Model for Prediction of the Concentration of Extracted Tin during Leaching of Cassiterite in Potassium Hydroxide Solution

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ABSTRACT

Model for prediction of the concentration of tin extracted during potassium hydroxide leaching of cassiterite has been derived. The model: \( A = N t^{1.53} \), indicates that the concentration of tin extracted is dependent on the residence time. It was found that the validity of the model is rooted in the expression \( \log A = \log(N t^{1.53}) \). Tin extraction per unit time as obtained from experiment and derived model are 2.6666 and 2.6268 mg/min respectively. The maximum deviation of the model-predicted concentration of dissolved tin from the corresponding concentration obtained from the experiment was found to be less than 8%, which is quite within the acceptable deviation limit of experimental results and hence, impacting about 92% confidence coefficient on the model.

Keywords: Model; Tin; Potassium Hydroxide; Cassiterite; Leaching

1. Introduction

Tin presently finds extensive use in industrial and domestic applications. As a result of this, extraction of tin from ores has continued to attract considerable attention. Extraction of metals from their ores and recovery from their various industrial wastes are a major step towards judicious utilization and conservation of our mineral resources. Various works have been done to extract metals from their ores [1-4]. Cassiterite, otherwise known as tin ore is the only tin mineral from which tin can be extracted in a commercial quantity. Matell [5] studied the extraction of tin from its ores by reduction of cassiterite to tin metal and then extracting the tin with aqueous inorganic acids.

Models are of central importance in many scientific contexts, useful for testing, analysis or training where real-world systems or concepts can be represented by a model [6,7]. One of such models as reported by Hwang et al. [7] is a numerical simulation of heat transfer during the microwave heating process of a two dimensional, magnetic dielectric, magnetite, subjected to heat conduction, convection and radiation. The heat transfer process was modeled using an explicit finite difference approach and the temperature profile for different heating parameters was generated through developing a code in mathematica 7.0.

The derivation of models for the evaluation of the concentration of some metal values leached in some ores, concentrates, calcine or other solid materials containing metal(s) in some aqueous solutions of acids, bases, complexing agents, etc has gained very wide interest among researchers in recent time. Many models have been evaluated involving the use of different acids for the leaching of some ores. One of such works as reported by Nwoye [8] is the model for the computational analysis of the solution temperature during leaching of iron oxide ore in hydrochloric acid solution. The model is expressed as:

\[ T = e^{N_t \gamma} \]  \hspace{1cm} (1)  
\[ T = e^{(8.9055/\gamma)} \]  \hspace{1cm} (2)

where \( T \) is the solution temperature (°C) during leaching of iron oxide ore using hydrochloric acid; \( N_t = 8.9055 \) (pH coefficient for hydrochloric acid solution during leaching of iron oxide ore) determined by Nwoye et al. [9]; \( \gamma \) is the final pH of the leaching solution at the time \( t \) when the solution temperature is evaluated.

Nwoye [10] also derived a model for computational analysis of the concentration of dissolved haematite and
heat absorbed by oxalic acid solution used during leaching of iron oxide ore. The models are:

\[ \% \text{Fe}_2\text{O}_3 = K \left( \frac{Z}{\mu} \right) \]  
(3)

\[ Q = K \cdot \mu \]  
(4)

where

\% \text{Fe}_2\text{O}_3 = \text{Concentration of dissolved haematite in oxalic acid solution;}

\( \gamma \) = Final pH of the leaching solution at time t at which \% \text{Fe}_2\text{O}_3 was obtained;

\( \mu \) = Weight of iron oxide added into the oxalic acid leaching solution (g);

\( K \) = Constant of proportionality associated with heat absorption;

\( Q \) = Quantity of heat (J) absorbed by oxalic acid solution during the leaching process (J).

Successful attempt has also been made [11] to derive a model for computational analysis of heat absorbed by hydrogen peroxide solution relative to the weight of iron oxide ore added. It is of the form:

\[ % \text{Fe}_2\text{O}_3 = \mu^{1.53} \]  
(5)

where \( \mu \) is the weight input of iron oxide ore (g); \% \text{Fe}_2\text{O}_3 and \% \text{Fe} are the concentrations of dissolved haematite and iron respectively in hydrogen peroxide solution during leaching. The model is rooted on the expression \( \% \text{Fe}_2\text{O}_3 \approx \% \text{Fe} \cdot (\mu)^{1.53} \) where both sides of the relationship are correspondingly almost equal.

The aim of this work is to develop a model for predicting the concentration of extracted tin during leaching of cassiterite in potassium hydroxide solution.

2. Materials and Methods

2.1. Materials

The sample of cassiterite ore concentrate used for this study was obtained from Jos, Plateau State, Nigeria.

2.2. Methods

2.2.1. Leaching Experiment

The ore was crushed to particle size of \( -212 \mu \text{m} \). Conventional leaching experiments were carried out in glass vessels which were put in a temperature-controlled water bath. Stirring was carried out using an overhead mechanized stirrer and a glass impeller. 250 ml of the leaching solution was heated to the desired temperature and then 1.0 g of cassiterite ore was added. Periodic sampling of 5 ml of liquor was drawn for chemical analysis using ICP-OES (Inductively Coupled Plasma—Optical Emission Spectrometer).

\[
\text{2.2.2. Model Formulation}
\]

Experimental results shown in Table 1 were used for the model derivation. Computational analysis on the experimental data in Table 1 using C-NIKBRAN (Nwoye, 2008) as shown in Table 2 resulted to Table 3 which indicates that

\[
\log A = \log \left( N t^{1.53} \right) \quad \text{approximately}
\]  
(6)

\[
A = N t^{1.53}
\]  
(7)

Introducing the value of \( N \) into Equation (7),

\[
A = 0.1898 t^{1.53}
\]  
(8)

where

\( A \) = Concentration (mg) of tin dissolved during leaching of cassiterite ore using potassium hydroxide solution;

\( N = 0.1898 \), interaction factor between ore and leaching solution;

1.53 = The leachability of the leaching solution.

Equation (8) is the derived model.

2.2.3. Model Validation

This model was validated using the correlation coefficients (CORREL), sum square techniques (SSQ) and

\[
| \begin{array}{c|c|c}
\text{Time (min)} & A_{exp} (mg) & A_{cal} (mg) \\
\hline
10 & 7.2 & 7.2 \\
30 & 30.8 & 30.8 \\
45 & 68.9 & 68.9 \\
60 & 112.0 & 112.0 \\
90 & 199.3 & 199.3 \\
110 & 257.6 & 257.6 \\
120 & 286.8 & 286.8 \\
\end{array}
| \]

Table 1. Experimental result of the variation of the concentration of tin obtained with time (conditions: 4 M KOH, temperature: 80°C, agitation speed: 500 rpm, particle size: \(-212 \mu\text{m}\)).

\[
| \begin{array}{c|c|c|c|c}
\text{Time (min)} & A_{exp} (mg) & \log A & 1.53 \log t & \text{Log0.1898} \\
\hline
10 & 7.2 & 0.8573 & 1.5300 & -0.7217 \\
30 & 30.8 & 1.4886 & 2.2600 & -0.7217 \\
45 & 68.9 & 1.8382 & 2.5294 & -0.7217 \\
60 & 112.0 & 2.0492 & 2.7206 & -0.7217 \\
90 & 199.3 & 2.2995 & 2.9900 & -0.7217 \\
110 & 257.6 & 2.4109 & 3.1233 & -0.7217 \\
120 & 286.8 & 2.4576 & 3.1812 & -0.7217 \\
\end{array}
| \]

Table 2. Analysis table showing variation of \( \log A \) with 1.53 \( \log t \).
Table 3. Variation of (LogA) with (Log0.1898 + 1.53 Logt).

<table>
<thead>
<tr>
<th>Time (min)</th>
<th>LogA</th>
<th>Log0.1898 + 1.53 Logt</th>
</tr>
</thead>
<tbody>
<tr>
<td>10</td>
<td>0.8573</td>
<td>0.8085</td>
</tr>
<tr>
<td>30</td>
<td>1.4886</td>
<td>1.5383</td>
</tr>
<tr>
<td>45</td>
<td>1.8382</td>
<td>1.8077</td>
</tr>
<tr>
<td>60</td>
<td>2.0492</td>
<td>1.9989</td>
</tr>
<tr>
<td>90</td>
<td>2.2995</td>
<td>2.2683</td>
</tr>
<tr>
<td>110</td>
<td>2.4109</td>
<td>2.4016</td>
</tr>
<tr>
<td>120</td>
<td>2.4576</td>
<td>2.4595</td>
</tr>
</tbody>
</table>

statistical and graphical methods.

2.2.4. Correlation Coefficients
The correlation coefficient is a measure of the degree of interaction between process parameters acting as dependent and independent variables.

2.2.5. Sum Square Deviational Method
The sum square deviation is the measure of the goodness of fit for each point. The difference between the prediction by the model and the observed is value squared given by the expression:

$$SSQ = \frac{\sum (Y(a,k_i,k_j) - Y_{exp})^2}{n}$$  \hspace{1cm} (9)

It is a direct measure of the accuracy of the average observation when divided by the number of observations and the square root taken. The smaller the average distance, the better the fit.

2.2.6. Statistical and Graphical Method
The validity of the model was established by comparing the model-predicted values and the experimental values. Comparison between these two values reveals deviations which were due to the physiochemical interactions between the ore and the leaching solution and also due to the surface properties of the ore, which were found to have played vital roles during the leaching process [11].

It is then expected that a correction factor be added to the model-predicted values to make up for those factors neglected during the model formulation.

The deviation, $Dv$ (%), of model-predicted $A$ values from the experimental values is expressed as:

$$Dv = \frac{A_{mod} - A_{exp}}{A_{exp}} \times 100$$  \hspace{1cm} (10)

where

$A_{mod}$ is the model-predicted concentration of tin leached out, and $A_{exp}$ is the corresponding experimental value.

Correction factor ($Cf$), if expressed as the negative of the deviation, then,

$$Cf = -Dv$$  \hspace{1cm} (11)

and

$$Cf = -100\left(\frac{A_{mod} - A_{exp}}{A_{exp}}\right)$$  \hspace{1cm} (12)

Addition of the corresponding $Cf$ values obtained from Equation (12) to the model-predicted values of the concentration of tin leached gives the exact experimental values.

3. Results and Discussion

3.1. Results
The results of the experiment on the variation of concentration of tin obtained with time is shown in Table 1, while that of the analysis of the variation of the model variables are presented in Tables 2, 3 and 4 respectively. The effects of residence time on the concentration of tin dissolved from experiment and as predicted by the derived model are presented in Figures 1 and 2 respectively. The graph of the comparison of the results obtained from the experiment and the derived model is as in Figure 3.

3.2. Discussion of Results
The correlation coefficients R between concentration of tin extracted and residence time as obtained from the experiment and derived model (Table 4) were calculated using Microsoft EXCEL as 0.9942 and 0.9916 respectively. Comparison of these proximate correlation coefficients indicates validity of the derived model.

The obtained value of the sum squared technique (SSQ) from Equation (9) and Table 4 is compared with average sum of the experimental results. The value is 5.92% deviation. This confers a high degree validity of 92% confidence coefficient.

The derived model is Equation (8). The comparison of Table 4. Comparison between concentrations of tin removed as predicted by model and as obtained from experiment.

<table>
<thead>
<tr>
<th>Time (min)</th>
<th>$A_{exp}$</th>
<th>$A_{mod}$</th>
<th>$Dv$ (%)</th>
<th>$Cf$ (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>10</td>
<td>7.2</td>
<td>6.4313</td>
<td>-10.68</td>
<td>+10.68</td>
</tr>
<tr>
<td>30</td>
<td>30.8</td>
<td>34.5376</td>
<td>+12.14</td>
<td>-12.14</td>
</tr>
<tr>
<td>45</td>
<td>68.9</td>
<td>64.2261</td>
<td>-6.78</td>
<td>+6.78</td>
</tr>
<tr>
<td>60</td>
<td>112.0</td>
<td>99.7396</td>
<td>-10.95</td>
<td>+10.95</td>
</tr>
<tr>
<td>90</td>
<td>199.3</td>
<td>185.4758</td>
<td>-6.94</td>
<td>+6.94</td>
</tr>
<tr>
<td>110</td>
<td>257.6</td>
<td>252.1314</td>
<td>-2.12</td>
<td>+2.12</td>
</tr>
<tr>
<td>120</td>
<td>286.8</td>
<td>288.0338</td>
<td>+0.43</td>
<td>-0.43</td>
</tr>
</tbody>
</table>

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Figure 1. Effect of residence time on the concentration of dissolved tin as obtained from the experiment.

Figure 2. Effect of residence time on the concentration of tin dissolved as predicted by the derived model.

Figure 3. Comparison of the concentration of dissolved tin in relation to the residence time as obtained from experiment and derived model.

The concentrations of dissolved tin as predicted by the model ($A_{mod}$) with those obtained from the experiments show insignificant positive and negative deviations, hence, depicting the reliability and validity of the model.

The data on deviations are shown in Table 4. The average deviation is calculated to be 7.15%, which is quite within the acceptable deviation limits from experimental results. The validity of the model is found to be rooted in Equation (8) where both sides are correspondingly approximately equal. Table 3 is also in agreement with Equation (6) where the values of $\log A$ is approximately equal to the value of $\log (N^{1.53})$.

The rate of dissolution (concentration of tin dissolved per unit time) (mg/min) was determined using the experimental values and the model-predicted values as per the following equation:

$$ A_t = \frac{A}{t} + c \quad (12) $$

Equation (12) therefore, implies that a plot of concentration of tin dissolved against residence time should give a straight line (Figure 1) with a slope equal to $S$, where $S$ is:

$$ S = \frac{\Delta A}{\Delta t} \quad (13) $$

and $\Delta A = \text{change in the concentration of tin dissolved} \ (A_1, A_2) \ \text{at times} \ t_2, t_1$.

Figure 1 gives a slope of 2.6666 mg/min, which is the concentration of tin removed per unit time during the actual experimental leaching process. Also, a similar plot (Figure 2) using the model-predicted values gave a slope equal to 2.6268 mg/min. This is the model-predicted concentration of dissolved tin per unit time of the leaching process. A comparison of these two rates shows a proximate agreement, indicating a high degree of validity for the model. Figure 3 showed that both the values of the dissolved tin from experiment (line $A_{exp}$) and the derived model (line $A_{mod}$) in relation to residence time are generally quite close, indicating proximate agreement and validity of the proposed model.

4. Conclusion

The model predicts the concentration of tin dissolved during leaching of cassiterite in potassium hydroxide solution. The validity of the models is rooted on the expression $\log A = \log 0.1898 \cdot t^{1.53}$ where both sides of the relationship are correspondingly approximately equal. Tin extraction per unit time as obtained from experiment and...
The average deviation of the amount of the model-predicted concentration of tin from the corresponding experimental values was found to be less than 8%, which is quite within the acceptable range of deviation limit of experimental results. Also, the rate of dissolution as obtained from experiment and derived model show proximate agreement, and hence, indicates a very high degree of validity for the model.

REFERENCES


