High Capacity Hydrogen Storage in Ni Decorated Carbon Nanocone: A First-Principles Study

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Abstract

Hydrogen adsorption and storage on Ni-decorated CNC has been investigated by using DFT. A single Ni atom decorated CNC adsorbs up to six H₂ with a binding energy of 0.316 eV/H₂. The interaction of 3H₂ with Ni-CNC is irreversible at 603 K. In contrast, the interaction of 4H₂ with Ni-CNC is reversible at 456 K. Further characterizations of the two reactions are considered in terms of the projected densities of states, electrophilicity, and statistical thermodynamic stability. The free energy of the reaction between 4H₂ and Ni-CNC, surface coverage and rate constants ratio meet the ultimate targets of DOE at 11.843 atm, 0.925 and 1.041 respectively. The Ni-CNC complexes can serve as high-capacity hydrogen storage materials with capacities of up to 11.323 wt.%. It is illustrated that unless the access of oxygen to the surface is restricted, its strong bond to the decorated systems will preclude any practical use for hydrogen storage.

Keywords

DFT, Hydrogen Storage, Nickel Complexes, CNC, Competitive Adsorption

1. Introduction

Hydrogen is considered to be an ideal fuel for many energy converters because of its low mass density and nonpolluting nature. Hydrogen can also be directly used in fuel cells in transportation applications. However, hydrogen storage, which is safe, effective and stable, remains a notable challenge to be overcome before hydrogen’s use in any automotive applications [1] [2]. Since the U.S. Department of Energy (DOE) has revised the targets for an on-board hydrogen storage medium (HSM), carbon-based materials have been considered candidates for a hydrogen storage media [3]. Accordingly, the medium should have a storage capacity of 4.50 wt.%

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by 2010 and 5.50 wt.% by 2015 [4] [5].

Carbonaceous nanostructures have attracted considerable interest due to the search for new materials with specific applications. Zero-dimensional C_{60}, one-dimensional nanotubes, and two-dimensional graphene sheets have been in focus due to their mechanical and electric transport properties [6]-[8]. Modification of the carbon nanostructure surface can be achieved by doping with B and Al [9] [10] or decorating with alkali metal [11], alkaline earth metal [12], transition metals (Ti, Ni, Pd and Pt) [13]-[17], and metal hydrides [18]. These modifications can be used to increase the interaction binding energy and therefore the hydrogen storage capacity. Lee et al. [19] have reported that functionalized SWCNT with Ni atoms can yield a storage capacity of 10 wt.%.

Various types of non-planar graphitic structures, such as carbon nanocones (CNCs), have been generated by using carbon arc and other related techniques [20]. CNCs are defined as hollow structures that are composed of carbon with a conical shape. The CNCs with different disclination angles have been observed in the pyrolysis of hydrocarbons [21]. Mechanical stability and sharp tip structures at the interface of CNCs usually have a lower density than carbon nanotubes, which makes them appropriate for field emissions due to the screening effect [22].

Carbon nanohorns (CNHs) are a subclass of the carbon nanocones CNCs family. CNHs have been selected and investigated for the use in hydrogen storage capacity because a significant amount of hydrogen is evolved at ambient temperatures [23]. Although the theoretical hydrogen storage on CNCs has not been heavily researched, nickel-doped CNCs are not reported. Ming-Liang Liao [24] investigated hydrogen adsorption behaviors of single walled carbon nanocones (SWCNCs) by molecular dynamics simulations. A. Gotzias et al. [25] examined hydrogen adsorption on CNHs and CNCs by using the grand canonical Monte Carlo method. Q. Wang et al. [26] tested the ability to store hydrogen by using the gradient corrected density functional theory. A. S. Shalabi et al. [27] investigated the reactions for hydrogen storage on Ti decorated carbon nanocones (CNC) by using density functional theory (DFT) calculations. Finally, J. Yang, et al. [28] presented an overview of experimental and computational techniques employed in the field of hydrogen storage materials research.

Theoretical studies have predicted that carbon-based materials decorated with transition metal (TM) atoms, such as Ti, Ni, Sc, and V, should be capable of binding up to five hydrogen molecules per metal atom with a binding energy between 7 and 12 kcal·mol^{-1} and a gravimetric density higher than 7 wt.% [11] [29]-[31]. Lee et al. [19] suggested that a single Ni atom deposited on a carbon nanotube could store up to five hydrogen molecules with a binding energy of 0.26 eV/H_{2} at a desorption temperature of 328 K [19]. Nickel decoration on carbonaceous nanostructures can be used to improve the capacity of these compounds toward hydrogen storage [19] [28] [32] [33]. To date, the focus of previous studies has been on hydrogen adsorption on single metal atom [14] [30]. It was suspected that metal clustering might have reduced the area of hydrogen holding and thus reduced the hydrogen uptake [34]. It has been observed that the low diffusion barrier of the Ni atom on the SWCNCS leads to high mobility of metal atoms and therefore leads to large formation energy of the Ni clusters that drives atomic aggregation. For the aggregation of metals on the SWCNCS, the major driving force is metal-to-metal attraction.

The aim of this work is to examine hydrogen storage capacity and the possibility of hydride formation upon hydrogen storage operation and to determine hydrogen storage capacity in the presence of oxygen molecules at the Ni decorated CNC. Finally, aggregation of the metal atoms on the adsorption media may occur (e.g., at ambient and elevated operational temperature) and should be carefully considered before one can assess the potential of the material for hydrogen storage.

2. Computational Methodology

Electronic calculations to determine structural optimization and total energy were performed using DFT. The DFT calculations were performed by simultaneously using Becke’s three parameter exchange function (B3) and the Lee Young Parr (LYP) correlation function [35]-[38]. B3LYP correctly reproduced the thermochemistry of many compounds, including transition metal atoms [39]-[42]. The analysis of electronic and thermochemical properties of CNC molecules was performed using the Gaussian 09 program [43]. The optimal geometries were visualized using the corresponding Gauss View software.

Full geometry optimizations, without symmetry constraints, were performed for CNC with a disclination angle of 120°, a height of 7 Å and with 72 carbon atoms. The optimal geometries of CNC, Ni-CNC, nH_{2}-Ni-CNC, nH_{2}-O_{2}-Ni-CNC and nH_{2}-Ni_{2}-CNC (n = 1 - 6) were determined at the B3LYP level of theory using 6 - 31 G (d, p) as the basis. This set uses Gaussian type functions (GTOs), adds d-type polarization functions to carbon,
f-type polarization functions to nickel, and p-type polarization functions to hydrogen. The adsorption mechanisms were determined with natural bond orbital (NBO) analysis and partial density of states (PDOS) plots, which are capable of providing a definitive description for charge redistribution. The projected densities of states (PDOS) and Fermi levels were performed using the Gauss Sum 2.2.5 program [44].

3. Results and Discussion

3.1. Structure of Pure and Ni Doped CNC

It is well-known that the decoration of carbonaceous nanostructures with TM atoms may be an attractive alternative to improve hydrogen storage capacity. Hence, the first SWCNC, decorated with single Ni atom, has been investigated.

The adsorption energy \( E_{\text{ads.}} \) of Ni atom on the surface was calculated as

\[
E_{\text{ads.}} = E_{\text{(Ni-CNC)}} - E_{\text{(CNC)}} - E_{\text{(Ni)}}
\]

where \( E_{\text{(Ni-CNC)}} \) and \( E_{\text{(CNC)}} \) are the total energy of the fully relaxed Ni-CNC and CNC, respectively. \( E_{\text{(Ni)}} \) is the energy of the isolated Ni atom. The negative binding energy corresponds to an exothermic process. The adsorption energy of Ni atom is \(-4.369\) eV, and the average distance between Ni atom and the nearest C atoms is \(1.843\) Å. This strong binding interaction may originate from the hybridization between the nickel atom and CNC as the atomic projected density of states (PDOS). The corresponding interactions to the pure Ni atom and doped Ni atom have been shown in Figure 1 and Figure 2. Due to low ionization potentials of the Ni atom, the s electrons are easily donated to the CNC. These donated electrons partially fill the unoccupied states of CNC as is indicated by the PDOS near the Fermi level (shown in Figure 1). The occupied s orbital of Ni, just below the Fermi energy at \(-6\) eV Figure 2(a), reduced in Figure 2(b) due to the charge transfer from the Ni atom to the CNC. Conversely, there is a finite probability for the CNC to donate back part of its received electrons to the low-lying d orbitals of the Ni atoms, resulting in strong hybridizations between the Ni and CNC.

The NBO analysis shows that a charge of \(0.590\) e is transferred from Ni to the CNC, as indicated by the decreased peak of Ni if it is supported on the CNC (Figure 2(b)). Consequently, the increased dipole moment of Ni-CNC (19.097 D), compared to the case of pristine CNC (12.774 D), is sufficient to enhance the van der Waal’s interaction between \(H_2\) molecules and the Ni-CNC. A fraction of the charge, between \(-0.223\) and \(-0.225\), is transferred from Ni and distributed to the nearest neighbor carbon atoms. This finding confirmed that Ni donates electrons to the neighboring C atoms of CNC, thereby resulting in the d-orbitals of the Ni atom overlapping with the sp\(^2\) orbitals of the C atoms. Such strong hybridizations can be observed from the resonated peaks in PDOS near \(-7\) eV, as shown in Figure 2(b).

![Figure 1. The partial density of states (PDOS) of (a) CNC (b) Ni doped CNC. The Fermi level is set to zero and indicated by a dotted line.](image)
3.2. H$_2$ Adsorption in Ni Doped CNC

Next, the interaction between the Ni/CNC complexes with H$_2$ molecules has been investigated. The average adsorption energy of a H$_2$ molecule at a Ni decorated CNC surface is obtained from the expression

$$ E_b(H_2) = \frac{E(nH_2_{-Ni-CNC}) - E(Ni-CNC) - E(nH_2)}{n} $$

(2)

In this equation, “$E$” is the total energy of the optimized structure, and “$n$” represents the number of adsorbed H$_2$ molecules. Negative energy indicates a stable exothermic process.

Figure 3 shows optimized geometries corresponding to a supported Ni atom that is surrounded by one to six H$_2$ molecules. The average adsorption binding energies and their corresponding distance per hydrogen molecule are presented in Table 1. From the viewpoint of adsorption geometry, it was noticed that the first 3 H$_2$ molecules were adsorbed on Ni by chemisorption. Further adsorption occurred as physisorption. This finding suggests that the first three hydrogen molecules interacted with the supported Ni-CNC via chemical bonds instead.
of the Kubas interaction. Under this condition, the H-H bonds were slightly elongated from 0.743 to 0.826 Å compared to the bond distance of 0.74 Å of an isolated H₂ molecule. This result confirmed that the bonds between H₂ and the supported Ni atom had both physical and chemical bond characteristics. The s electrons of hydrogen were slightly hybridized with the d orbital of Ni, which weakened the interaction between Ni and C atoms of CNC. Therefore, the average adsorption distances between the CNC and the decorated Ni atom were enhanced due to the subsequent addition of H₂ molecules. The corresponding Ni-C distance also elongated to between 1.896 and 1.926 Å. The average H₂-Ni adsorption distances were also found to have increased when more H₂ molecules were adsorbed. These results are reported in Table 1.

It is observed that there are three different mechanisms for hydrogen adsorption on metal decorated Carbonaceous compounds: 1) polarization under the effect of the electrical field induced by the supported metal atoms; 2) the hybridization between H₂ molecules and metal atoms that is modulated by the electrostatic potential induced by metal atoms; and 3) the formation of hydrogen super-molecules. The substantial charge redistribution (due to the Ni atoms donating their s electrons to the C-sp² in the CNC) can lead to a high electric field near the Ni atoms. Consequently, the electric field causes the polarization of H₂ molecules. In the interactions of H₂ molecules with a decorated Ni atom, the positive charge on the Ni atom and the Coulomb’s repulsive energy also reduces. Theoretically, the interaction of H₂ with TM basically arises due to the hybridization of the d levels of TM with H₂ levels. To elucidate the hybridization between the Ni atoms and H₂ molecules, the PDOS of three and four H₂ per Ni atom on CNC have been plotted in Figure 4 and Figure 5. In Figure 4, the peaks are centered at approximately −14 - 16 eV, which corresponds to the hybridization of the Ni 3d with the H₂ σ orbitals. The peaks that are centered at approximately 1 - 3 eV correspond to the hybridization of the Ni 3d with the H₂ σ* orbitals. Conversely, the hydrogen PDOS are shown in the range between −17 eV and −12 eV and are split into several peaks. This finding confirms the formation of bonding and antibonding states between the H₂ molecules, which results in the formation of the hydrogen super-molecule.

3.3. Interactions of 3H₂ and 4H₂ with Ni-CNC

Two types of interactions between nH₂ and Ni-CNC can be identified from Table 1: 1) irreversible interactions between nH₂ (n = 1 - 3) and Ni-CNC 2) reversible interactions between nH₂ (n = 4 - 6) and Ni-CNC. The irreversible interactions are outside the range of the desirable energy (−0.2 to −0.6 eV), as recommended by the DOE for practical applications. In contrast, the reversible interactions fall within this range. To characterize the nature of these two types of interactions, we considered the following theoretical descriptors.

3.3.1. Electronic Properties

The electronic descriptors, formation energy (ε), ionization potential (IP), electron affinity (EA), chemical potential (l), electronegativity (χ), chemical hardness(η) and electrophilicity index (ω) of the complexes nH₂-Ni-CNC (where n = 3, 4) were considered in Table 2.

The IP and EA can be calculated from the highest occupied (HOMO) and the lowest unoccupied (LUMO)
Figure 4. PDOS of (a) three H$_2$ molecules, (b) decorated Ni atoms in the (3H$_2$-Ni-CNC) system. The Fermi level is set to zero and indicated by a dotted line.

Figure 5. PDOS of (a) four H$_2$ molecules (b) decorated Ni atoms in the (4H$_2$-Ni-CNC) system. The Fermi level is set to zero and indicated by a dotted line.

**Table 2.** The total energy ($E_{\text{total}}/\text{Eh}$), formation energy ($\varepsilon$/eV), energy gap ($E_g$/eV), ionization potential ($I$/eV), electron affinity ($A$/eV), chemical hardness ($\eta$/eV), electronegativity ($\chi$/eV), and electrophilicity ($\omega$/eV) of the complexes nH$_2$-Ni-CNC (for n = 3, 4).

<table>
<thead>
<tr>
<th>System</th>
<th>$E_{\text{total}}$</th>
<th>$\varepsilon$</th>
<th>$E_g$</th>
<th>$I$</th>
<th>$A$</th>
<th>$\eta$</th>
<th>$\chi$</th>
<th>$\omega$</th>
</tr>
</thead>
<tbody>
<tr>
<td>3H$_2$-Ni-CNC</td>
<td>$-4253.369$</td>
<td>$-1.868$</td>
<td>0.498</td>
<td>5.558</td>
<td>5.061</td>
<td>0.249</td>
<td>5.309</td>
<td>2.009</td>
</tr>
<tr>
<td>4H$_2$-Ni-CNC</td>
<td>$-4254.548$</td>
<td>$-1.871$</td>
<td>0.489</td>
<td>5.555</td>
<td>5.066</td>
<td>0.244</td>
<td>5.310</td>
<td>2.046</td>
</tr>
</tbody>
</table>

molecular orbital energies using Koopmans’ approximation [45] where, $IP$—HOMO and $EA$—LUMO. The chemical potential $\mu$ and $\chi$ are defined as [45] $\mu = -\chi = -\frac{IP + EA}{2}$.

Pearson [46] introduced two parameters ‘chemical hardness ($\eta$)’ and ‘chemical softness ($S$)’ to account for the
stability of a molecule. Hardness ($\eta$) can also be expressed in terms of HOMO and LUMO, implying a finite difference approach [45], as follows: $\eta \approx \frac{IP + EA}{2} \approx \frac{E_{\text{LUMO}} - E_{\text{HOMO}}}{2}$. The softness can be defined as $S = \frac{1}{2\eta}$ [47]. Parr [48] defined electrophilicity index ($\omega$) as:

$$\omega = \frac{\mu^2}{2\eta} = \frac{Z^2}{2\eta}$$

which measures the energy stabilization when the molecule accepts an additional electrical charge from the environment. It is noted that a lower energy gap ($E_g$) between the LUMO and HOMO of a compound implies a greater and easier possibility of the electron transition between these energy levels. Additionally, a small value for $E_g$ for the compound is an indicator of lower chemical stability. In other words, the respective chemical hardness ($\eta$) should be low and electrophilicity ($\omega$), which is a parameter indicating reactivity, should be high.

The results presented in Table 2 show that the 4H$_2$-Ni-CNC shows a notably lower value of $E_g$ and $\eta$ and a maximum value compared to the 3H$_2$-Ni-CNC. The $\eta$ value for a compound essentially represents how chemically hard a compound is. Because 4H$_2$-Ni-CNC is chemically softer, it implies that it is a better candidate in electronic transport. The electrophilicity index ($\omega$) is one of the DFT based parameters which quantifies how reactive a molecule or compound is. It is clear from the present analysis that the lower $E_g$ and $\eta$ values and higher $\omega$ for the 4H$_2$-Ni-CNC (compared to the 3H$_2$-Ni-CNC compound) implies its favorable nature for the possible electronic transport and conductivity. Polarizability is closely associated with the softness ($S$) of a system, where the more polarizable a chemical system is, the softer the compound, and vice versa.

### 3.3.2. Thermodynamic Properties

The thermodynamics of the hydrogen storage reaction is one of the most fundamental properties of the hydrogen storage material. Thermodynamic properties indicate that the pressure of desorbed hydrogen and operating temperature are required for a fuel cell. The heat requirements for desorption and the potential for on-board recharge (or “reversibility”) are also associated with the thermodynamic properties of the storage reaction.

The thermodynamic properties of the 3H$_2$-Ni-CNC and 4H$_2$-Ni-CNC complexes can be calculated from standard statistical mechanical equations to include the finite-temperature translational, rotational and vibrational energies. The enthalpy ($H_r$) can be calculated as follows:

$$H_r = E_{\text{elec}}(T = 0) + E_{\text{vib}}(T = 0) + E_{\text{rot}}(T) + E_{\text{tra}}(T) = PV$$

where $E_{\text{elec}}(T = 0)$ is the total electronic energy, $E_{\text{vib}}(T = 0)$ is the zero point vibrational energy (ZPVE), which is a linear sum of the fundamental harmonic frequencies, and $E_{\text{rot}}(T)$, $E_{\text{tra}}(T)$ are vibrational, rotational, and translational contributions, respectively.

Similarly, the total entropy ($S$) can be expressed as

$$S = S_{\text{elec}} + S_{\text{vib}} + S_{\text{rot}} + S_{\text{tra}}$$

where $S_{\text{elec}}$, $S_{\text{vib}}$, $S_{\text{rot}}$, and $S_{\text{tra}}$ are the electronic, vibrational, rotational, and translational terms, respectively. The change in the standard Gibbs free energy is given by

$$\Delta G = \Delta H_r - T \Delta S$$

where $\Delta H_r = H_p - H_R$ and $\Delta S = S_p - S_R$, or simply

$$\Delta G = G_p - G_R$$

where $P$ = product, and $R$ = reactants.

The results of thermochemical properties of entropy, enthalpy, Gibbs free energy changes, thermal energies ($E_i$), and heat capacities at constant volume ($C_v$), for the reactions 8 and 9 processed from 100 K to 700 K are presented in Table 3.

$$3H_2 + \text{Ni-CNC} \rightarrow 3H_2\text{-Ni-CNC}$$

and

$$4H_2 + \text{Ni-CNC} \rightarrow 4H_2\text{-Ni-CNC}$$

It can be clearly deduced from this table that as temperature ($T$) increases, the values of enthalpy ($H$) and entropy ($S$) increase, while the Gibbs free energy ($G$) decreases. The negative Gibbs free energy ($G$) also indicates
an exothermic process, where the system releases energy to its surroundings during the adsorption process. The system then gradually reaches a stable condition of equilibrium. Thus, the reaction with \( G = -31.276 \text{ kcal/mol} \) at 100 K has a higher probability of occurring than that of \( G = 6.036 \text{ kcal/mol} \) at 700 K, (shown in Figure 6).

The polynomial regression

\[
y = a_5 x^5 + a_4 x^4 + a_3 x^3 + a_2 x^2 + a_1 x + a_0
\]

was subsequently applied to reactions (8) and (9) from 100 to 700 K after replacing \( y \) by \( T \) and \( x \) by \( \Delta G \). The residual sum of squares (rss = 0) value at \( \Delta G = 0 \) occurs at \( T = 603 \) K and 454 K, respectively. This implies that the two complexes, 3H\(_2\)-Ni-CNC and 4H\(_2\)-Ni-CNC, tend to release all hydrogen molecules above 603 and 454 K, respectively. In other words, the higher the amount of hydrogen molecules at the Ni-CNC interface, the lower temperature of hydrogenation. This can be explained by the relatively lower stability of the higher hydrogenated Ni-CNC. The other statistical thermodynamic parameters also characterized the two types of interactions, where \( \Delta S \), \( E_t \), and \( C_v \) values of the reversible interaction were always greater than those of irreversible interaction at the same temperature range.

3.3.3. Optimal Reaction Enthalpy

The temperature and pressure range at which a hydrogen storage system should operate is dictated by the environment and the requirements of the fuel cell. This approach translates vehicle operating constraints into thermodynamic constraints, which can be used to guide material development. Enthalpy is considered as the quantity of heat that must be added to (or subtracted from) the system during hydrogen release (or uptake). It is demonstrated that materials that have large enthalpies of desorption are undesirable because they require high temperatures for hydrogen release. In principle, a system with a small desorption enthalpy is capable of liberating

![Table 3. Temperature (T/K), Gibbs free energy \( \Delta G \) (kcal/mol), enthalpy change \( \Delta H \) (kcal/mol), entropy change \( \Delta S \) (cal/mol.K), thermal energy \( E_t \) (K.cal/mol), and heat capacity at constant volume \( C_v \) (cal/mol.K) of the complexes nH\(_2\)-Ni-CNC (for n = 3, 4).](image)

![Figure 6. Variations of Gibbs free energy (\( \Delta G \)) with temperature (T) of the complexes 1: 3H\(_2\)-Ni-CNC and 2: 4H\(_2\)-Ni-CNC.](image)
hydrogen at low temperatures but will require notably high pressures to recharge. Consequently, the enthalpy is an important engineering design parameter [28]. It is possible to identify a range of reaction enthalpies that satisfy the ultimate DOE targets of temperatures and pressures by using the van’t Hoff equation. These targeted temperatures and pressures are presented in Table 4. The van’t Hoff equation can describe the equilibrium between gas phase hydrogen and one or more condensed phases [49]:

\[ P_{H_2} = P_o \exp \left( \frac{-\Delta H}{RT} + \frac{\Delta S}{R} \right) \]

where \( P_{H_2} \) and \( P_o \) are referred to the equilibrium pressure and a reference pressure (typically atmospheric pressure), respectively, \( T \) is the absolute temperature, \( R \) is the gas constant, \( S \) and \( H \) respectively represent the change in entropy and enthalpy, which accompanies the hydrogen storage reaction to describe \( H_2 \) uptake in sorbent materials [28].

The thermodynamics of 4H\(_2\)-Ni-CNC complex have been calibrated with the ultimate targets of DOE at (−0.2 to −0.6 eV) for physisorption, (−40°C to 105°C) for (min./max.) temperature, (0.3/1.2MPa) for (min./max.) pressure, and (7.5%). The results shown in Table 4 illustrate that the equilibrium pressure of 1.2 MPa is equal to the ultimate target for maximum \( H_2 \) pressure that is required in the fuel cell. The desorption reaction requires a desorption enthalpy of −25.45 kJ/mol \( H_2 \), which is in agreement with the previous theoretical calculations of Yang et al. [28], who reported efficiency considerations that target the lower third of this range (\( H = 20 - 30 \) kJ/mol \( H_2 \)), are optimal.

In addition, the Langmuir isotherm is based on the monolayer adsorption on the active sites of the adsorbent. Langmuir suggested that the mechanism of the adsorption process is defined as \( A + S = AS \), where \( A \) is a gas molecule and \( S \) is an adsorption site. The direct and inverse rate constants are \( k \) and \( k^{-1} \). Surface coverage, which is defined as the fraction of the number of adsorption sites occupied in the equilibrium, is shown in Equation (12).

\[ K = \frac{k}{k^{-1}} = \frac{\theta}{(1-\theta)P} \]

where \( P \) is the partial pressure of the gas. Substituting the values of (0.925) and \( P \) (11.843 atm.) of the reversible reaction from Equation (9) gives the value (\( k = 1.041 \)).

### 3.4. Effect of Clustering Ni on CNC

For the next step, we examined the interactions and clustering effects of Ni ((e.g. Ni dimer at CNC) on the nature of hydrogen uptake. Full geometry optimizations at the B3LYP/6-31g (d, p) level of theory were carried out for the complexes nH\(_2\)-Ni\(_2\)-CNC (n = 2, 4, 6, 8, 10, 12). The corresponding geometry is shown in Figure 7. The average adsorption energy, of \( n = 2, 4, 6, 8, 10, 12 \) hydrogen molecules at Ni dimer decorated CNC, is obtained from the expression,

\[ E_b(H_2) = \left[ \frac{E(nH_2-Ni_2-CNC) - E(Ni_2-CNC) - E(nH_2)}{n} \right] \]

The average adsorption energies of with their geometric parameters are listed in Table 5. The results indicate that the bond length of Ni-Ni is 2.43 Å and it is elongated compared to that of the free Ni dimer at 2.01 Å. The bond lengths of Ni-C are higher than those in Figure 3, due to the internal interactions between the two Ni atoms that weaken the Ni–C interaction. Conversely, the interaction between CNC and Ni dimer weakens the Ni-Ni bond. The average adsorption energies of nH\(_2\)-Ni-CNC (n = 1 - 6) complexes are approximately −1.068, −0.926, −0.622, −0.468, −0.387 and −0.316 eV per \( H_2 \), which is stronger than that on Ni dimer at −1.057, −0.820, −0.546, −0.416, −0.333 and −0.278 eV, respectively. These values indicate that the formation of the Ni dimer also weakens the interaction between the \( H_2 \) and the doped CNC. Figure 7 shows the saturated hydrogen uptake on a Ni\(_2\) cluster. Note that 2 of the 6 adsorbed hydrogen molecules are completely dissociated and bonded in the atomic form (irreversible reaction), while the other four \( H_2 \) remain in molecular form (reversible reaction). This suggests that clustering of Ni not only alters the binding energy of the \( H_2 \) molecules but also the nature of H bonding. This adsorption behavior may be explained based on the charge-transfer mechanism discussed earlier. In fact, the average charge transfer from the Ni dimer of nH\(_2\)-Ni\(_2\)-CNC (n = 2 - 12) complexes to the CNC is only 0.48 and 0.39 eV per Ni atom, which is less than that of a single Ni atom of nH\(_2\)-Ni-CNC (n = 1 - 6).
Table 4. The (min./max.) temperature (T), (min./max.) pressure (P), free energy change (ΔG), enthalpy change (ΔH), and surface coverage (θ) of the highest hydrogen storage capacity reaction 4H₂ + Ni-CNC = 4H₂-Ni-CNC.

<table>
<thead>
<tr>
<th>T(°C/K)</th>
<th>P(MPa/atm.)</th>
<th>ΔG(kcal/mol)</th>
<th>ΔH(kJ/mol H₂)</th>
<th>θ</th>
</tr>
</thead>
<tbody>
<tr>
<td>105/378.15</td>
<td>1.2/11.8430792</td>
<td>−13.61</td>
<td>−25.33</td>
<td>0.925</td>
</tr>
<tr>
<td>105/378.15</td>
<td>0.3/2.9607698</td>
<td>−9.44</td>
<td>−25.33</td>
<td>0.744</td>
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<tr>
<td>−40/233.15</td>
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<td>−22.38</td>
<td>−25.45</td>
<td>0.925</td>
</tr>
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<td>−40/233.15</td>
<td>0.3/2.9607698</td>
<td>−19.81</td>
<td>−25.45</td>
<td>0.744</td>
</tr>
</tbody>
</table>

Table 5. Average adsorption energies of H₂ Eₐ(H₂) on Ni dimer at CNC complex, average distance between Ni and CNC d(Ni-CNC), average distances between Ni and H₂ (d_{Ni-H}), average H₂ bond length (d_{H-H}), charges (Q) in a.u. and the expected hydrogen storage capacity (wt.%) of the complexes nH₂-Ni₂-CNC (n = 2, 4, 6, 8, 10, 12). Complete surface coverage affords up to 24 Ni and 144 H₂. Energies are given in eV and lengths in Å.

<table>
<thead>
<tr>
<th>System</th>
<th>Eₐ(H₂)</th>
<th>d_{Ni-CNC}</th>
<th>d_{Ni-Ni}</th>
<th>Q_{Ni}</th>
<th>Q_{C}</th>
<th>Q_{H-H}</th>
<th>d_{H-H}</th>
<th>Capacity/wt.%</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>n = 1 - 2</td>
<td>n = 3 - 6</td>
<td></td>
<td></td>
<td></td>
<td></td>
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</tr>
<tr>
<td>2H₂-Ni₂-CNC</td>
<td>−1.057</td>
<td>1.873</td>
<td>0.475</td>
<td>0.475</td>
<td>−0.712</td>
<td>−0.066</td>
<td>0.842</td>
<td>2.084</td>
</tr>
<tr>
<td>4H₂-Ni₂-CNC</td>
<td>−0.820</td>
<td>1.913</td>
<td>0.378</td>
<td>0.375</td>
<td>−0.639</td>
<td>0.217</td>
<td>0.815</td>
<td>4.082</td>
</tr>
<tr>
<td>6H₂-Ni₂-CNC</td>
<td>−0.546</td>
<td>1.913</td>
<td>0.375</td>
<td>0.380</td>
<td>−0.641</td>
<td>0.230</td>
<td>0.816</td>
<td>6.001</td>
</tr>
<tr>
<td>8H₂-Ni₂-CNC</td>
<td>−0.416</td>
<td>1.913</td>
<td>0.391</td>
<td>0.394</td>
<td>−0.648</td>
<td>0.226</td>
<td>0.815</td>
<td>7.845</td>
</tr>
<tr>
<td>10H₂-Ni₂-CNC</td>
<td>−0.333</td>
<td>1.913</td>
<td>0.395</td>
<td>0.391</td>
<td>−0.651</td>
<td>0.225</td>
<td>0.814</td>
<td>9.617</td>
</tr>
<tr>
<td>12H₂-Ni₂-CNC</td>
<td>−0.278</td>
<td>1.913</td>
<td>0.395</td>
<td>0.395</td>
<td>−0.652</td>
<td>0.226</td>
<td>0.815</td>
<td>11.323</td>
</tr>
</tbody>
</table>

Optimized Ni—Ni free without CNC = 2.0085 Å.

Figure 7. Optimized structure of one to six H₂ adsorbed at nickel dimer doped CNC (nH₂-Ni₂-CNC) where n [1 - 6]. The circles in grey, blue and white denote carbon, nickel and hydrogen atoms, respectively. For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.
complexes to the CNC at 0.61 and 0.43 eV, respectively.

The expected gravimetric hydrogen storage capacities for \( nH_2-Ni_2-CNC \) (\( n = 2 - 12 \)) complexes are listed in Table 5. For \( nH_2-Ni_2-CNC \) (\( n = 2, 4 \)) complexes, the average adsorption energies of \( H_2 \) are \(-1.057 \) and \(-0.820 \) eV, respectively, which is beyond the highest adsorption requirement (\(-0.60 \) eV). The hydrogen storage capacities of these two configurations are calculated to be 2.084% and 4.082%, respectively. The average adsorption energies of \( nH_2-Ni_2-CNC \) (\( n = 6, 8, 10, 12 \)) complexes are \(-0.55, -0.50, -0.42 \) and \(-0.35 \) eV, respectively, which meet the DOE energy domain (\(-0.20 \) to \(-0.60 \) eV). The hydrogen storage capacities of these four configurations are expected to be 6.001%, 7.845%, 9.617%, and 11.323%, respectively. Consequently, these results indicate that the Ni-decorated \( C_72 \) stories capable of storing 144 hydrogen molecules attached to 24 Ni atoms. Thus, the hydrogen storage capacity is up to 11.323 wt.%, which exceeds the DOE target for 2015 [5].

3.5. Interaction of Oxygen with Ni Decoration

Decoration of different carbonaceous materials with metals has been investigated as an alternative to improve their capacity for hydrogen storage [9] [14] [19] [30] [32] [50] [51]. To follow experimental conditions, the effect of oxygen contamination from any residual atmosphere or pre-existing oxygen impurities on the nanotube surface, was examined. Rojas et al. [52] found that low quantities of oxygen present in the gas phase should yield the oxidation of the titanium atoms, even when hydrogen is stored in the system. They concluded that if the experimental system is exposed to air, titanium atoms on these surfaces are expected to oxidize to titanium dioxide. Felten et al. [53] studied the role of oxygen at the interface between titanium and carbon nanotubes. They observed that the presence of oxygen significantly weakened the Ti-CNT interaction and the Ti atoms at the surface preferentially bonded to oxygenated sites. Among these, oxygen molecules were found to be a strong inhibitor competitor for hydrogen adsorption.

To study the competition between \( O_2 \) and \( H_2 \) molecules at the Ni-CNC surface, we calculated the oxygen displacement energy that corresponded to the energy required to replace the adsorbed oxygen atom by \( nH_2 \) adsorbed hydrogen molecules. This displacement energy was calculated according to

\[
E_{dis} = E \left( O_2 - Ni-CNC \right) + n \cdot E_{H_2} - E_{O_2} - E \left( nH_2 - Ni-CNC \right)
\]

where \( E(nH_2-Ni-CNC) \) and \( E(O_2-Ni-CNC) \) denote the total energy of the substrate (Ni-CNC system) in the presence of \( nH_2 \) hydrogen molecules and \( O_2 \) oxygen molecules, respectively, \( n \) is the number of hydrogen molecules, and \( E_{O_2} \) and \( E_{H_2} \) are the energies of the isolated oxygen and hydrogen molecules respectively. In all cases, the values for \( E_{dis} \) are shown in Table 6, which indicate that the replacement of oxygen by hydrogen is energetically impeded.

The results show that the two O atoms bind strongly to a single Ni atom (\(-3.799 \) eV) and Ni-O bonds of 1.76 Å, which significantly weakens the Ni-C interaction (bonds dilated to 2.02 Å). Consequently, the quantity of oxygen present in the initial surface layer crucially controls the Ni-CNC interaction. This is because initial Ni deposition preferentially forms Ni-O bonds, strongly reducing the interaction between the hydrogen molecules and Ni-CNC.

The average adsorption energy of \( H_2 \) molecule at the surface of \( O_2-Ni-CNC \) was calculated according to

\[
E_a(H_2) = \frac{E \left( nH_2 - O_2 - Ni-CNC \right) - E \left( O_2 - Ni-CNC \right) - n \cdot E_{H_2}}{nH_2}
\]

where \( E(nH_2-O_2-Ni-CNC) \) and \( E(O_2-Ni-CNC) \) are defined earlier. The geometries obtained are shown in Figure 8. The results are reported in Table 6 and show that even at low oxygen concentrations, the interaction of the \( O_2 \) molecule with the Ni decoration on CNC leads to the irreversible formation of nickel dioxide, and displaces the hydrogen molecule. The resulting nickel dioxide produces a lower storage capability than nickel at CNC. The formation of nickel dioxide was confirmed by further theoretical calculations [54].

The destabilization of the \( O_2 \) molecule by the adsorbed hydrogen molecule may be expressed as

\[
E_b(O_2) = E \left( nH_2 - O_2 - Ni-CNC \right) - E \left( nH_2 - Ni-CNC \right) - E_{O_2}
\]

\( E_b(O_2) \) is shown in the third column of Table 6, where it is found that the addition of hydrogen molecules exhibited a decrease in the binding energy of the oxygen molecules. However, \( O_2 \) molecules remained strongly adsorbed on the surface, even in the presence six hydrogen molecules, with a binding energy of \(-2.633 \) eV.
Table 6. \( E_{\text{dis}} \) Oxygen displacement energy corresponding to the energy required to replace the adsorbed oxygen atom by \( n\text{H}_2 \) adsorbed hydrogen molecules. \( E_a(\text{H}_2) \) adsorption energy (per hydrogen atom) of hydrogen species on a surface where one oxygen molecule is already adsorbed on the Ni atom. \( E_b(\text{O}_2) \) binding energy of the oxygen molecule on a surface where \( n\text{H}_2 \) hydrogen molecules are already adsorbed on the Ni atom.

<table>
<thead>
<tr>
<th>System</th>
<th>( E_a(\text{H}_2) )</th>
<th>( \Delta E_{\text{dis}} )</th>
<th>( E_b(\text{O}_2) )</th>
<th>( d_{\text{Ni-CNC}} )</th>
<th>( d_{\text{ads}} )</th>
<th>( d_{\text{Ni-H}} )</th>
<th>( Q_{\text{Ni}} )</th>
<th>( Q_{\text{C}} )</th>
<th>( Q_{\text{H-H}} )</th>
<th>( Q_{\text{O}_2} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>1H_2-O_2-Ni-CNC</td>
<td>−0.694</td>
<td>−2.781</td>
<td>−3.475</td>
<td>2.018</td>
<td>1.658</td>
<td>0.789</td>
<td>0.729</td>
<td>−0.326</td>
<td>0.099</td>
<td>−0.623</td>
</tr>
<tr>
<td>2H_2-O_2-Ni-CNC</td>
<td>−0.376</td>
<td>−0.973</td>
<td>−2.698</td>
<td>2.019</td>
<td>1.659</td>
<td>3.941</td>
<td>0.789</td>
<td>0.734</td>
<td>−0.324</td>
<td>0.090</td>
</tr>
<tr>
<td>3H_2-O_2-Ni-CNC</td>
<td>−0.230</td>
<td>−0.647</td>
<td>−2.694</td>
<td>2.019</td>
<td>1.659</td>
<td>4.177</td>
<td>0.789</td>
<td>4.257</td>
<td>0.738</td>
<td>−0.325</td>
</tr>
<tr>
<td>4H_2-O_2-Ni-CNC</td>
<td>−0.189</td>
<td>−0.482</td>
<td>−2.686</td>
<td>2.020</td>
<td>1.656</td>
<td>4.068</td>
<td>0.745</td>
<td>4.470</td>
<td>0.745</td>
<td>0.739</td>
</tr>
<tr>
<td>5H_2-O_2-Ni-CNC</td>
<td>−0.166</td>
<td>−0.373</td>
<td>−2.633</td>
<td>2.019</td>
<td>1.659</td>
<td>3.461</td>
<td>0.745</td>
<td>3.779</td>
<td>4.490</td>
<td>0.745</td>
</tr>
<tr>
<td>6H_2-O_2-Ni-CNC</td>
<td>−0.146</td>
<td>−0.317</td>
<td>−2.778</td>
<td>2.021</td>
<td>1.657</td>
<td>3.588</td>
<td>0.789</td>
<td>3.828</td>
<td>4.503</td>
<td>0.745</td>
</tr>
</tbody>
</table>

Figure 8. Optimized structure of competition between hydrogen and oxygen adsorption on the nickel doped CNC of one to six \( \text{H}_2 \). Balls in grey, blue, red and white denote carbon, nickel, oxygen and hydrogen atoms respectively. For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.
Consequently, under normal conditions, oxygen interferes strongly with hydrogen adsorption. The calculations show strong qualitative variations in the charge transfer behavior due to the adsorption of O$_2$ molecule at Ni-CNC surface. From Table 1, the interaction of Ni atom on CNC shows a strong net charge transfer from the Ni to the CNC resulting in a Ni charge of $+0.589$ e, where the H$_2$ molecules transfer charge to the decorated Ni atom. In contrast, the interaction of oxygen molecules with Ni-CNC causes the charge at the Ni atom to increase to $+0.971$ e. This is due to the O$_2$ molecules being more electronegative and withdrawing electrons from the metal charge on the oxygen atoms ($-0.655$ e). Therefore, the dipole moment of O$_2$-Ni-CNC and Ni-CNC is calculated to be 10.831 and 19.097, respectively. This is sufficient to reduce the van der Waal’s interaction between hydrogen and O$_2$-Ni-CNC. Figure 9 confirms the results in Table 6 and the adsorption properties that were discussed earlier. Ao et al. [55] [56] showed that the application of a perpendicular electric field may act as a catalyst for the dissociative adsorption of hydrogen on pristine and nitrogen-doped graphene. Therefore, the application of an external field could be an alternative to favor the selective hydrogen adsorption. This subject will be a topic of future research.

4. Conclusions

Using DFT calculations, Ni-decorated CNC has been investigated for hydrogen storage applications. PDOS and NBO analysis have been performed to understand the H$_2$ adsorption mechanism. The adsorption mechanism for H$_2$ on Ni decorated CNC was primarily attributed to the polarization induced by electrostatic field of metal atoms on CNC and the hybridization between the Ni atom and hydrogen molecules. Two types of reactions (reversible and irreversible) were characterized in terms of (PDOS), electrophilicity, and statistical thermodynamic

![Figure 9](image-url). PDOS of (a) oxygen molecule (b) decorated Ni atoms in the (4H$_2$-O$_2$-Ni-CNC) system. The Fermi level is set to zero and indicated by a dotted line.
competitive adsorption between H\textsubscript{2} and O\textsubscript{2} molecules strongly favors oxygen. Therefore, O\textsubscript{2} strongly reduces the bient conditions. However, due to lower migration barriers and strong metal-to-metal attraction, aggregation of metal atoms in the form of a metallic layer or cluster on typical experimental CNC seems inevitable. It was observed that the structure where Ni atoms cluster was ~0.738 eV lower in energy than when they remained isolated. Ni\textsubscript{2}-CNC can bind six H\textsubscript{2} molecules and their corresponding storage capacity is 11.323 wt.%, which is higher than the revised 2015 target of U.S. DOE. Consequently, Ni-CNC could be used as a high capacity hydrogen storage medium in onboard automobile applications. On the other hand, the present results show that the competitive adsorption between H\textsubscript{2} and O\textsubscript{2} molecules strongly favors oxygen. Therefore, O\textsubscript{2} strongly reduces the interaction of hydrogen molecules with the Ni-CNC. Consequently, this interaction will inhibit the practical use for hydrogen storage.

References


