Control of Instable Chaotic Small Power System

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Received 7 February 2015; accepted 25 February 2015; published 28 February 2015

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Abstract

In this paper, we aim to control an instable chaotic oscillation in power system that is considered to be small system by using a linear state feedback controller. First we will analyze the stability of the mentioned power system by means of modern nonlinear theory (Bifurcation and Chaos). Our model is based on a three bus power system that consists of multi generators containing both dynamic and static loads. They are considered to be in the form of an induction motor in parallel with a capacitor, as well as a combination of constant power along with load impedance, PQ. We consider the load reactive power as the control parameter. At this stage, after changing the control parameter, the study showed that the system is experiencing a subcritical Hopf bifurcation point. This leads to a chaos within the system period doubling path. We then discuss the system controllability and present that the all chaotic oscillations fade away through the linear controller that we impose on the system.

Keywords

Bifurcation, Instable Chaotic Oscillation, Linear Controller, Voltage Collapse, Chaotic Oscillation Fade Away, Small Power Systems

1. Introduction

In the past so many researchers have used the voltage collapse case study within a power system. Here, the power system performs as a significant part of the sequential event that is accompanied by an unstable voltage profile [1]. This voltage collapse will lead to load losses that will be yielded into a tripping on the load lines and subsequently, a total shutdown will affect the considered area. The Kingdom of Saudi Arabia, United States of America, United

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Kingdom, Japan, France and many other countries have had several incidents that are associated with the collapse of voltage leading into a total area shutdown. There are so many reasons that contribute to these incidents. Some of which are focused on the loads whether it is high or low on the tap changing transformers and the reactive power injected at the bus. All these will lead to a voltage level breakdown. In order to control the voltage collapse occurrence, several techniques may be applied such as Static Var Compensator (SVC), and Series Capacitor Bank (SCB).

Throughout the past most of the work that was conducted would have linked the voltage collapse to a static bifurcation done by Kwatny et al. [2], Schlutere et al. [3], and Thomas and Tirununchit [4]. While, the dynamic bifurcation was linked by Abed and Varaiya [5], Abed et al. [6], Rajagopalan et al. [7], Dobson et al. [8], and Nayfeh et al. [9].

Combining both control theories along with the applications of bifurcation theory is a challenge and great interest to many researchers in the design of controllers for nonlinear systems that exhibit bifurcations models. Both Abed and Fu [10] [11] have detailed combination of working on feedback stabilization and bifurcation control simultaneously. Abed et al. [6] and Chiang et al. [12] looked at the issue of utilizing the concept of nonlinear control in power system. Subsequently, Baillieu et al. [13] have studied nonlinear feedback system while at a chaotic motion. In addition, Chang & Chen [14] have investigated bifurcation characteristics under PID controller for nonlinear systems.

Recent studies are directed at combining control of bifurcation along with chaos in dynamical system simultaneously. Thus, the emphasis will be weighted on design techniques that will result into a prescribed nonlinear dynamic system for the controlled processes. Moreover, bifurcation control stimulates its usage by a control input modifying its bifurcation characteristics for the parameterized system. The control model will be considered for a static or a dynamic feedback and with an open loop system.

Our objective is to control, stabilize, and delay a given bifurcation. We also aim for reducing the bifurcation amplitude, getting a bifurcation solution, and finally optimizing the performance index located near the bifurcation.

In the end, we reshape the bifurcation diagram of the system [10]. Using the controlled laws derived and used in [10], we transform an unstable subcritical bifurcation point into a point to be considered as supercritical stable bifurcated. These control laws are called “static state feedback” and have the general form of \( u = u(x) \). These results have a wide span of applications. These applications are not limited to subsynchronous resonance in power system [15], as well as the voltage collapse in electrical power system [16].

2. Mathematical Model

The small power system model is known to be highly nonlinear dynamic system. It is represented by an algebraic along with a set of ordinary differential equations. In this paper, we followed the work done by Nayfeh et al. [9] considering a model that represent the load by an induction motor, a capacitor, constant power and constant impedance \( PQ \) load. The three bus power system consists of two generators feeding a load, which is represented by an induction motor in parallel with a capacitor and combined with a \( PQ \) load. One generator is considered as an infinite bus while the other generator has a constant voltage magnitude of \( E_m \). After Nayfeh et al. [9], the following set equations govern the small power system and are written as:

\[
k_{pm} \dot{x}_1 + k_{pm} \dot{x}_2 = -E_0 Y_0 \sin(x_1 + \theta_m) - E_m Y_m x_1 \sin(x_1 - x_3 + \theta_m)
\]

\[
+ \left[ Y_0 \sin(\theta_m) + Y_m \sin(\theta_m) \right] x_2^2 \left( p_1 + p_2 x_2 + p_3 x_2^2 \right) P_1 - P_0 - k_{pm} x_2
\]

\[
k_{qm} \dot{x}_1 = E_0' Y_0' x_2 \cos(x_1 + \theta_m') + E_m' Y_m' x_2 \cos(x_1 - x_3 + \theta_m')
\]

\[- \left[ Y_0' \cos(\theta_m') + Y_m' \cos(\theta_m') \right] x_2^2 \left( q_1 + q_2 x_2 + q_3 x_2^2 \right) Q_1 - Q_0 - k_{qm} x_2 - k_{qm} x_2^2
\]

\[
\dot{x}_3 = x_4
\]

\[
\dot{x}_4 = \left( 1/M \right) \left( -d_m x_4 + P_m + x_3 Y_m x_2 \sin(x_1 - x_3 - \theta_m) + x_2^2 Y_m \sin(\theta_m) \right)
\]

Now, we add the linear control systems, thus the state-space equations are coupled to the previous four equations resulting into:

\[
\dot{x}_2 = \left( 1/T_g \right) \left( x_4 K_g - x_2 \right)
\]
where $x_1$ and $x_3$ are the power angles of the machine and the load, respectively. Furthermore, $x_2$ is the load voltage, and $x_4$ is the radian frequency of the load, while $x_5$, $x_6$, $x_7$, and $x_8$ are the exciter, amplifier, proportional controller, and the sensor, respectively. The above eight equations provide an equilibrium solution along with a dynamic solution to our model. Table 1 shows the load and generator parameters that have been used. All the parameters are given in per unit except for the angles, which are measured in degrees.

3. Numerical Simulation

The equilibrium solutions are found by setting of the system of Equations (1)-(8) to be equal to zeros. The stability of these solutions depends on the eigenvalues of the Jacobian matrix of set of Equations (2)-(8) evaluated each at the equilibrium point.

### Table 1. Parameters for the load and generator.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
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</thead>
<tbody>
<tr>
<td>$k_{pw}$</td>
<td>0.4</td>
</tr>
<tr>
<td>$k_{ps}$</td>
<td>0.3</td>
</tr>
<tr>
<td>$k_{q_1}$</td>
<td>-0.03</td>
</tr>
<tr>
<td>$k_{q_2}$</td>
<td>-2.8</td>
</tr>
<tr>
<td>$k_{q_2}$</td>
<td>2.1</td>
</tr>
<tr>
<td>$T$</td>
<td>8.5</td>
</tr>
<tr>
<td>$P_o$</td>
<td>0.6</td>
</tr>
<tr>
<td>$Q_o$</td>
<td>1.3</td>
</tr>
<tr>
<td>$P_1$</td>
<td>0.0</td>
</tr>
<tr>
<td>$Y_o$</td>
<td>20.0</td>
</tr>
<tr>
<td>$\theta_o$</td>
<td>$-5.0^0$</td>
</tr>
<tr>
<td>$E_o$</td>
<td>1.0</td>
</tr>
<tr>
<td>$C$</td>
<td>12.0</td>
</tr>
<tr>
<td>$Y_1$</td>
<td>8.0</td>
</tr>
<tr>
<td>$\theta_m$</td>
<td>$-12.0^0$</td>
</tr>
<tr>
<td>$E_m$</td>
<td>2.5</td>
</tr>
<tr>
<td>$Y_m$</td>
<td>5.0</td>
</tr>
<tr>
<td>$\theta_n$</td>
<td>$-5.0^0$</td>
</tr>
<tr>
<td>$E_m$</td>
<td>1.0</td>
</tr>
<tr>
<td>$P_m$</td>
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</tr>
<tr>
<td>$d_m$</td>
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</tr>
<tr>
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<tr>
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<tr>
<td>$T_e$</td>
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<tr>
<td>$K_e$</td>
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</tr>
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<td>$K_c$</td>
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</tr>
<tr>
<td>$M$</td>
<td>0.3</td>
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</table>
Nayfeh et al. [9] studied a small power system using theories of bifurcation theory that are shown in Figure 1. They have noticed that the small power system experiences a dynamical bifurcation (Hopf bifurcation). There are two Hopf bifurcation points $H_1$ and $H_2$ at the control parameters $Q_1 = 6.9929$ and $7.2229$, respectively, and a saddle-node bifurcation $SN$ at $Q_1 = 7.2238$. They have also found that the two Hopf bifurcation points $H_1$ and $H_2$ are subcritical and supercritical points respectively, as shown in the bifurcation diagram in Figure 2. They showed that the system experiences the limit cycle and then period-two, period-four, and so on till the behavior of the system became chaotic. Figure 3 shows the chaotic oscillation of the system. Hence, for values of $6.9105 \leq Q_1 \leq 6.9449957$, the system response may be constant or dynamic (limit-cycle or chaos), depending on the initial conditions. Because the chaos is very sensitive to initial condition.

In order to control and eliminate the chaotic oscillations, a linear control via proportional controller must be added to the system. This linear controller will fade away the eighth order system of Equations (1)-(8). The subcritical Hopf bifurcation, $H_1$ and hence control chaos and voltage collapse there, a nonlinear feedback controller is designed by Nayfeh et al. [9]. Their controller transforms the left Hopf bifurcation point, shown in Figure 3, from a subcritical into a supercritical one as indicated in Figure 3. They have also used a nonlinear controller that has the form of $K_\omega^3$ and it is added to Equation (2). They show that by increasing the value of $K$, we will reduce the amplitude of the limit-cycle born at $H_1$. Furthermore, by choosing a gain $K$ larger than a critical value of 58.56, one can suppress the period-doubling bifurcations and hence the chaos and its associated crisis bifurcation and voltage collapse as shown in Figure 3. In this paper the linear added controller, Equations (6)-(8), were able to eliminate all chaotic oscillations and are shown in Figures 4-6.
Figure 3. The chaotic oscillation of the system.

Figure 4. Chaotic oscillations 1.

Figure 5. Chaotic oscillations 2.
4. Conclusion

The modern nonlinear theories of bifurcation and chaos are applied to a small three bus power system. The results showed that the system, without any controller, has a dangerous subcritical Hopf bifurcation point. That means when $6.9105 \leq Q_1 \leq 6.949957$, the system response may be constant or dynamic (limit-cycle or chaos), depending on the initial conditions. A comparison between the uncontrolled and controlled system was discussed and investigated. The study has revealed that the linear controller stabilizes the system by eliminating all chaotic oscillations. Hence, the system became completely stable over the whole range of the control parameter point $Q_1$.

Acknowledgements

We would like to acknowledge the funding of this project (08-ENE416-5) by the Science and Technology Unit at Taibah University through the National Science, Technology, and Innovation Plan for Saudi Arabia.

References


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