Fuzzy Decision Method Applied in Action of Reactive Power Compensation Devices in Wind System

Xueming Li¹, Li Feng², Yi Tang², Yonghua Chen¹

¹NARI Group Corporation, Nanjing, China
²School of Electrical Engineering, Southeast University, Nanjing, China
Email: lixueming@sgepri.sgcc.com.cn, lfseuee@163.com, tangyi@seu.edu.cn, chenyonghua@sgepri.sgcc.com.cn

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Abstract

Frequent occurrence of large-scale cascading trip-off of wind turbine raises the concern about the decision process of ordered control of reactive power compensation devices. The theory of fuzzy multi-attribute decision making is adopted to ascertain the action sequence of reactive power compensation devices. First, a set of evaluation indexes including control sensitivity, regulation margin, response time, response level and cost is set up, and fuzziness of the proposed qualitative indexes is introduced to make them comparable to the proposed quantitative indexes. Then a method to calculate fuzzy weight of each index is put forward for evaluating relative importance of the proposed indexes. Finally, the action sequence of reactive power compensation devices is determined through the theory of fuzzy compromise decision making. The case study shows that the proposed method is effective to obtain the action sequence of reactive power compensation devices which correspond to experience.

Keywords

Wind Power System; Reactive Power Compensation Device; Ordered Control; Fuzzy Multi-Attribute Decision Making; Evaluation Index

1. Introduction

With the development of new energy, the amount of wind power system combined to power grid is increasing. However, the large-scale connection of wind farms with power grid has adverse effect on the safety of power grid [1-3]. In consideration of China’s large-scale centralized development of wind power [4], reactive and voltage problems deserve more attention. According to requests of China’s relevant standards in wind power combined to power grid such as Q/GDW392-2009, GB/T19963-2011, power system should be able to take part in reactive and voltage control and contain reactive power compensation devices [5]. Equipment like variable speed-constant frequency WTGS, Static Var Compensator (SVC), Static Synchronous Compensator (STATCOM), On Load Tap Changing transformer (OLTC), fixed-switchable shunt capacitors can be used in wind power sys-
system to release reactive power and obviously these equipment have different dynamic responsive characteristics.

Reactive power compensation device taking preset actions according to local electric parameters data is a commonly used control strategy in grid. This control strategy is simple enough to put to use and works well in traditional grid. Nevertheless, this strategy doesn’t take action sequence into account which possibly leads to severe security and stability issues in grid combined with wind power system. For example, several large-scale cascading trip-off of wind turbine happening in 2011 are caused by unordered regulation and actions of reactive power compensation device to a large extent [6]. Hence, a control strategy considering action sequence of various reactive power compensation devices is desperately needed.

It is an important step to evaluate reactive power compensation devices reasonably when designing control strategy for reactive power compensation devices due to different reactive power compensation device requirements in different power system state. For example, regulation economy comes first in all considered factors when power system is in a good state and when power system is in fault state, recovering the power system as soon as possible is most important. This paper aims to achieve the latter requirement and mainly talks about the action sequence of various reactive power compensation devices in wind power system when a fault happened in power system.

As the basis of determining various reactive power compensation devices’ action sequence, it is necessary to find out a variety characteristics of reactive power compensation device and relative importance of these characteristics. Besides this, it is rather difficult to transform all kinds of fuzzy concepts reasonably and take each index into account synthetically. In order to solve the difficulty, fuzzy multi-attribute decision making theory which shows great effects in power system research is involved in this paper. Fuzzy multi-attribute decision making theory has been successfully applied to power system research such as making black-start scheme [7], making equipment maintenance strategy [8], evaluating high voltage transmission mode [9] and so on. First of all, this paper proposes influence factors need to be considered when making action sequence of reactive power compensation devices and quantifies qualitative index with fuzzy number. Then action sequence is determined through the theory of fuzzy compromise decision making. Finally this proposed method is applied to a simulation case and works out an action sequence of reactive power compensation devices.

2. Index System for Determining Action Sequence

2.1. Principal Factor of Wind Power System’s Reactive Power Regulation

This paper identifies factors from two aspects. On one hand characteristics of reactive power compensation devices used in wind farm are taken into consideration such as response time, regulation level and cost etc. On the other hand the effect on power grid that reactive power compensation devices have should also be considered such as voltage regulation ability, impact on other nodes when voltage regulation and so on. From above several important factors of wind power system’s reactive power and voltage regulation are listed below:

1) Voltage of nodes in power system can be regulated by controlling reactive power compensation device for example switching control of compensation capacitors and STATCOM. It is obvious that regulation effects are different because nodes in different electric position have different regulation sensitivity. In order to find out most effective control variable, sensitivity of control variable can be calculated by voltage reactive sensitivity method.

2) Regulation margin is an important index because of limiting conditions of device and operation condition such as voltage limit of wind farm’s terminal, capacity limit of shunt capacitor bank, regulating range limit of voltage regulating transformer, regulating variable limit of SVC and STATCOM.

3) Different control variable has different dynamic operating characteristics, so difference in response time is rather big. The requirement of response time is severe when fault happened in power grid because voltage must be regulated back to normal quickly.

4) Response degree of control variables is different from each other after they changed because of effects of power system’s run-state. This index can only be evaluated qualitatively considering that real-time state of grid changes too fast to be measured.

5) Considering cost and self-character, running cost of control variables is different because of different added losses and fault rate. When fault happens, running cost is an unvalued index in most cases.

Index (1), index (2) and index (3) are quantitative indexes according to description of each index above. These three factors usually can be ascertained by off-line calculation or real-time data acquisition and dynamic
updating for example index (1) can be figured out by network topology and operation mode and index (2), (3) can be directly got by surveying operation condition and intrinsic parameter of device. Index (4) and index (5) are connected with operation condition of grid network which means they hardly can be quantified directly. Considering this characteristic of index (4) and (5), fuzzy number concept is involved in this paper and it is used as a tool to transform qualitative data into math expression.

2.2. Expression of Qualitative and Quantitative Index

As previously mentioned, index (4) and index (5) can’t be shown as accurate math expression directly while concept of triangular fuzzy number [10] is helpful to solve this problem. Usually expression of triangular fuzzy number is written as \( \tilde{N} = (m; \alpha, \beta) \) or \( \tilde{N} = (l, m, r) \), \( l = m - \alpha \), \( r = m + \beta \). \( \alpha \) and \( \beta \) are recognized as left and right diffusion of fuzzy number \( \tilde{N} \) and fuzzy number \( \tilde{N} \) is shown as below:

It is easily to transform ordinary number into triangular fuzzy number by set \( \alpha = \beta = 0 \) and the expression is \( m = (m; 0, 0) \). In order to quantify index (4) and (5), Bipolar Scaling proposed by MacCrimmon is used in this paper and its transforming method is shown in Figure 1.

In Figure 2, index is divided as earnings index and cost index and there is a one-to-one correspondence between importance level and quantitative data. By analyzing definitions of index (4) and (5), index (4) is judged as earnings index while index (5) is cost index. Both of index (4) and (5) can be transformed into triangular fuzzy number by determining their importance level.

2.3. Weight Analysis

Determining weight value for each index is an important step before making compound decision while decision maker usually can’t set accurate weight value for each index by his experience. Under this circumstances, this paper assumes that decision maker know the relative importance of indexes which contributes to working out each index’s weight value in triangular fuzzy number form. By referring to document [10], calculation method is concluded and shown in Table 1.

1) Construct fuzzy reciprocal matrix. Element of this matrix is determined by rule of quantization which is shown below.

For example if index I is more important than index j then set \( \tilde{w}_{ij} = \left( \frac{1}{l_{ij}}, 5, \frac{1}{r_{ij}} \right) \) where \( l_{ij} \) and \( r_{ij} \) represents fuzzy level of this judgment. It assumes that \( r_{ij} - m_{ij} = m_{ij} - l_{ij} = 2 \). Then fuzzy reciprocal matrix \( \tilde{W} = \left( \tilde{w}_{ij} \right)_{n \times n} \)

1. Figure 1. Form of triangular fuzzy number.

2. Figure 2. Bipolar scaling.
Table 1. Rule of quantization.

<table>
<thead>
<tr>
<th>Relative important degree $m_i$</th>
<th>1</th>
<th>3</th>
<th>5</th>
<th>7</th>
<th>9</th>
</tr>
</thead>
<tbody>
<tr>
<td>i compared with j equally important</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Little more important</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Important</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Obviously important</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Absolutely important</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

can be constructed with this method.

2) Work out weight value for each index. Weight value for each index can be calculated by following formula.

$$l_j = \left( \prod_{j=1}^{n} l_{ij} \right)^{\frac{1}{n}}$$

$$m_i = \left( \prod_{j=1}^{n} m_{ij} \right)^{\frac{1}{n}}$$

$$r_i = \left( \prod_{j=1}^{n} r_{ij} \right)^{\frac{1}{n}}$$

Then weight value for index I is $\tilde{w}_I = \left( \frac{l_i}{m_i}, \frac{m_i}{r_i}, \frac{r_i}{l_i} \right)$.


It assumes that available reactive power compensation devices set is $A = \{A_1, A_2, \ldots, A_m\}$ and from 1.1, indexes set considered in determining action sequence of reactive power compensation devices can be represented as $C = \{C_1, C_2, \ldots, C_r\}$. According to reactive power compensation devices set and indexes set, a full matrix $X = \left( x_{ij} \right)_{n \times r}$ can be constructed. $x_{ij}$ represents value for index $C_j$ and reactive power compensation device $A_i$. As is mentioned in 1.3 weight value matrix for each index is $\omega_i^* = (\omega_i^*)_r$ and $\omega_i$ represents weight value for index $C_j$.

In this paper, fuzzy ideal solution ($\tilde{M}^+$) and fuzzy negative ideal solution ($\tilde{M}^-$) are used as reference standard. Satisfaction concept is introduced to help measure the difference between action plan and fuzzy ideal solution. After calculating satisfaction value for each device’s index, satisfaction value for each device can be figured out by weighted sum with weight value matrix $\tilde{\omega} = (\tilde{\omega}_j)_r$. Finally, action sequence of reactive power compensation devices can be listed by comparing devices’ satisfaction value each other.

Step 1: Fuzzy ideal solution and fuzzy negative ideal solution

Fuzzy ideal solution is a set made up of optimal index value in all considered devices. Because of the difference between earnings index and cost index, the way to work out fuzzy ideal solution is different. Take fuzzy index for example and its choosing method is shown in Table 2.

Accurate number shares the same method. For fuzzy negative ideal solution, its definition is similar to fuzzy ideal solution which means they have a similar way to worked out.

Step 2: Satisfaction matrix with fuzzy weight

This is defined as the satisfaction of action device $A_i$ to index $j$. For a fuzzy number, its calculating formula is defined as follows:

$$\lambda_{ij} = \frac{d_L(\tilde{x}_{ij}, \tilde{M}_{jr}) + d_R(\tilde{x}_{ij}, \tilde{M}_{jr})}{d_L(\tilde{M}_{jr}, \tilde{M}_{jr}) + d_R(\tilde{M}_{jr}, \tilde{M}_{jr})}$$

$d_L(a,b), d_R(a,b)$ represents hamming distance between $a$ and $b$.

Multiply satisfaction matrix by weight value matrix and get weighted satisfaction matrix $\tilde{\lambda}_{ij}^w$:

$$\tilde{\lambda}_{ij}^w = \tilde{w}_j \lambda_{ij}$$
Table 2. Method of calculating fuzzy ideal solution.

<table>
<thead>
<tr>
<th>categories</th>
<th>Fuzzy ideal solution</th>
<th>Membership function</th>
</tr>
</thead>
<tbody>
<tr>
<td>earnings</td>
<td>$\tilde{M}_i = \max{\tilde{x}_i}$</td>
<td>$\mu_{w_i}(x) = \sup_{x_{j1}, x_{j2}, \ldots, x_{jn}} \min{\mu_{w_1}(x_{j1}), \ldots, \mu_{w_n}(x_{jn})}$</td>
</tr>
<tr>
<td>cost</td>
<td>$\tilde{M}_i = \min{\tilde{x}_i}$</td>
<td>$\mu_{w_i}(x) = \sup_{x_{j1}, x_{j2}, \ldots, x_{jn}} \min{\mu_{w_1}(x_{j1}), \ldots, \mu_{w_n}(x_{jn})}$</td>
</tr>
</tbody>
</table>

So the weighted satisfaction matrix can be written as: $\tilde{A}^w = [\tilde{A}^w_{ij}]$.

Step 3: Determine preferred value $T_i^\lambda$ is defined as weighted sum of satisfaction value of action device $A_i$ and it can be calculated by following formula:

$T_i^\lambda = \tilde{x}_i^w \oplus \tilde{x}_i^w \oplus \ldots \oplus \tilde{x}_i^w, n = 5$

$\oplus$ represents general addition of fuzzy number and its membership function is:

$\mu_{T_i^\lambda}(x) = \sup_{x_{j1}, x_{j2}, \ldots, x_{jn}} \min\{\mu_{\tilde{x}_i^w}(x_{j1}), \ldots, \mu_{\tilde{x}_i^w}(x_{jn})\}$

After getting $\tilde{T}_i^\lambda$, greatest fuzzy set $\max(\tilde{T}_i^\lambda)$ and minimal fuzzy set $\min(\tilde{T}_i^\lambda)$ can be determined and their membership function can be defined as follows:

$\mu_{\max(\tilde{T}_i^\lambda)}(x) = \sup_{x_{j1}, x_{j2}, \ldots, x_{jn}} \min\{\mu_{\tilde{x}_i^w}(x_{j1}), \ldots, \mu_{\tilde{x}_i^w}(x_{jn})\}$

Relative utility function $f(\tilde{T}_i^\lambda)$ can be calculated by membership formula:

$\mu_{f(\tilde{T}_i^\lambda)}(r) = d_1 [\tilde{T}_i^\lambda, \min(\tilde{T}_i^\lambda)] + d_2 [\tilde{T}_i^\lambda, \min(\tilde{T}_i^\lambda)]$

Finally the action sequence of reactive power compensation device is worked out by ranking the value of $f(\tilde{T}_i^\lambda)$ from largest to smallest.

4. Simulation Case

In Figure 3, there are several reactive power compensation devices like MCR-SVC, TCR-SVC, fixed capacitor and STATCOM in this local grid. Besides this, this local grid includes wind power system which adds difficulty in regulating voltage and reactive power. In this simulation case, it assumes that a fault happened in power system and switch off reactive power compensation devices to clear up overvoltage. So in this paper it is aim to determine the action sequence of reactive power compensation devices to regulate voltage back to normal as soon as possible (Table 3).

Decision-making matrix $\tilde{D}$ can be calculated with method in 1.2.

$D = \begin{bmatrix}
0.00283 & (0.4,0.5,0.6) & 44 & 0.1 & (0.4,0.5,0.6) \\
0.000809 & (0.6,0.7,0.8) & 88 & 0.03 & (0.2,0.3,0.4) \\
0.000845 & (0.8,0.9,1.0) & 11 & 0.01 & (0.0,0.1,0.2) \\
0.0000728 & (0.6,0.7,0.8) & 22 & 0.03 & (0.2,0.3,0.4) \\
0.00282 & (0.6,0.7,0.8) & 46 & 0.03 & (0.2,0.3,0.4) \\
0.000806 & (0.2,0.3,0.4) & 100 & 1 & (0.8,0.9,1.0)
\end{bmatrix}$
Figure 3. Structure of simulation case.

Table 3. Attributes of reactive power compensation devices.

<table>
<thead>
<tr>
<th>nodes</th>
<th>Device classification</th>
<th>Sensitivity of regulating voltage p.u./Mvar</th>
<th>response degree</th>
<th>response time</th>
<th>Output reactive power/Mvar</th>
<th>response cost</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>MCR-SVC</td>
<td>0.00283</td>
<td>me</td>
<td>0.1</td>
<td>44</td>
<td>me</td>
</tr>
<tr>
<td>4</td>
<td>TCR-SVC</td>
<td>0.000809</td>
<td>H</td>
<td>0.03</td>
<td>88</td>
<td>VH</td>
</tr>
<tr>
<td>3</td>
<td>STATCOM</td>
<td>0.000845</td>
<td>VH</td>
<td>0.01</td>
<td>11</td>
<td>H</td>
</tr>
<tr>
<td>5</td>
<td>TCR-SVC</td>
<td>0.0000728</td>
<td>H</td>
<td>0.03</td>
<td>22</td>
<td>VH</td>
</tr>
<tr>
<td>2</td>
<td>TCR-SVC</td>
<td>0.00282</td>
<td>H</td>
<td>0.01</td>
<td>46</td>
<td>VH</td>
</tr>
<tr>
<td>9</td>
<td>FC</td>
<td>0.000806</td>
<td>L</td>
<td>1</td>
<td>100</td>
<td>L</td>
</tr>
</tbody>
</table>

According to rule of quantization fuzzy reciprocal matrix $W$ is set up.

$$
W = \begin{bmatrix}
    (1,1) & (1,1) & (1,1) & (1,1) \\
    2 & 3 & 4 & 5 & 6
\end{bmatrix}
$$

Since fuzzy reciprocal matrix $W$ is set up, weight for each index can be calculated.

$$
\hat{w} = \left[ (0.28, 0.41, 0.57), (0.21, 0.27, 0.32), (0.16, 0.21, 0.18), (0.10, 0.01, 0.02), (0.03, 0.04, 0.05) \right]
$$

Fuzzy ideal solution and fuzzy negative ideal solution can be found out by using method mentioned in 2.2.

$$
\hat{M}^+ = \left[ 0.00283, 0.8, 0.9, 1.0, 100, 1, (0.8, 0.9, 1.0) \right]
$$

$$
\hat{M}^- = \left[ 0.0000728, 0.2, 0.3, 0.4, 11, 0.01, (0.0, 0.1, 0.2) \right]
$$

Relative satisfaction matrix is set up and shown as follows.

$$
\lambda = \hat{A}_y \hat{A}_y = \begin{bmatrix}
    1 & 0.3 & 0.371 & 0.091 & 0.5 \\
    0.266 & 0.5 & 0.865 & 0.020 & 0.25 \\
    0.280 & 0.7 & 0 & 0 & 0 \\
    0 & 0.5 & 0.124 & 0.020 & 0.25 \\
    0.996 & 0.5 & 0.393 & 0.020 & 0.25 \\
    0.266 & 0 & 1 & 1 & 1
\end{bmatrix}
$$
Weighted satisfaction matrix is worked out easily.

\[
\tilde{\mathbf{X}} = \left[ \hat{\lambda}^* \right] = \left[ \mathbf{w} \otimes \hat{\lambda} \right] = \begin{bmatrix}
(0.28,0.41,0.57) & (0.105,0.135,0.16) & (0.063,0.081,0.096) & (0.060,0.063,0.067) \\
(0.075,0.109,0.152) & (0.147,0.189,0.224) & (0.138,0.147,0.156) \\
(0.078,0.115,0.160) & (0.063,0.067,0.071) \\
0 & (0.16,0.17,0.18) \\
(0.279,0.408,0.568) & (0.105,0.135,0.16) & (0.063,0.067,0.071) \\
(0.074,0.109,0.152) & (0.020,0.021,0.022) \\
(0.009,0.010,0.011) & (0.0015,0.020,0.025) \\
(0.002,0.0022,0.0024) & (0.008,0.010,0.013) \\
(0.10,0.11,0.12) & (0.03,0.04,0.05) \\
\end{bmatrix}
\]

1) Sum weighted matrix can be worked out.

\[
\tilde{\mathbf{X}}^T = \begin{bmatrix}
(0.508,0.584,0.769) \\
(0.328,0.403,0.483) \\
(0.225,0.304,0.384) \\
(0.135,0.168,0.197) \\
(0.457,0.622,0.814) \\
(0.364,0.429,0.502) \\
\end{bmatrix}
\]

2) Finally relative utility function \(f\left(\tilde{\mathbf{X}}^T\right)\) can be figured out with \(\tilde{\mathbf{X}}^T\).

\[
f\left(\tilde{\mathbf{X}}^T\right) = \begin{bmatrix}
0.911 \\
0.405 \\
0.216 \\
0.106 \\
0.789 \\
0.998 \\
\end{bmatrix}
\]

By ranking \(f\left(\tilde{\mathbf{X}}^T\right)\) from largest to smallest, the action sequence of reactive power compensation devices is determined. The action sequence is: fixed capacitor at pooling station B230, MCR-SVC at wind farm 1, TCR-SVC at wind farm 1, TCR-SVC at wind farm 2, STATCOM at wind farm 3 and TCR-SVC at wind farm 4.

5. Conclusion

This paper proposes a method to determine action sequence of reactive power compensation devices in wind power system at the time of voltage regulating. Characteristics of reactive power compensation devices have impact on grid and these characteristics include qualitative index and quantitative index which can’t be evaluated by a certain judging standard. Fuzzy theory is introduced in this paper to solve this problem. Each index of reactive power compensation device can be expressed perfectly with fuzzy multi-attribute decision making theory and by using this theory result corresponds to real condition more accurately.

References


