

Gedanken Experiment for Initial Expansion of the Universe and Effects of a Nearly Zero Inflaton in Pre-Planckian Physics Space-Time Satisfying Traditional Slow Roll Formulas Which Happens in Pre-Planckian Regimes Even If $\dot{\phi}^2 \gg V_{\text{SUSY}}$

Andrew Walcott Beckwith

Physics Department, College of Physics, Chongqing University Huxi Campus, Chongqing, China

Email: Rwill9955b@gmail.com, abeckwith@uh.edu

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Abstract

We first of all consider what if the initial inflaton was nearly zero instead of proportional to a Planck mass, in a SUSY type potential. Using the construction of Padmanabhan about general inflaton physics and the conditions of what are usual constituent slow roll requirements for inflation, and also of Kolb, Pi and Raby about a SUSY potential, we come up with the counter intuitive formulation of how usual tests for slow roll give the standard answers even if the inflaton in the SUSY potential as given by Kolb, Pi, and Raby is initially zero. The result gives support to a formulation of VEV conditions used right after a Planck instant of time. As it is, we will from first principles examine what adding acceleration does as to the HUP previously derived. In doing so we will be tying it in our discussion with the earlier work done on the HUP. The HUP results, so modified are appropriate for the Pre-Planckian results and may explain why the slow roll formulation as given by Padmanabhan holds where there is the phenomenon of $\dot{\phi}^2 \gg V_{\text{SUSY}}$ for Pre-Planckian space-time. This leads to a very paradoxical result that in Pre-Planckian physics the traditional slow roll formulas are satisfied even if $\dot{\phi}^2 \gg V_{\text{SUSY}}$. But it also puts in extremely tight restrictions upon the formulation of the degree of freedom problem, as given in Equation (26) in this document.

Keywords

Inflaton, SUSY, VEV, Heisenberg Uncertainty Principle, Slow Roll, Pre-Planckian

1. Introduction to the Basic Problem, as Far as SUSY Potential Physics. Starting off with a Summary of Why $\phi \sim \xi^+ \ll M_{\text{Planck}}$ in $\dot{\phi}^2 \gg V_{\text{SUSY}}$ Situations, so the Square of H , Is >0

In this introduction, we use the results of how we set the state for a modified Pre-Planckian physics HUP. This will be leading to initial conditions which will lead to, later $\dot{\phi}^2 \gg V_{\text{SUSY}}$ in Pre-Planckian space-time physics, which will in turn lead to our main analysis result that in the Pre-Planckian Space-time, that $\dot{\phi}^2 \gg V_{\text{SUSY}}$, will still lead to space-time conditions for which we have, the slow roll conditions, as outlined by Padmanabhan [1], which merge seamlessly into the inflationary conditions, even if, in the Planckian space-time we have $\dot{\phi}^2 \ll V_{\text{SUSY}}$. In the regime which we have $\dot{\phi}^2 \gg V_{\text{SUSY}}$ we have that $\phi \sim \xi^+ \ll M_{\text{Planck}}$, for times $t \ll$ Planck time interval. By the time we have $\dot{\phi}^2 \ll V_{\text{SUSY}}$ we have that $\phi \sim M_{\text{Planck}}$ for Planck time. One of the findings will be that the square of the Hubble parameter, when $\phi \sim \xi^+ \ll M_{\text{Planck}}$, will be >0 only if $\dot{\phi}^2 \gg V_{\text{SUSY}}$, which occurs when the time is in the Pre-Planckian space-time regime and $\phi \sim M_{\text{Planck}}$ when time is Planck time in value, just before the advent of inflation. In doing so, if $\phi \sim M_{\text{Planck}}$, $\dot{\phi}^2 \gg V_{\text{SUSY}}$ no longer holds. But to get to this derivation, we will attempt to set up a modification of the HUP which will be part of how $\phi \sim \xi^+ \ll M_{\text{Planck}}$ in $\dot{\phi}^2 \gg V_{\text{SUSY}}$ situations, so the square of H , is >0 . This will be linked to the modification of the HUP brought up, which is largely from [2]. This leads to the satisfaction of the slow roll hypothesis, usual formulation still holding in the Pre-Planckian regime, in spite that $\phi \sim \xi^+ \ll M_{\text{Planck}}$, will be >0 only if $\dot{\phi}^2 \gg V_{\text{SUSY}}$.

2. Re-Hash of Discussion Given in [2] about Modification of HUP

As stated in [2] we will be examining a Friedmann equation for the evolution of the scale factor, using explicitly one case being when the acceleration of expansion of the scale factor is kept in, and the intermediate cases of when the acceleration factor, and the scale factor is important but not dominant. In doing so we will be tying it in our discussion with the earlier work done on the HUP but from the context of how the acceleration term will affect the HUP, and making sense of [2]

$$\left\langle (\delta g_{uv})^2 (\hat{T}_{uv})^2 \right\rangle \geq \frac{\hbar^2}{V_{\text{Volume}}^2} \xrightarrow{uv \rightarrow tt} \left\langle (\delta g_{tt})^2 (\hat{T}_{tt})^2 \right\rangle \geq \frac{\hbar^2}{V_{\text{Volume}}^2} \quad (1)$$

$$\& \delta g_{rr} \sim \delta g_{\theta\theta} \sim \delta g_{\phi\phi} \sim 0^+$$

Namely we will be working with [2]

$$\delta t \Delta E = \frac{\hbar}{\delta g_{tt}} \equiv \frac{\hbar}{a^2(t) \cdot \phi} \ll \hbar \quad (2)$$

$$\Leftrightarrow S_{\text{initial}} (\text{with} [\delta g_{tt}]) = (\delta g_{tt})^{-3} S_{\text{initial}} (\text{without} [\delta g_{tt}]) \gg S_{\text{initial}} (\text{without} [\delta g_{tt}])$$

i.e. the fluctuation $\delta g_{tt} \ll 1$ dramatically boost initial entropy. Not what it

would be if $\delta g_{tt} \approx 1$. The next question to ask would be how could one actually have [2]

$$\delta g_{tt} \sim a^2(t) \cdot \phi \xrightarrow{\phi \sim \text{Very Large}} 1 \tag{3}$$

In short, we would require an enormous “inflaton” style ϕ valued scalar function, and $a^2(t) \sim 10^{-110}$. How could ϕ be initially quite large? Within Planck time the following for mass holds, as a lower bound [2] [3] [4]

$$m_{\text{graviton}} \geq \frac{2\hbar^2}{(\delta g_{tt})^2 l_P^2} \cdot \frac{(E-V)}{\Delta T_{tt}^2} \tag{4}$$

Here, [2]

$$K.E. \sim (E-V) \sim \dot{\phi}^2 \propto a^{-6} \tag{5}$$

3. What Is the Argument against the Usual Heisenberg Uncertainty Principle?

We will be looking at the likelihood of recovery of the usual Heisenberg uncertainty principle as would be seen if [2]

$$\delta g_{tt} \sim a^2(t) \cdot \phi \xrightarrow{\phi \sim \text{Very Large}} 1 \tag{6}$$

In short, we would require an enormous “inflaton” style ϕ valued scalar function, and $a^2(t) \sim 10^{-110}$, *i.e.* assuming a quantum bounce with $a^2(t) \sim 10^{-110}$, but not zero, so as to have Equation (2) render the usual Heisenberg uncertainty principle, would require a scalar value ϕ initially of almost infinite value, and there is no reason this would occur, *i.e.* what we will attempt to do is to model inputs from what can be deduced via deconstructing the super symmetric models, as so beloved by the physics community.

4. The SUSY Potential Utilized. And Its Role for

$\phi \sim \xi^+ \ll M_{\text{Planck}}$ in $\dot{\phi}^2 \gg V_{\text{SUSY}}$ Situations, So the Square of H , Is >0

Going to Kolb, Pi, and Raby, [5] we outline certain problems with the usual SUSY models which in effect argues strongly against a scalar value ϕ initially of almost infinite value. The target of what we are examining is an old but still referenced model of inflation in the case of a super symmetric potential of the form of a VEV, which is what we should be considering, namely, if we use a scalar value ϕ of a Higgs field, with

$$V(\text{SUSY} - \text{VeV}) \cong \mu^4 \cdot \left[1 - \tilde{b} \cdot \ln\left(\frac{\phi}{\mu}\right) \right] + O\left(\frac{\mu}{\phi}\right) \tag{7}$$

With [] a minimum value for Equation (23) according to the first derivative, ϕ , if μ is the super symmetry breaking scale, and

$$\begin{aligned} \tilde{b} &= -b \ln\left(\frac{\phi\mu}{m_{\text{Planck}}^2}\right) \\ &\&b = O(1) \end{aligned} \tag{8}$$

Were this followed, we would also would have a defined mass, for the scalar field which is given in [] by the following

$$\mu_\phi^2 \cong \frac{\mu^4}{m_{\text{Planck}}^2} \tag{9}$$

With a minimization of a SUSY style Equation (7), and Equation (9) below if $\phi \cong m_{\text{Planck}}$. The contention we have is that if one wanted to have Equation (9) satisfied, that with the scale factor ALMOST zero, but not zero, that there is no way to have $\phi \cong m_{\text{Planck}}$, and to keep fidelity with the usual HUP relationships of change in energy times change in time as greater than or equal to \hbar . Here is the [] provided SUSY potential for a vanishing VeV [5]

$$V(\phi) = \mu^4 \cdot \left[b \cdot \ln^2 \left(\frac{\phi}{m_{\text{Planck}}} \right) + \left(1 - \left(\frac{\phi}{m_{\text{Planck}}} \right)^2 \right)^2 \right] \tag{10}$$

i.e. this is still, with some tweaking a commonly accepted SUSY VeV model, with a minimum if $\phi \cong m_{\text{Planck}}$, and due to Equation (10) we can argue pretty straight forwardly, that if $\phi \cong m_{\text{Planck}}$ no longer holds, that the variation in the Pre-Planckian metric as brought up in Equation (10) will NOT allow for the resumption of the usual HUP

So, $\Delta E \Delta t \geq \hbar$ will in the Pre-Planckian regime, break down [2]. We will next then consider what to expect if there is a dynamical systems treatment for an emergent VeV and what this says physically.

5. Examining What Happens to Equation (10) If in Pre Planckian Space Time $\phi^2 \gg V_{\text{SUSY}}$ due to

$$\phi \sim \xi^+ \ll M_{\text{Planck}}$$

We will be looking at the value of Equation (10) if $\phi \sim \xi^+ \ll M_{\text{Planck}}$. In short, we have then that

$$\begin{aligned} (\Delta l)_{ij} &= \frac{\delta g_{ij}}{g_{ij}} \cdot \frac{l}{2} \\ (\Delta p)_{ij} &= \Delta T_{ij} \cdot \delta t \cdot \Delta A \end{aligned} \tag{11}$$

If we use the following, from the Robertson-Walker metric [2] [6] [7].

$$\begin{aligned} g_{tt} &= 1 \\ g_{rr} &= \frac{-a^2(t)}{1 - k \cdot r^2} \\ g_{\theta\theta} &= -a^2(t) \cdot r^2 \\ g_{\phi\phi} &= -a^2(t) \cdot \sin^2 \theta \cdot d\phi^2 \end{aligned} \tag{12}$$

Following Unruth [8] [9], write then, an uncertainty of metric tensor as, with the following inputs

$$a^2(t) \sim 10^{-110}, r \equiv l_p \sim 10^{-35} \text{ meters} \tag{13}$$

Then, the surviving version of Equation (7) and Equation (8) is, then, if

$$\Delta T_u \sim \Delta \rho \quad [2] [8] [9]$$

$$V^{(4)} = \delta t \cdot \Delta A \cdot r$$

$$\delta g_{uu} \cdot \Delta T_u \cdot \delta t \cdot \Delta A \cdot \frac{r}{2} \geq \frac{\hbar}{2} \Leftrightarrow \delta g_{uu} \cdot \Delta T_u \geq \frac{\hbar}{V^{(4)}} \quad (14)$$

This Equation (14) is such that we can extract, up to a point the HUP principle for uncertainty in time and energy, with one very large caveat added, namely if we use the fluid approximation of space-time [10]

$$T_{ii} = \text{diag}(\rho, -p, -p, -p) \quad (15)$$

Then [2]

$$\Delta T_u \sim \Delta \rho \sim \frac{\Delta E}{V^{(3)}} \quad (16)$$

Then,

$$\delta t \Delta E \geq \frac{\hbar}{\delta g_{uu}} \neq \frac{\hbar}{2} \quad \text{Unless } \delta g_{uu} \sim O(1) \quad (17)$$

How likely is $\delta g_{uu} \sim O(1)$? Not going to happen.

6. How We Can Justifying Writing $\delta g_{rr} \sim \delta g_{\theta\theta} \sim \delta g_{\phi\phi} \sim 0^+$ Values. And Other Inequalities

To begin this process, we will break it down into the following coordinates. In the rr , $\theta\theta$, and $\phi\phi$ coordinates, we will use the Fluid approximation, $T_{ii} = \text{diag}(\rho, -p, -p, -p)$ [2] with

$$\delta g_{rr} T_{rr} \geq - \left| \frac{\hbar \cdot a^2(t) \cdot r^2}{V^{(4)}} \right| \xrightarrow{a \rightarrow 0} 0$$

$$\delta g_{\theta\theta} T_{\theta\theta} \geq - \left| \frac{\hbar \cdot a^2(t)}{V^{(4)}(1 - k \cdot r^2)} \right| \xrightarrow{a \rightarrow 0} 0 \quad (18)$$

$$\delta g_{\phi\phi} T_{\phi\phi} \geq - \left| \frac{\hbar \cdot a^2(t) \cdot \sin^2 \theta \cdot d\phi^2}{V^{(4)}} \right| \xrightarrow{a \rightarrow 0} 0$$

If as an example, we have negative pressure, with T_{rr} , $T_{\theta\theta}$, and $T_{\phi\phi} < 0$, and $p = -\rho$, then the only choice we have, then is to set $\delta g_{rr} \sim \delta g_{\theta\theta} \sim \delta g_{\phi\phi} \sim 0^+$, since there is no way that $p = -\rho$ is zero valued. If so, then we will go to the behavior of Equation (10) and $\dot{\phi}^2 \gg V_{\text{SUSY}}$ due to $\phi \sim \xi^+ \ll M_{\text{Planck}}$.

1) Working with Equation (10) as a link to $\dot{\phi}^2 \gg V_{\text{SUSY}}$ due to $\phi \sim \xi^+ \ll M_{\text{Planck}}$

The key equation is to look at the following expression for the Hubble parameter, which is [1]

$$H^2 = \frac{1}{3M_p^2} \cdot \left(\frac{\dot{\phi}^2}{2} + V_{\text{SUSY}} \right) \quad (19)$$

Here, we will be having $\dot{\phi}^2 \gg V_{\text{SUSY}}$ due to $\phi \sim \xi^+ \ll M_{\text{Planck}}$ because, then The key equation is to look at the following expression for the Hubble parameter,

ter, which is leading to

$$\begin{aligned}
 \dot{\phi}^2 &\gg V_{\text{SUSY}} \\
 \phi &\sim \xi^+ \ll M_{\text{Planck}} \\
 \phi &\sim M_{\text{Planck}} \\
 H^2 &= \frac{1}{3M_P^2} \cdot \left(\frac{\dot{\phi}^2}{2} + V_{\text{SUSY}} \right) \\
 \left(\frac{\dot{\phi}^2}{2} + \left[V = V_{\text{SUSY}} (\phi \sim \xi^+ \ll M_{\text{Planck}}) \right] \right) &> 0 \\
 \text{if } \dot{\phi}^2 &\gg \left| V = V_{\text{SUSY}} (\phi \sim \xi^+ \ll M_{\text{Planck}}) \right| \\
 \text{with } V &= V_{\text{SUSY}} (\phi \sim \xi^+ \ll M_{\text{Planck}}) \ll 0 \\
 \text{and } V_{\text{SUSY}} = V(\phi) &= \mu^4 \cdot \left[b \cdot \ln^2 \left(\frac{\phi}{m_{\text{Planck}}} \right) + \left(1 - \left(\frac{\phi}{m_{\text{Planck}}} \right)^2 \right)^2 \right] \\
 \tilde{b} &= -b \ln \left(\frac{\phi \mu}{m_{\text{Planck}}^2} \right)
 \end{aligned} \tag{20}$$

2) Working with Slow Roll If we are using Equation (20) if $\phi \sim \xi^+ \ll M_{\text{Planck}}$

From using Padmanabhan [1], we have the following which we write as for slow roll parameters

$$\begin{aligned}
 \epsilon(\phi) &= \frac{M_P^2}{2} \cdot \left(\frac{\left(\frac{\partial V(\phi)}{\partial \phi} \right)}{V(\phi)} \right)^2 \\
 \eta(\phi) &= M_P^2 \cdot \left(\frac{\left(\frac{\partial^2 V(\phi)}{\partial \phi^2} \right)}{V(\phi)} \right)
 \end{aligned} \tag{21}$$

Then, if $\phi \sim \xi^+ \ll M_{\text{Planck}}$

$$\begin{aligned}
 \epsilon(\phi) &= \frac{M_P^2}{2} \cdot \left(\frac{\left(\frac{\partial V(\phi)}{\partial \phi} \right)}{V(\phi)} \right)^2 \Bigg|_{\phi \sim \xi^+ \ll M_{\text{Planck}}} \sim \frac{2}{\ln^2(\xi^+ / M_{\text{Planck}})} \sim 0^+ \\
 \eta(\phi) &= M_P^2 \cdot \left(\frac{\left(\frac{\partial^2 V(\phi)}{\partial \phi^2} \right)}{V(\phi)} \right) \Bigg|_{\phi \sim \xi^+ \ll M_{\text{Planck}}} \sim \frac{2}{\ln^2(\xi^+ / M_{\text{Planck}})} \sim 0^+
 \end{aligned} \tag{22}$$

Note that this is commensurate with this K.E. as proportional to have the left side of Equation (22) almost infinite in value and in turn that also relates to

$$\begin{aligned} \delta g_{tt} &\sim a^2(t) \cdot \phi \ll 1, \\ \text{if } \phi_{\text{initial}} &\sim \xi^+ \end{aligned} \quad (23)$$

Which due to [11] becomes similar to using Equation (24) in

$$\rho_w \propto a^{-3(1-w)} \quad (24)$$

Then by Equation (23) and Equation (24)

$$\Delta E \sim \frac{\hbar}{\delta t \cdot [\delta g_{tt} \sim a^2(t) \cdot \phi]} \sim \rho \cdot V (\text{volume}) \quad (25)$$

If we are in a very small Pre-Planckian regime of space-time, we could, then write Equation (24) as then proportional to $g^* T^4$ [11], with g^* initial degrees of freedom, leading to $w = 1/3$, and initial degrees of freedom as

$$g^* \sim \frac{\hbar}{\delta t_{\text{initial}} \cdot [a_{\text{initial}}^2(t) \cdot \phi_{\text{initial}} \cdot T_{\text{initial}}^4 \cdot V (\text{initial-volume})]} \quad (26)$$

As given by Kolb and Turner, the projected degrees of freedom max out about 110, while unorthodox treatment of the same problem lead to an upper bound of about 1000. Needless to say though, the given Equation (26) only works if there is an extremely small, almost zero inflaton value, as given by the following: $\phi \sim \xi^+ \ll M_{\text{Planck}}$. This is to counteract the enormity of the initial temperature. We will say more about this topic later in subsequent publications.

7. Conclusion

We think the only explanation is that even if Equation (21) and Equation (22) are not satisfied with an almost zero inflaton magnitude, the only explanation we have is of a causal discontinuity which would effectively wipe out a good deal of the information and structure from Pre-Planckian to Planckian space time, even if the behavior of Equation (21) and Equation (22) is commensurate with the Planckian slow roll conditions. We will write more of this in a subsequent publication. This will complete our full development of an extension of [12] as well as issues raised in [13], and [14] where Corda calculated the magnitude of the inflaton, which has results which we will try to reconcile as to our present theoretical developments.

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