Application of High Tension Roll Separator for the Separation of Titanium Bearing Minerals: Process Modeling and Optimization

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ABSTRACT

The High Tension Roll Separator (HTRS) is one of the main electrostatic unit operations employed to separate titanium minerals like ilmenite, rutile and leucoxene which behave as conducting from zircon, sillimanite, garnet and monazite which behave as non-conducting minerals when a high potential difference is applied. Three process inputs, namely roll speed, feed material temperature and roll speed have been optimized. Experiments were conducted based on the Box-Behnken factorial design; the results were analyzed using response surface methodology (RSM). A new term, called Operational Quality Index (OQI) has been defined as a process output, which is maximized by quadratic programming, to obtain the optimum operating conditions. The maximum value of OQI obtained under the constraints of grade >96% and recovery >98% is 195.53, at the following operating conditions—Temperature: 102 °C, Feed Rate: 1.75 tph and Roll Speed: 132 rpm. Under these conditions, the grade and recovery obtained are 96.6% and 98.9% respectively.

Keywords: High Tension Roll Separator; Response Surface Methodology; Titanium; Box-Behnken Design

1. Introduction

Significant research has been dedicated, over the past decade, to enhance plant performance and efficiency to economically concentrate titanium bearing minerals from beach sand deposit. The heavy mineral industry employs different unit operations, in series, to produce high grade titanium minerals (ilmenite, rutile, etc.), with the focus on maximizing recovery, along with the quality. The High Tension Roll Separator (HTRS) is one of the main electrostatic unit operations employed to separate conducting from non-conducting fractions. Titanium minerals like ilmenite, rutile and leucoxene behave as conducting whereas zircon, sillimanite, garnet and monazite behave as non-conducting minerals when a high potential difference is applied.

HTRS are conventional ionizing field separators utilizing a grounded roll to neutralize the charge of the feed material, when passed through high voltage ionizing field. The conducting particles lose their charge to the grounded roll and follow a trajectory depending on the centrifugal force developed by the speed of the rotor. The non-conducting particles are pinned to the roll, transported further and removed by mechanical means like brush or by high voltage AC wiper [1-5]. HTRS is of two types—static and dynamic. The operation efficiency of HTRS depends on the suitable selection of process variables at which the response reaches its optimum, in this case the maximum value. In the present work Response Surface Methodology (RSM) has been used as the optimization tool. This has been widely used as a dependable method of process optimization [6-10]. “Design of Experiments” strategies are available in literature, to be used based on the objective of the work, such as randomized block designs [8,10]. For evaluation of process variables, the two level factorial designs together with response surface methodology has been used because these techniques use factors with more than three levels, and in this way they can establish quadratic models using central composite, Box-Behnken and Doehlert design [6].

The Box-Behnken design followed by the use of RSM has been proposed for the present study. RSM has been widely used for modeling and optimization of process parameters, in particular chemical and pharmaceutical systems [11-18], with limited application in the field of mineral processing. A basic understanding of the factors that influence the separation in a HTRS is well established from classical works [19-21]. In mineral processing, grade and recovery are the important output parameters which will designate the efficiency of the process/separation with variable process inputs. Maximizing these two variable outputs should be the basic aim of any
research in the field of mineral processing.

The HTRS parameters that affect the separation are the roll speed, feed rate, temperature of the feed material, humidity, the feed characteristics such as mineral surface condition, and feed size distribution [1,2]. In the current work, an attempt is made to optimize three process variables of prime importance, namely roll speed, feed rate and temperature of the feed, which are predicted to play a significant role in concentrating titanium minerals (ilmenite, rutile, etc.). In any process plant, under a given set of operating conditions, the grade and recovery are fixed and it is a well-established knowledge that both grade and recovery are inversely related. High grade material can be obtained with very low recovery, which may not be desirable. The reverse of this also holds true. To circumvent this problem, it is proposed to create an index that represents the grade and recovery obtained under the same operating conditions. The value of the process parameters that maximize this index are the true optimum operating conditions. Optimization studies are carried out by using quadratic programming by the mathematical software package MATLAB 7.1.

**Response Surface Methodology**

Response Surface Methodology (RSM) is collection of statistical and mathematical methods that are useful for modeling and analyzing problems. In this technique, the main objective is to optimize the response surface that is influenced by various process parameters. The RSM also quantifies the relationship between the controllable input parameters and the obtained response surfaces [4].

The design procedure of RSM is

1) Designing of a series of experiments for adequate and reliable measurement of the response of interest.
2) Developing a mathematical model of the second order response surface with the best fittings.
3) Finding the optimal set of experimental parameters that produce a maximum or minimum value of response.
4) Representing the direct and interactive effects of process parameters through two and three dimensional plots.

If all variables are assumed to be measurable then the response surface can be expressed as:

\[
 y = f(x_1, x_2, x_3, \ldots x_k) \quad (1)
\]

where \( y \) is the output of the system, and \( x_i \) the variables of action called factors.

The objective is to optimize the response \( y \) with an assumption that the independent variables are continuous and controllable through the experimentation. It is also required to find a suitable approximation for the true functional relationship between independent variables and the response surface, typically a second-order model is utilized in response surface methodology [7,22,23].

\[
 y = \beta_0 + \sum_{i=1}^{k} \beta_i x_i + \sum_{i=1}^{k} \beta_i^2 x_i^2 + \sum_{i=1}^{k} \sum_{j=1}^{k} \beta_{ij} x_i x_j + \varepsilon \quad (2)
\]

where \( x_1, x_2, \ldots, x_k \) are input factors which influence the response \( y; \beta_0, \beta_i, (i = 1, 2, \ldots, k), \beta_{ij} (i = 1, 2, \ldots, k; j = 1, 2, \ldots, k) \) are unknown parameters and \( \varepsilon \) is a random error. The \( \beta \) coefficients, which should be determined in the second-order model, are obtained by the least square method. Generally Equation (2) can be written in matrix form.

\[
 Y = bX + \varepsilon \quad (3)
\]

where \( Y \) is defined to be a matrix of measured values, \( X \) to be a matrix of independent variables. The matrices \( \beta \) and \( \varepsilon \) consist of coefficients and errors, respectively. The solution of Equation (3) can be obtained from the above matrix equation as

\[
 b = \left( X'X \right)^{-1} X'Y \quad (4)
\]

where \( X' \) is the transpose of the matrix \( X \) and \( \left( X'X \right)^{-1} \) is the inverse of the matrix \( X'X \). The coefficients, i.e. the main effect (\( \beta_i \)) and two-factors interactions (\( \beta_{ij} \)) can be estimated from the experimental results by computer simulation programming applying least squares method using MATLAB 7.1. [6,22,23].

**2. Materials and Methods**

**2.1. Materials**

The mineral sample used for this study was taken from the Kuduremokhi region of Tamil Nadu, India. The sample was initially deslimed in the laboratory using hydrocyclone test rig and then concentrated by multistep gravity concentration using spiral concentrator to achieve the desired heavy mineral concentrate i.e. more than 90% heavy minerals [24]. Thus the obtained heavy mineral concentrate has been subjected for the particle size analysis, X-ray diffraction studies, and mineralogical studies. Particle-size measurement of the sand sample was performed using standard laboratory Sieve Shaker. The size distribution of the sample is given in Table 1. As it can be elucidated from Table 1, about 90.5% of the material is having size less than 500 µm; it may also be noted that about 25.5% of the sample is having the size below 125 µm. In order to obtain a closed sized feed material, the sample was subjected to screening using 500 µm as top screen and 125 µm as the bottom screen. Oversize of 500 µm and undersize of 125 µm were removed. Only −500 + 125 µm size fraction was used for the experimental work. The feed sample has been subjected for the X-ray diffraction study for the identification of the mineral phases which has been shown in Figure 1. From Figure 1, it is revealed that the sample contains ilmenite as a major mineral and rutile, monazite, etc.
Table 1. Size distribution of feed sample.

<table>
<thead>
<tr>
<th>Mesh size (µm)</th>
<th>Weight (%)</th>
<th>Cumulative weight % passing</th>
</tr>
</thead>
<tbody>
<tr>
<td>−600 + 500</td>
<td>7.6</td>
<td>100</td>
</tr>
<tr>
<td>−500 + 425</td>
<td>15.8</td>
<td>92.4</td>
</tr>
<tr>
<td>−425 + 355</td>
<td>22.1</td>
<td>76.6</td>
</tr>
<tr>
<td>−355 + 250</td>
<td>17.2</td>
<td>54.5</td>
</tr>
<tr>
<td>−250 + 125</td>
<td>11.8</td>
<td>37.3</td>
</tr>
<tr>
<td>−125 + 100</td>
<td>6.1</td>
<td>25.5</td>
</tr>
<tr>
<td>−100 + 75</td>
<td>3.9</td>
<td>19.5</td>
</tr>
<tr>
<td>−75</td>
<td>15.5</td>
<td>15.5</td>
</tr>
</tbody>
</table>

Table 2. Mineral composition of feed sample.

<table>
<thead>
<tr>
<th>Mineral</th>
<th>Mass %</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ilmenite</td>
<td>71.5</td>
</tr>
<tr>
<td>Rutile</td>
<td>3</td>
</tr>
<tr>
<td>Monazite</td>
<td>1.5</td>
</tr>
<tr>
<td>Zircon</td>
<td>5.2</td>
</tr>
<tr>
<td>Garnet</td>
<td>3.75</td>
</tr>
<tr>
<td>Sillimanite</td>
<td>11.55</td>
</tr>
<tr>
<td>Quartz</td>
<td>3.5</td>
</tr>
</tbody>
</table>

zircon, garnet, sillimanite and quartz minerals are present in minor quantity. The mineralogical studies were carried out for the sample using a Leica petrological optical microscope, to quantify the different minerals. The mineralogical assemblage of the feed sample has been tabulated in Table 2. From Table 2, it is observed that the feed sample contains 74.5% of titanium bearing minerals such as ilmenite and rutile as conducting minerals and remaining minerals such as monazite, zircon, garnet sillimanite and quartz are non-conducting.

2.2. Experimental Work

The sample was then prepared for experiments using HTRS by initial desliming using cyclone test rig, followed by gravity concentration with spirals to achieve about 90% heavy mineral concentrate, containing titanium bearing minerals like ilmenite, rutile and leucoxene, while non-conducting minerals include garnet, zircon, sillimanite, monazite, other heavy minerals like pyroxenes and amphiboles together with free quartz. Close sized sample of −500 + 125 microns was prepared and used for all the experiments. A typical HTRS experiment involved the following sequence steps:

1) Pre-heat the sand to the desired temperature.
2) Start the HTRS rotor and apply voltage.
3) Finally, start the feeder while adjusting the splitter position.

The experimental program was designed to achieve better quality and quantity by suitably selecting the process variables. All the experiments were conducted on laboratory model HTRS (MDL Australia make). The values along with levels of three independent process variables—temperature ($X_1$), feed rate ($X_2$) and roll speed ($X_3$)—that have been used in this study are given in Table 3. All other parameters are kept constant throughout the experiments. The results obtained were used for the computer simulation programming applying least square method.

The levels are chosen to be in sync with plant operation data. The feed rate is suitable for the laboratory—scale HTRS of 250mm diameter. Below 100°C, moisture is retained which affects the separation and heating above 140°C, leads to undesirable wastage of energy.

3. Results and Discussion

A three factor, three levels Box-Behnken design was used to determine the responses such as grade and recovery of the conducting minerals. For any experiment, we calculate the grade and recovery as process outputs. However, since these two are inversely related, maximizing any one would not represent the optimum operating condition. Hence it is proposed to define a new index, Operational Quality Index (OQI), given by,

$$OQI = \frac{\text{Assay value of product} \times \text{Yield} \% \times \text{Assay value of the product}}{\text{Assay value of the feed}}$$

The ideal separation in mineral processing would have an OQI value of 200. However, in all “real” separation practices, OQI would be less than this value. The operating conditions that maximize OQI under constraints are the actual optimum operating condition for the unit operation. The experimental values of OQI obtained from factorial (Box-Behnken) designed experiments are tabulated in Table 4.

From the experimental results, grade and recovery are
TABLE 3. PROCESS VARIABLE VALUES AND LEVELS.

<table>
<thead>
<tr>
<th>S.No</th>
<th>Variables</th>
<th>Levels and codes</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Temperature in °C (X₁)</td>
<td>(-1) 100 120 140</td>
</tr>
<tr>
<td>2</td>
<td>Feed rate in tph (X₂)</td>
<td>(0) 1.5 2.0 2.5</td>
</tr>
<tr>
<td>3</td>
<td>Roll speed in rpm (X₃)</td>
<td>(+1) 120 150 180</td>
</tr>
</tbody>
</table>

TABLE 4. FACTORIAL DESIGN AND OQI VALUES.

<table>
<thead>
<tr>
<th>Exp. No</th>
<th>Condition/coded variables</th>
<th>OQI</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Experimental</td>
</tr>
<tr>
<td>1</td>
<td>-1 -1 0</td>
<td>195.2</td>
</tr>
<tr>
<td>2</td>
<td>1 -1 0</td>
<td>195.2</td>
</tr>
<tr>
<td>3</td>
<td>-1 1 0</td>
<td>194.7</td>
</tr>
<tr>
<td>4</td>
<td>1 1 0</td>
<td>194.4</td>
</tr>
<tr>
<td>5</td>
<td>-1 0 -1</td>
<td>193.3</td>
</tr>
<tr>
<td>6</td>
<td>1 0 -1</td>
<td>185.6</td>
</tr>
<tr>
<td>7</td>
<td>-1 0 1</td>
<td>194.1</td>
</tr>
<tr>
<td>8</td>
<td>1 0 1</td>
<td>195.2</td>
</tr>
<tr>
<td>9</td>
<td>0 -1 -1</td>
<td>193.8</td>
</tr>
<tr>
<td>10</td>
<td>0 1 -1</td>
<td>186.8</td>
</tr>
<tr>
<td>11</td>
<td>0 -1 1</td>
<td>194.4</td>
</tr>
<tr>
<td>12</td>
<td>0 1 1</td>
<td>193.8</td>
</tr>
<tr>
<td>13</td>
<td>0 0 0</td>
<td>195.1</td>
</tr>
<tr>
<td>14</td>
<td>0 0 0</td>
<td>195.1</td>
</tr>
<tr>
<td>15</td>
<td>0 0 0</td>
<td>195.1</td>
</tr>
</tbody>
</table>

A comparison between the predicted values of OQI from Equation (7) and experimental results are made in Figure 2, which shows that predicted values and the observed data points are in very good agreement (R² of 0.91).

In order to check the adequacy of the model in terms of classical statistics, a plot of predicted values vs. residuals is made. As discussed by Montgomery [12], there is no relation between the predicted values and the residuals (Figure 3). In addition, a plot of cumulative normal probability as a function of predicted values is made, showing a satisfactory linear relationship (Figure 4).

Effect of Variables on OQI of Conducting Minerals

As the temperature of the feed material increases at lower roll speeds, the conducting fraction quality increases; on the other hand, at low levels of feed material temperature, the recovery of the conducting materials increases with an increase in roll speed. However, to improve the economy of the process, it is desired to keep grade above a certain specified value and maximize recovery at this level and this condition of operation is achieved with the help of OQI.

For better understanding, the statistical model is described in terms of three dimensional (3D) response surface plots between two independent variables and quality of the conducting minerals at center level of the third variable. Figure 5 shows the effects of temperature and feed rate on OQI of the conducting fraction at center level of roll speed. It is observed that at center level of roll speed there is a trivial effect on OQI with temperature or feed rate variations. This is due to the fact that at higher temperatures, grade obtained is higher. At higher temperatures, the work function is high which results in more pinning effect of the non-conducting particles, thereby affecting the recovery. At higher feed rates and lower temperatures, excessive multilayer formation results in more recovery with low grade. Hence, in this range, the OQI values almost remain constant.

Figure 6 explains the effects of temperature and roll speed on OQI of the conducting fraction at center level of feed rate. The OQI of the conducting fraction in-

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creases initially with increase in roll speed, because of the drastic increase in recovery with respect to rate of quality reduction, due to the fact that the centrifugal force dominates the pinning force of non-conducting particles. Further it may be inferred that the roll speed controls the selective charging at the ionizing zone and discharging to the rotor. With further increase in roll speed above a certain value, there is a drastic lowering of grade of the product.

**Figure 7** shows the effects of feed rate and roll speed at center level of temperature. It can be observed from the figure that there is a trivial effect of feed rate on OQI of the conducting fraction.

Maximizing the functions given by Equations (5) and (6) is done by using the maximization toolbox in MATLAB 7.1. It is observed that a maximum grade of 97.7% is predicted under conditions of high temperature, intermediate feed rate and low roll speed; however, the recovery is only 88.5%. On the other hand, recoveries of around 99.8% can be achieved at low temperatures, high roll speeds and intermediate feed rates, with a product grade of 94.9%. In order to obtain a balance between the recovery and grade, an attempt is made to maximize the variable OQI, with the constraint that grade has to be >96% and recovery >98%. The maximization is done based on Constrained Function Optimization. It is observed that the maximum value of OQI obtained under the given constraints is 195.53. This is obtained at the following operating conditions—Temperature: 102°C, Feed Rate: 1.75 tph and Roll Speed: 132 rpm. Under these operating conditions, from Equations (5) and (6), the grade and recovery obtained are 96.6% and 98.9% respectively.

### 4. Conclusion

The primary process input parameters of a High Tension Roll Separator (HTRS), namely the roll speed of the rotor, feed material temperature and feed rate are optimized in this study, using experimental data and quadratic programming. For the optimization studies, a new
output index—Operational Quality Index (OQI)—has been applied successfully to optimize input parameters for efficient operation. Statistical models were developed for OQI, as well as both grade and recovery of the conducting minerals individually. The predicted values obtained using the models were in very good agreement with the observed values ($R^2$ value of 0.91 for OQI; similar values obtained for both grade and recovery). Process optimization, viz. maximization of OQI has been done by keeping the constraints of grade >96% and recovery >98%. The maximum value of OQI obtained under the given constraints is 195.53, at the following operating conditions—Temperature: 102°C, Feed Rate: 1.75 tph and Roll Speed: 132 rpm. Under these operating conditions, the grade and recovery obtained are 96.6% and 98.9% respectively. Normally, the separation efficiency index, which is a % recovery from the formula, is associated with coal washing processes; while coefficient of separation is nothing but an index derived from recovery/distribution percentages of concentrates and rejects. Though these indices are useful in predicting the process performance, using the quality and quantity of different fractions, these are not completely significant for process variable optimization studies. Therefore, it was found that the concept of OQI is simple and more reliable in this regard.

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REFERENCES


