Design Analysis of DC-DC Converters Connected to a Photovoltaic Generator and Controlled by MPPT for Optimal Energy Transfer throughout a Clear Day

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ABSTRACT

The DC-DC converters are widely used in photovoltaic generating systems as an interface between PV module and the load. These converters must be chosen to be able to match the maximum power point (MPP) of PV module when climatic conditions change with different resistive load values. So DC-DC converters must be used with MPPT controller in order to reduce losses in the global PV system. This article focuses on the effect of climatic conditions on design of two components (inductance, capacitance) for three topologies of DC-DC converters commonly used in PV systems. When climatic conditions change, the boundary of inductance and capacitance parameters of DC-DC converter will change. These two parameters must be properly sized to achieve optimal efficiency for each converter. The design optimization is based on two principles: 1) for a steady-state operation in a continuous conduction mode, the inductance value for all choppers must be greater than the maximum value of boundary inductance, and 2) in order to limit the output voltage ripple of DC-DC converter below a desired value, the filter capacitance must be larger than the maximum value of boundary capacitance.

KEYWORDS

DC-DC Converter; Energy Efficiency; Design; Load Matching; MPPT

1. Introduction

When a PV module is directly coupled to a given load resistance $R_{LA}$ (Figure 1), the operating point is located at A. For another value of resistive load $R_{LB}$, the operating point will move to B. During this range of load variation, there is only one point at which the PV module provides its maximum power point (MPP). This occurs when load resistance is equal to the optimal value (load resistance at MPP: $R_L = R_{opt}$). But it’s very difficult to select a fixed load which matches this value, and even if it is done, this point itself changes under changed climatic conditions.

To overcome this problem, a maximum power point tracker system (MPPT) must be used to force the PV module’s operating point at the MPP. MPPT can extract more than 97% of the PV power when properly optimized. The goal of the MPPT is to match the impedance of load to the optimal impedance of PV module [1]. MPPT uses the DC-DC converter for a different purpose: regulating the input voltage at the PV module’s MPP and providing load matching for the maximum power transfer [2].

On the other hand, when a DC-DC converter is interposed between the PV module and the load, the operating point depends on the impedance seen by the module ($R_{in}$), which shows dependence on two parameters: $R_L$ and duty cycle ($\alpha$). Thus, under different loads, the duty cycle can be adjusted to change $R_{in}$ to match $R_{opt}$ at any cli-
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2. Theory Development

2.1. PV Module Modelling

A single exponential model [20-22] (one diode model) considered as the most popular model for solar cells describes the relationship between voltage and current. This relationship given by a PV module is written as:

$$I_{pv} = I_{ph} - I_s \left[ \exp \left( \frac{V_{pv} + R_{sh} I_{pv}}{n N_s V_T} \right) - 1 \right]$$

where $N_s$ is the number of cells connected in series. This model contains five parameters, photogenerated current ($I_{ph}$), reverse saturation current ($I_s$), series resistance ($R_{pv}$), shunt resistance ($R_{sh}$) and diode ideality factor ($n$). The one diode model circuit is shown in Figure 2.

To make a better model, the computation of $I_{ph}$, $I_s$ and $R_{pv}$ parameters includes temperature effects. The $R_{sh}$ and $n$ parameters are considered constant and equal respectively to 1000 $\Omega$ and 1.21. These two values are estimated to attain the best match with the I-V curves on the datasheet of the given PV module.

2.2. MPPT Method Analysis

The location of the MPP in the I-V curve of PV module is not known beforehand and always changes dynamically depending on irradiance and temperature. Therefore, the MPP needs to be located by tracking algorithm, which is the heart of MPPT controller. The goal of the MPPT is to match the load resistance $R_L$ to the optimal output resistance of PV module $R_{opt}$ defined as:

$$R_{opt} = \frac{V_{mpv}}{I_{mpv}}$$

When $R_L$ matches with that of $R_{opt}$ ($R_L = R_{opt}$), the maximum power transfer from PV to the load will occur.

The MPPT method used in this work is called: “output sensing method”, it measures the power change of PV at the output side of converter and uses the duty cycle as a control variable [2]. This control method employs the Perturbation and Observation (P&O) algorithm to locate the MPP. The flowchart of algorithm is shown in Figure 3.

In order to accommodate duty cycle as a control variable, the P&O algorithm [23] used here is a slightly modified version of the classic one, but the idea how it works is the same. The algorithm perturbs the duty cycle and measure the output power of converter. If the power is increased, the duty cycle is further perturbed in the same direction; otherwise the direction will be reversed. When the output power of the converter is reached at the

![Figure 1: Operating point of a PV module with different resistive load.](image1)

![Figure 2: A one diode equivalent circuit for PV module used in the MATLAB simulation.](image2)
peak, the PV module is supposed to be operating at MPP.

2.3. Operation of DC-DC Converters

The three basic DC-DC converters commonly used in PV systems are: buck, boost and buck-boost converters [24], are shown in Figure 4. The characteristic parameters of each topology can be described by the following parameters listed in Table 1 [25].

The converter can operate in two distinct modes of operation, the continuous conduction operation (CCO) or the discontinuous conduction operation (DCO). The CCO occurs when inductance current is always greater than zero and is preferred for high efficiency and good utilization of semiconductors switches and passive components [26]. The DCO is not preferred since the dynamic order of the converter is reduced [26].

The inductance L is used to filter the input and output current of the converter. L_{bo} is the boundary value of L for a given duty cycle α to ensure that the chopper is operated in CCO mode [25]. The capacitance C allows minimizing the output voltage ripple of the converter, so C_{bo} is the boundary capacitance value required for a given duty cycle α to reduce the output ripple voltage of the converter to specified desired value [25]. The above parameters can be computed using the relationships given in Table 1.

We note that these relations were deduced under the assumption that the converter is lossless and always operates in CCO mode.

3. Results and Discussions

The following simulation work is carried out under the climatic conditions in Tunisia. The SIEMENS SM-50H [27] was selected as photovoltaic generator for the simulation. The module consists of 33 single-crystalline silicon solar cells connected in series and provides 50 W as nominal maximum power in STC. The characteristic parameters of this module are shown in appendix.

Figure 5 shows the climatic data used for this study. The set of these data is the measurements of a sunny day of March in Tunisia. The figure shows that the lowest irradiance is 191 W/m² at 26.7°C while the highest irradiance was 1064 W/m² at 40°C. From these data, we calculate values of optimum resistance R_{opt} at highest

Figure 3. Flowchart of P&O algorithm with the output sensing method.
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Figure 4. DC-DC converters diagram commonly used. (a) Boost; (b) Buck; (c) Buck-boost.

Table 1. Characteristic parameters for each DC-DC converter [25].

<table>
<thead>
<tr>
<th>Parameter</th>
<th>boost</th>
<th>buck</th>
<th>buck-boost</th>
</tr>
</thead>
<tbody>
<tr>
<td>$A_v = \frac{V_0}{V_{pv}}$</td>
<td>$\frac{1}{1-\alpha}$</td>
<td>$\alpha$</td>
<td>$\frac{\alpha}{1-\alpha}$</td>
</tr>
<tr>
<td>$A_i = \frac{I_i}{I_{pv}}$</td>
<td>$1-\alpha$</td>
<td>$\frac{1}{\alpha}$</td>
<td>$\frac{1-\alpha}{\alpha}$</td>
</tr>
<tr>
<td>$R_{sw}$</td>
<td>$\left(1-\alpha\right)^2 R_i$</td>
<td>$\frac{R_i}{\alpha^2}$</td>
<td>$\frac{(1-\alpha)^2}{\alpha^2} R_i$</td>
</tr>
<tr>
<td>$L_{sw}$</td>
<td>$\frac{(1-\alpha)^2 \alpha R_i}{2f}$</td>
<td>$\frac{(1-\alpha)R_i}{2f}$</td>
<td>$\frac{(1-\alpha)^2 R_i}{2f}$</td>
</tr>
<tr>
<td>$C_{sw}$</td>
<td>$\frac{\alpha V_i}{\Delta V_{f}R_i f}$</td>
<td>$\frac{(1-\alpha)V_i}{8\Delta V_{f}L f}$</td>
<td>$\frac{\alpha V_i}{\Delta V_{f}R_i f}$</td>
</tr>
</tbody>
</table>

Figure 5. Irradiance and cell temperature data for a sunny day of March in Tunisia.

Table 2 summarizes these data.

The irradiance and temperature parameters change systemically during the day, consequently the MPP will change; thus, the duty cycle must be adjusted in order to track the new MPP. Hence, boundary values of capacitance and inductance ($C_{bo}, L_{bo}$) will also change (Table 1). The values of these components sized for a certain duty cycle may be less than the chosen converter design parameters. Therefore, the converter may work in DCO mode with large output voltage ripple which reduces the converter efficiency.

In order to reach the ideal choice of these parameters, we will study the behaviour of $C_{bo}$ and $L_{bo}$ later along the day according to changing in climatic conditions using the following criteria:
- a typical switching frequency for all DC-DC converters of 50 KHz.
- suitable load resistor associated to each converter.
- a maximum percentage ripple of output voltage $\Delta V_o/V_o$ equal to 2%.

climatic conditions ($R_{opt,(min)}$) shown in the middle of the day (12 h) and $R_{opt}$ at lowest climatic conditions ($R_{opt,(max)}$) shown at the end of the day. Thus, Figure 6 demonstrates the variation of $R_{opt}$ throughout the day.
Figure 6. Optimum resistance trajectory for a sunny day of March in Tunisia.

Table 2. Module characteristic in low and high climatic conditions.

<table>
<thead>
<tr>
<th>Climatic conditions</th>
<th>P_{m,pv} (W)</th>
<th>I_{m,pv} (A)</th>
<th>V_{m,pv} (V)</th>
<th>R_{opt} (Ω)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hightest</td>
<td>49.82</td>
<td>3.31</td>
<td>15.05</td>
<td>4.54</td>
</tr>
<tr>
<td>Lowest</td>
<td>8.75</td>
<td>0.585</td>
<td>14.95</td>
<td>25.54</td>
</tr>
</tbody>
</table>

3.1. Design for Buck Converter

For buck converter, the resistor load is chosen to be $R_L = 3 \, Ω < R_{opt,(min)}$ as presented in Figure 7(a). The effect of duty cycle $\alpha$ on $L_{bo}$ and $C_{bo}$ is demonstrated in Figure 7(b), where $C_{bo}$ is drawn with different values of filter inductance $L$. We note that curve 1 corresponds to $L = L_{bo,(max)}$, and then other curves are obtained by increasing $L$ in steps of $2 \, µH$. In curve 2, when $L = L_{bo}$ it’s apparent that $C_{bo}$ is constant and independent of $\alpha$, but increasing $L$ over $L_{bo,(max)}$ gives a significant decreasing in $C_{bo}$. The impedance matching is available at A to B which corresponds to a variation of duty cycle between 0.347 and 0.825 (Figure 7(a)) and this leads to a decreasing of $L_{bo}$ from 19.58 $µH$ ($L_{bo,(max)}$) to 5.25 $µH$ ($L_{bo,(min)}$). At point C, the duty cycle is $\alpha = 0.6$, and $L_{bo} = L_{1,bo} = 12 \, µH$. If climatic conditions changes, this point moves to D corresponding to $\alpha = 0.6$ and $L_{bo} = L_{2,bo} = 15 \, µH > L_{1,bo}$. It turns out that the choice of $C_{bo}$ is constant and independent of $\alpha$, but increasing $L$ over $L_{bo,(max)}$ gives a significant decreasing in $C_{bo}$. The impedance matching is available at A to B by varying duty cycle between 0.14 and 0.617 (Figure 7(a)) which leads to an increase of $C_{bo}$ from $4.66 \, µF$ ($C_{bo,(min)}$) to $20.58 \, µF$ ($C_{bo,(max)}$). Therefore, the filter capacitance $C$ must be greater than $C_{bo,(min)}$ which occurs at the lowest climatic conditions for loads lower than $R_{opt,(max)}$.

In curve 1, it can be seen that $C_{bo}$ decrease from 83.3 $µF$ ($C_{bo,(max)}$) to 22.3 $µF$ ($C_{bo,(min)}$) when the operating point varies from A to B. For a given climatic condition, if the duty cycle is $\alpha = 0.6$ corresponding to point C, $C_{bo} = C_{1,bo} = 51 \, µF$. If this point moves to D corresponding to $\alpha = 0.5$, $C_{bo}$ will increase to $C_{2,bo} = 63.8 \, µF > C_{1,bo}$. Consequently, the choice of $C_{1,bo}$ will make the output voltage ripple of the buck converter larger than the desired limit value. In order to avoid this problem, the filter capacitance $C$ must be designed for a value larger than $C_{bo,(max)}$, which is obtained at the lowest climatic conditions for loads lower than $R_{opt,(max)}$.

3.2. Design for Boost Converter

In this study, the resistor load is chosen to be $R_L = 30 \, Ω > R_{opt,(max)}$ as shown in Figure 8(a). Figure 8(b) shows the variation of $L_{bo}$ and $C_{bo}$ according to $\alpha$. It can be seen that when $\alpha$ is increased, $C_{bo}$ will increase linearly. When the climatic conditions changes from the lowest to the highest value, the operating point moves from A to B respectively. Thereafter, the impedance matching is available at A to B by varying duty cycle between 0.14 and 0.617 (Figure 8(a)) which leads to an increase of $C_{bo}$ from $4.66 \, µF$ ($C_{bo,(min)}$) to $20.58 \, µF$ ($C_{bo,(max)}$). Therefore, the filter capacitance $C$ must be greater than $C_{bo,(max)}$ which occurs at the highest climatic conditions for loads lower than $R_{opt,(max)}$. $L_{bo}$ takes a hill curve form, the peak of the hill is noted $L_{bo,(peak)} = 44.77 \, µH$ obtained for a duty cycle $\alpha_{m} = 1/3$. This particular value of duty cycle is obtained while solving the following equation.
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for the chosen load value and the switching frequency given by:

$$\frac{dL_{bo}}{d\alpha} = 0, \text{ where } L_{bo} = 3 \times 10^{-3} \left(1 - \alpha \right)^2 \alpha$$  \hspace{1cm} (3)

We note that $L_{bo,\text{peak}}$ always occurs at $\alpha_m = 1/3$ only if it is included in the operating range of duty cycle variation and this value is constant and independent of any other parameters. Finally, $L_{bo,\text{peak}} = L_{bo,\text{max}}$ in this study.

3.3. Design for Buck-Boost Converter

Several previous studies investigated that the buck-boost converter has not any constraint for the choice of load. In our study, $R_{\text{opt,\text{min}}} < R_L = 8 \ \Omega < R_{\text{opt,\text{max}}}$, is chosen as shown in Figure 9(a). When the operating point moves from A to B by changing in climatic conditions from the lowest to the highest, the impedance matching is available at A to B by varying duty cycle between 0.36 to 0.575. And subsequently, a linear increase of $C_{bo}$ from 45 $\mu$F ($C_{bo,\text{min}}$) to 71.8 $\mu$F ($C_{bo,\text{max}}$) is shown in Figure 9(b). Whereas, $L_{bo}$ is decreased linearly from 32.77 $\mu$H ($L_{bo,\text{max}}$) to 14.45 $\mu$H ($L_{bo,\text{min}}$). To ensure that the buck-boost converter operates in CCO mode, the inductance $L$ must be chosen larger than $L_{bo,\text{max}}$, which is always at the lowest climatic conditions for any loads values. And, to ensure a limit value of the ripple in output voltage at a desired value, $C$ must be designed for a value larger than $C_{bo,\text{max}}$, which is always at the highest climatic conditions for any loads values.

4. Conclusions

The goal of this study is to achieve the highest performance of three topologies of DC-DC converters connected to a single PV module and controlled by MPPT throughout a clear day in Tunisia. These topologies of converters are commonly used in PV systems.

This goal can be achieved only if each converter is properly sized. Thereafter, the effect of changing climatic conditions on the choice of filter inductance and capacitance of each type of converter is investigated. We stated that the inductance for these converters must be greater than $L_{bo,\text{max}}$ to guarantee a CCO mode. We have investigated that this value occurs at the lowest climatic conditions for all DC-DC converters except the boost converter which may occur at any location during the period of system operating. Also in order to limit the output voltage ripple of DC-DC converters below a required value, we stated that the capacitance must be larger than $C_{bo,\text{max}}$. We have investigated that this value occurs at the lowest conditions for buck converter and at the highest conditions for boost and buck-boost converters.

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http://www.a1solar.co.uk/sm50-h.pdf

**Nomenclature**

\( V_{pv} \): output voltage from PV module (V).
\( I_{pv} \): output current from PV module (A).
\( A_v \): converter voltage gain.
\( A_i \): converter current gain.
\( R_{in} \): input resistance to converter (Ω).
\( \Delta V_o \): output ripple voltage of converter (V).
\( L_{bo} \): boundary value of inductance (µH).
\( C_{bo} \): boundary value of capacitance (µF).
\( R_L \): load resistance (Ω).
\( R_{opt} \): PV output resistance at MPP (Ω).
\( I_s \): reverse saturation current.
\( P_{mp} \): PV module maximum power (W).
\( V_{mp} \): PV voltage at MPP (V).
\( I_{mp} \): PV current at MPP (A).
\( G_{in} \): incident irradiance intensity (W/m²).
\( V_T \): thermal voltage \((V_T = (K \cdot T)/q)\)
\( K \): Boltzmann’s constant (J/K).
\( T \): cell temperature (°C).
\( q \): electron charge \((1.602 \times 10^{-19} \, \text{C})\).

**Abbreviations**

STC: Standard Test Condition.
MPP: Maximum Power Point.
MPPT: Maximum Power Point Tracker.
CCO: Continuous Condition Operation.
DCO: Discontinuous Condition Operation.