free path of air, which can be calculated based on the following formula [14]:

\[ \lambda = \nu \left( \frac{\pi m}{2kT} \right)^{\frac{1}{2}} \]  (5)

where \( \nu \) is the kinematic viscosity, \( m \) is the molecule mass of air.

In the computation, some diffusivities of nanoparticles are given in Table 1.

### Table 1. Diffusivities of nanoparticle with different diameters.

<table>
<thead>
<tr>
<th>( d_p ) (nm)</th>
<th>1</th>
<th>5</th>
<th>10</th>
<th>20</th>
<th>50</th>
</tr>
</thead>
<tbody>
<tr>
<td>( D_p ) ( (\text{m}^2/\text{s}) )</td>
<td>4.99e−6</td>
<td>2.02e−7</td>
<td>5.11e−8</td>
<td>1.34e−8</td>
<td>2.29e−9</td>
</tr>
</tbody>
</table>

3. Result and Discussion

3.1. Particle Mass Concentration

In this work, nanoparticles redistribute not only due to the air current, which will carry particles from the upstream to downstream, but also the Brownian motion, which is the presumably random moving of particles suspended in a fluid, and as a result, particles will be driven from the regions of higher concentration to lower, namely, Brownian diffusion acts to homogenize particles.

Figure 2 shows the instantaneous contours of nanoparticle mass fraction (Q) over the flow field at different time steps, from Figures 2(a) to (d) \( t = 100, 500, 1000 \) and 2000. As we can see, at the developing stage of flow in Figures 2(a) and (c), the particle mass concentration pattern develops as the flow vorticity develops. The distribution is nearly uniform at the lower reaches of the nozzle exit, where the value of \( Q \) is also highest, i.e. 0.1, and the region is finally stretched to nearly a quarter of the entire domain length (i.e. about 25 mm), seen in Figure 2(d). In the front of the jet flow, the primary vortex...
keeps rolling-up, transporting and mixing the particle to the fluid where did not carry particles. The concentration is lower at the core region of the swirl for the particles carried are less and less in the process of vortex rolling. In one word, when the jet flow is developing on, the pairing vortices always tend to carry the particle from upstream to downstream, from the central axis region to the outer mixing layer of jet.

When the flow is fully developed at the time step \( t = 2000 \), particles can be found in the whole jet central axis line with some particles have already carried out of the computational domain. It can also be found that at the front of the jet flow, particles distribute more homogeneous for they have more residence time to diffuse from higher concentration region, i.e. core region of the vortex, to the lower concentration region, i.e. outer region of the vortex.

Figure 3 shows the time averaged particle concentration distribution in the cross-stream direction at different flow positions (after the flow is fully developed, from time step 2000 to 3000). We can see that all the distribute patterns in the figure are similar to Gaussian distribution form. While the flow length \( x \) is increasing, the maximum of the concentration is reducing and the high value region is extending from the central axis line to the outer of the jet. Furthermore, the curves are steeper at the positions closing to the nozzle exit but flatter far away from the exit.

3.2. Diffusion Contribution

To thorough compare the Brownian diffusion with different particle size, we computed three particle diameter \( d_p = 1 \) nm, 10 nm and 50 nm in one simulation process simultaneously. It is shown previously in the particle distribution control equation, i.e.

\[
\frac{\partial \overline{Q}}{\partial t} + \frac{\partial (\overline{Q} \pi)}{\partial x_j} = D_p \frac{\partial^2 Q}{\partial x_j \partial x_j} + S_Q
\]  

(2)

The diffusion effect is relative to the second derivative of particle mass fraction and the particle diffusivity. It’s to say that the particle distribution and the particle size both contribute to particle diffusion. In a given case, the local particle distribution is the major influence factor. While for cases with different particle size, the particle diameter is also the major factor. For the three selective particle diameters, \( D_p \) for 50 nm is smallest, for 1 nm is far larger than 10 nm.

To show the tiny differences between the three cases, we also simulated a situation with \( D_p = 0 \), meaning there is no diffusion in the flow developing, as a reference \( Q_0 \). So the result of \( Q - Q_0 \) is meaning the concentration contributed only by the diffusion term. The contours of \( Q - Q_0 \) for different diameters are given in Figure 4 at time step \( t = 2000 \).

In Figure 4, it can be find that the maximum concentration contributed by diffusion is present at the mixing layer near the nozzle exit, between the static and injecting fluid. The farther away from the nozzle exit in the cross-stream direction, the smaller the concentration is. The concentration near the nozzle exit is much higher than that at the downstream of the jet flow too. It can also be seen that the maximum concentration contributed by diffusion is several order smaller than that contributed by flow convection. While diameter increasing, the particle diffusion ability reducing. As a result, the maximum concentration contributed by diffusion is decreasing too. Comparing Figures 4(a)-(c), the difference is much larger between (a) and (b) than that between (b) and (c). It can be explained from the \( D_p \) value difference for \( d_p = 1 \) nm, 10 nm and 50 nm.

4. Conclusions

The nanoparticle transportation and Brownian diffusion in planar jet flow is simulated via large eddy simulation in this work. To thorough compare the Brownian diffusion with different particle size, we computed three particle diameter \( d_p = 1 \) nm, 10 nm and 50 nm in one simulation process simultaneously. The main features are as follows.

1) At the flow developing stage, the particle mass concentration pattern develops as the flow vorticity develops. The distribution is nearly uniform, with the value of 0.1, at the lower reaches of the nozzle exit and the region is finally stretched to nearly a quarter of the entire domain length.

2) When the jet flow is developing on, vortexes always carry the particle from upstream to downstream, from the
3) When the flow is fully developed, at the front of the jet flow, particles distribute more homogeneous for they have more residence time to diffuse from higher concentration region, i.e. core region of the vortex, to the lower concentration region, i.e. outer region of the vortex.

4) The time averaged particle concentration distribution patterns are similar to Gaussian distribution form. Furthermore, the curves are steeper at the positions closing to the nozzle exit but flatter far away from the exit.

5) The maximum concentration contributed by diffusion is present at the mixing layer near the nozzle exit. The farther away from the nozzle exit in the cross-stream direction, the smaller the concentration is. The maximum concentration contributed by diffusion is several order smaller than that contributed by flow convection.

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