Calculation of Thermal Pressure Coefficient of Dense 
C_{15}H_{32}, C_{17}H_{36}, C_{18}H_{38} and C_{19}H_{40} Using pVT Data

Vahid Moeini*, Abol Ghasem Mahdianfar
Department of Chemistry, Payame Noor University, Tehran, Iran
Email: *v_moeini@yahoo.com

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ABSTRACT
The thermal pressure coefficients in liquid n-Pentadecane (C15), n-Heptadecane (C17), n-octadecane (C18) and n-nonadecane (C19) was measured using pVT data. The measurements were carried out at pressures up to 150 MPa in the temperature range from 293 to 383 K. The experimental results have been used to evaluate various thermophysical properties such as thermal pressure coefficients up to 150 MPa with the use of density and temperature data at various pressures. New parameters of the linear isotherm regularity, the so-called LIR equation of state, are used to calculate of thermal pressure coefficients of n-Pentadecane (C15), n-Heptadecane (C17), n-octadecane (C18) and n-nonadecane (C19) dense fluids. In this paper, temperature dependency of linear isotherm regularity parameters in the form of a first order has been developed to second and third order and their temperature derivatives of new parameters are used to calculate thermal pressure coefficients. The resulting model predicts accurately thermal pressure coefficients from the lower density limit at the Boyle density at the from triple temperature up to about double the Boyle temperature. The upper density limit appears to be reached at 1.4 times the Boyle density. These problems have led us to try to establish a function for the accurate calculation of the thermal pressure coefficients based on the linear isotherm regularity theory for different fluids.

Keywords: Thermal Pressure Coefficient; Petroleum Industry; Molecular System; The Helmholtz Energy; Lennard-Jones (12,6)

1. Introduction
A study of the thermophysical properties as a function of pressure and temperature in a homologous series of chemical compounds is of great interest not only for industrial applications for example, in the petroleum industry, but also for fundamental aspects for understanding the influence of the chain length of the components on the liquid structure and then developing models for an accurate representation of the liquid state. With this aim in mind, a research program of thermal pressure coefficients (TPC) measurements under pressure on most paraffins between decane and triacontane was initiated as a part of a project on crude oil characterization [1-3].

One of the most difficult problems within the context of the thermodynamics lies in the shortage for experimental data for some basic quantities such as thermal pressure coefficients (TPC) which are tabulated for extremely narrow temperature ranges, normally around the ambient temperature for several types of liquids. Furthermore, the measurements of the thermal pressure coefficients made by different researchers often reveal systematic differences between their estimates [4,5].

The idea has been presented a simple method that use to calculate thermal pressure coefficient directly in place of using equations of state to analysis experimental pVT data [6-8]. The equation of state described in papers is explicit in Helmholtz energy \( A \) with the two independent variables density \( \rho \) and \( T \). At a given temperature, the thermal pressure coefficient can be determined by Helmholtz energy [9-15].

Another work has led to try to establish a correlation function for the accurate calculation of the thermal pressure coefficients for different fluids over a wide temperature and pressure ranges. The most straightforward way to derive the thermal pressure coefficient is the calculation of thermal pressure coefficient with the use of the principle of corresponding states which covers wide temperature and pressure ranges. The principle of corresponding states calls for the reduced thermal pressure at a given reduced temperature and density to be the same for all fluids. This is true, since the corresponding-states approach is appropriate for conditions of low density in which the fluid molecules are far apart and thus have little interaction. Moreover, at low density, the gas behaves
ideally and its thermal pressure coefficient is temperature independent and approaches $\rho R$ in the zero-density limit. However, as density increases, molecular interactions become increasingly important and the principle of corresponding states fails. The leading term of this correlation function is the thermal pressure coefficient of a perfect gas, which each gas obeys in the low density range. Using this condition it can predict the thermal pressure coefficient of different supercritical fluids and refrigerants up to densities $\rho \approx \rho_c$. As mentioned before, as density increases, molecular interactions become increasingly important and the principle of corresponding states fails. It found out “empirically” that at high densities it is possible to apply the principle of corresponding states to different fluids according to the magnitude of their critical densities versus $10^{21}$.

A general regularity was reported for pure dense fluids, namely testing literature results for $pVT$ for pure dense fluids, according to which $(Z-1)V^2$ is linear with respect to $\rho^2$ for each isotherm, where $Z = pV/RT$ is the compression factor. This equation of state works very well for all types of dense fluids, for densities greater than the Boyle density but for temperatures below twice the Boyle temperature. The regularity was originally suggested on the basis of a simple lattice-type model applied to a Lennard-Jones (12,6) fluid. The purpose of this paper is to examine whether the regularity extends to calculation of the thermal pressure coefficients in liquid n-Pentadecane (C15), n-Heptadecane (C17), n-octadecane (C18) and n-nonadecane (C19) [16-19].

At present work, linear isotherm regularity has been used to calculate the thermal pressure coefficient. The purpose of this paper is to point out an expression for the thermal pressure coefficient of dense fluids using the linear isotherm regularity. In this article, in Section 1, we present a simple method that keeps first order temperature dependency of parameters in linear isotherm regularity versus inverse temperature. Then, the thermal pressure coefficient is calculated by linear isotherm regularity. In Section 2, temperature dependency of parameters in linear isotherm regularity has been developed to second order. In Section 3, temperature dependency of parameters in linear isotherm regularity has been developed to third order and then thermal pressure coefficient is calculated by linear isotherm regularity in each state.

2. Theory

A general regularity which was reported for pure dense fluids, according to which $(Z-1)V^2$ is linear with respect to $\rho^2$, each isotherm as,

$$ (Z-1)V^2 = A + B\rho^2 $$

where $Z = pV/RT$ is the compression factor, $\rho = 1/V$ is the molar density, and $A$ and $B$ are the temperature-dependent parameters.

$$ \frac{\rho}{p/RT} = 1 + A\rho^2 + B\rho^3 $$

2.1. First Order Temperature Dependency of Parameters

We first calculate pressure by linear isotherm regularity, and then use first order temperature dependency of parameters to get the final the thermal pressure coefficient for the dense fluid. Where

$$ A = A_2 - \frac{A_i}{RT} $$

$$ B = \frac{B_i}{RT} $$

Here $A_i$ and $B_i$ are related to the intermolecular attractive and repulsive forces, respectively, while $A_2$ is related to the non-ideal thermal pressure and $RT$ has its usual meaning.

In the present work, the starting point in the derivation is Equation (2). By substitution of Equation (3) and Equation (4) in Equation (2) we obtain the pressure for dense fluid.

$$ p = \rho RT + A_2\rho^3RT - A_2\rho^3 + B_2\rho^3 $$

We first drive an expression for the thermal pressure coefficient using first order temperature dependency of parameters. The final result is $\text{TPC}^{(0)}_{LIR}$

$$ \left( \frac{\partial p}{\partial T} \right)_\rho = R\rho + A_2R\rho^3 $$

According to Equation (6), the experimental value of density and value of $A_2$ from the Table 1 can be used to calculate the value of the thermal pressure coefficient.

For this purpose we have plotted $A$ versus $1/T$ that intercept shows value of $A_2$. Table 1 shows the $A_2$ values for four fluids of $C_{12}H_{22}, C_{13}H_{26}, C_{18}H_{38}$ and $C_{19}H_{40}$. Then we obtain the thermal pressure coefficient of $C_{12}H_{22}, C_{13}H_{26}, C_{18}H_{38}$ and $C_{19}H_{40}$ dense fluids. $C_{17}H_{36}$ serve as our primary test fluids because of the abundance of available $pVT$ data. Such calculations are similar to the other fluids examined. Because plots are subject to experimental error, we also show the coefficient of determination $R^2$, which is simply the square of the correlation coefficient. Here $R^2$ should be within 0.005 of unity for a straight line to be considered a good fit [4,18]. In result, the linear limit is estimated by a limit of $R^2 \geq 0.995$. Thus, in accordance with the square of the correlation coefficient in Table 1, the thermal pressure coefficient using the LIR$^{(0)}$ model yields inaccurate results for the liquid phase. Also, this deviation exists significantly for the
Table 1. The calculated values of $A_2$ for different fluids using Equation (3) and the coefficient of determination ($R^2$).

<table>
<thead>
<tr>
<th>Fluid</th>
<th>$A_2$</th>
<th>$(T_{\text{min}} - T_{\text{max}}) / K$</th>
<th>$R^2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>C15H32</td>
<td>3.8465</td>
<td>303.15 - 383.15</td>
<td>0.9931</td>
</tr>
<tr>
<td>C17H36</td>
<td>3.8855</td>
<td>313.15 - 383.15</td>
<td>0.9874</td>
</tr>
<tr>
<td>C18H38</td>
<td>2.9676</td>
<td>313.15 - 383.15</td>
<td>0.9737</td>
</tr>
<tr>
<td>C19H40</td>
<td>7.4784</td>
<td>323.15 - 383.15</td>
<td>0.9983</td>
</tr>
</tbody>
</table>

supercritical phase. Whereas, we predict that deviation concern to be inaccurate values of $A_2$. For this purpose we have plotted $A$ versus $1/T$ that intercept shows value of $A_2$. **Figures 1(a) and (b)** show plots of $A$ and $B$ versus inverse temperature for C17H36. It is clear that $A$ and $B$ versus inverse temperature are not first order.

### 2.2. Second Order Temperature Dependency of Parameters

In order to solve this problem, the linear isotherm regularity equation of state in the form of truncated temperature series of $A$ and $B$ parameters have been developed to second order for dense fluids. **Figures 2(a) and (b)** show plots of $A$ and $B$ parameters versus inverse temperature for C17H36 fluid. It is clear that $A$ and $B$ versus inverse temperature are second order. Thus, we obtain extended parameters $A$ and $B$ resulted in the second order equation, as

$$A = A_1 + \frac{A_2}{T} + \frac{A_3}{T^2} \tag{7}$$

$$B = B_1 + \frac{B_2}{T} + \frac{B_3}{T^2} \tag{8}$$

The starting point in the derivation is Equation (2) again. By substitution of Equations (7) and (8) in Equation (2) we obtain the pressure for dense fluid.

$$p = \rho RT + A_1 \rho^3 RT + A_2 \rho^3 R + \frac{A_3 \rho^3 R}{T}$$

$$+ B_1 \rho^5 RT + B_2 \rho^5 R + \frac{B_3 \rho^5 R}{T} \tag{9}$$

First, second and third temperature coefficients and their temperature derivatives were calculated from this model and the final result is for the thermal pressure coefficient to form $\text{TPC}^{(i)}_{\text{Lin}}$.

$$\left( \frac{\partial p}{\partial T} \right)_\rho = \rho R + A_1 \rho^3 R - \frac{A_2 \rho^3 R}{T^2}$$

$$+ B_1 \rho^5 R - \frac{B_2 \rho^5 R}{T^2} \tag{10}$$

As Equation (10) shows, that it is possible to calculate the thermal pressure coefficient at each density and temperature by knowing $A_1, A_2, B_1, B_2$. For this purpose we have plotted extending parameters of $A$ and $B$ versus $1/T$ that intercept and coefficients show the values of $A_2, A_3, B_1, B_2$ that are given in Table 2.

### 2.3. Third Order Temperature Dependency of Parameters

In another step, we test to form of truncated temperature series of $A$ and $B$ parameters to third order (**Figures 3(a)** and (b)).
Figure 2. (a) Plot of $A$ versus inverse temperature. The solid line is the linear fit to the $A$ data points, for C$_{17}$H$_{36}$; (b) Plot of $B$ versus inverse temperature. The solid line is the linear fit for C$_{17}$H$_{36}$.

Figure 3. (a) Plot of $A$ versus inverse temperature. The solid line is the linear fit to the $A$ data points, for C$_{17}$H$_{36}$; (b) Plot of $B$ versus inverse temperature. The solid line is the linear fit for C$_{17}$H$_{36}$.

Table 2. The calculated values of $A_1$, $A_3$, using Equation (7) and $B_1$, $B_3$, using Equation (8) for different fluids and the coefficient of determination ($R^2$).

<table>
<thead>
<tr>
<th>Fluid</th>
<th>$A_1$</th>
<th>$A_3$</th>
<th>$R^2$</th>
<th>$B_1$</th>
<th>$B_3$</th>
<th>$R^2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>C$<em>{15}$H$</em>{32}$</td>
<td>10.9156</td>
<td>816865.8686</td>
<td>0.9961</td>
<td>-0.7634</td>
<td>-76880.7076</td>
<td>0.9933</td>
</tr>
<tr>
<td>C$<em>{17}$H$</em>{36}$</td>
<td>17.7236</td>
<td>1653515.0792</td>
<td>0.9950</td>
<td>-1.2741</td>
<td>-142952.2089</td>
<td>0.9909</td>
</tr>
<tr>
<td>C$<em>{18}$H$</em>{38}$</td>
<td>24.7654</td>
<td>2604637.9359</td>
<td>0.9965</td>
<td>-1.7380</td>
<td>-207122.0903</td>
<td>0.9933</td>
</tr>
<tr>
<td>C$<em>{19}$H$</em>{40}$</td>
<td>19.3144</td>
<td>1507260.4826</td>
<td>0.9993</td>
<td>-1.9978</td>
<td>-212489.3619</td>
<td>0.9987</td>
</tr>
</tbody>
</table>
\[ A = A_1 + \frac{A_2}{T} + \frac{A_3}{T^2} + \frac{A_4}{T^3} \]  \hspace{1cm} (11)

\[ B = B_1 + \frac{B_2}{T} + \frac{B_3}{T^2} + \frac{B_4}{T^3} \]  \hspace{1cm} (12)

The starting point in the derivation is Equation (2) again. By substitution of Equations (11) and (12) in Equation (2) we obtain the pressure for dense fluid.

\[ p = \rho RT + A_1 \rho^3 RT + A_2 \rho^3 R + \frac{A_3 \rho^3 R}{T} + \frac{A_4 \rho^3 R}{T^2} + B_1 \rho^3 RT + B_2 \rho^3 R + \frac{B_3 \rho^3 R}{T} + \frac{B_4 \rho^3 R}{T^2} \]  \hspace{1cm} (13)

The final result is for the thermal pressure coefficient to form $TPC_{LIR}^{(1)}$.

\[ \left( \frac{\partial p}{\partial T} \right)_\rho = \rho R + A_1 \rho^3 R - \frac{A_2 \rho^3 R}{T} - \frac{2A_3 \rho^3 R}{T^2} + B_1 \rho^3 R - \frac{B_2 \rho^3 R}{T} - \frac{2B_3 \rho^3 R}{T^2} \]  \hspace{1cm} (14)

That based on Equation (14) to obtain the thermal pressure coefficient, it is necessary to determine values $A_1, A_2, A_3, B_1, B_2, B_3$ that these values are given in Table 3.

### 3. Experimental Tests and Discussion

Specific experiments on heavy hydrocarbons to set up a base which can then be used to define new models especially adapted to these complex mixtures. With this aim in mind, an investigation was carried out on pure hydrocarbons with more than 16 carbon atoms, as hexadecane in mind, an investigation was carried out on pure hydrocarbons especially adapted to these complex mixtures. With this aim in mind, an investigation was carried out on pure hydrocarbons with more than 16 carbon atoms, as hexadecane in mind, an investigation was carried out on pure hydrocarbons especially adapted to these complex mixtures. With this aim in mind, an investigation was carried out on pure hydrocarbons with more than 16 carbon atoms, as hexadecane in mind, an investigation was carried out on pure hydrocarbons especially adapted to these complex mixtures. 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With this aim in mind, an investigation was carried out on pure hydrocarbons with more than 16 carbon atoms, as hexadecane in mind, an investigation was carried out on pure hydrocarbons especially adapted to these complex mixtures.

### Table 3. The calculated values of $A_1, A_2, A_4$, using Equation (11) and $B_1, B_3, B_4$ using Equation (12) for different fluids and the coefficient of determination ($R^2$).

<table>
<thead>
<tr>
<th>Fluid</th>
<th>$A_1$</th>
<th>$A_2$</th>
<th>$A_3$</th>
<th>$A_4$</th>
<th>$R^2$</th>
<th>$B_1$</th>
<th>$B_3$</th>
<th>$B_4$</th>
<th>$R^2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>C13H32</td>
<td>-93.432</td>
<td>-35442209</td>
<td>4092639689</td>
<td>0.9991</td>
<td>7.3985</td>
<td>2759206</td>
<td>-320115246</td>
<td>0.9977</td>
<td></td>
</tr>
<tr>
<td>C15H36</td>
<td>-167.6568</td>
<td>-64932579</td>
<td>7650580115</td>
<td>0.9990</td>
<td>13.1535</td>
<td>5039286</td>
<td>-595426635</td>
<td>0.9982</td>
<td></td>
</tr>
<tr>
<td>C17H36</td>
<td>-101.234</td>
<td>-42652676</td>
<td>5199955241</td>
<td>0.9992</td>
<td>7.4384</td>
<td>3088930</td>
<td>-378708409</td>
<td>0.9976</td>
<td></td>
</tr>
<tr>
<td>C19H40</td>
<td>-235.2681</td>
<td>-95893208</td>
<td>11571460287</td>
<td>0.9998</td>
<td>27.8504</td>
<td>11207165</td>
<td>-1356688401</td>
<td>0.9998</td>
<td></td>
</tr>
</tbody>
</table>
4. Results

In this paper, we derive an expression for as the thermal pressure coefficient of C15H32, C17H36, C18H38 and C19H40 dense fluids using the linear isotherm regularity\[1,3,18\]. Unlike previous models, it has been shown in this work that, the thermal pressure coefficient can be obtained without employing any reduced Helmholtz energy [9-15]. Only, $pVT$ experimental data have been used for the calculation of the thermal pressure coefficient. Comparison of the calculated values of the thermal pressure coefficient using the linear isotherm regularity with the values obtained experimentally show that validity of the use of the Linear isotherm regularity for studying the thermal pres-
pressure coefficient of dense fluids of the monatomic is doubtful [18]. The validity of the use of the linear isotherm regularity equation state for calculating the thermal pressure coefficient of dense fluids of the polyatomic is not also precise [5]. In this work, it has been shown that the temperature dependences of the intercept and slope of using linear isotherm regularity are nonlinear. This problem has led us to try to obtain the expression for the thermal pressure coefficient using the extending the intercept and slope of the linearity parameters versus inversion of temperature to 2 order. The thermal pressure coefficient are predicted from this simple model are in good agreement with experimental data. The results show the accuracy of this method is general quite good.

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REFERENCES
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