Hydrodynamic Performance Analysis of the Ducted Propeller Based on the Combination of Multi-Block Hybrid Mesh and Reynolds Stress Model

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Abstract

In order to analyze the hydrodynamic performance of the ducted propeller with high precision, this paper proposes a new method which combines Multi-Block Hybrid Mesh and Reynolds Stress Model (MBHM & RSM). The calculation errors of MBHM & RSM and standard two-equation model (standard k-ε model) on the ducted propeller JD7704 +Ka4-55 are compared. The maximum error of the total thrust coefficient $K_T$, the duct thrust coefficient $K_{TN}$, the torque coefficient $K_Q$ and the open-water efficiency $\eta_0$ of MBHM & RSM are 2.98%, 4.01%, 1.46%, and 0.89%, respectively, which are lower than those of standard k-ε model. Indeed, the pressure distribution on the propeller surfaces, the pressure and the velocity vector distribution of the flow field are also analyzed, which are consistent with the theory. It is demonstrated that MBHM & RSM on the thruster dynamics analysis are feasible. This paper provides reference in the thruster designing of underwater robot.

Keywords

Multi-Block Hybrid Mesh, RSM, Ducted Propeller, Hydrodynamic Performance

1. Introduction

The propeller of a Remotely Operated Vehicle (ROV) is an important part, whose dynamic performance deter-
mines the motion characteristics, control performance and efficiency of underwater robot. In recent years, many scholars engage in the research of the dynamics performance of the ducted propeller. For example, Baltazar et al. [1] analyzed the open water performance of the propeller with and without duct using panel method, but the error is high. Moustafa Abdel-Maksoud et al. [2] designed a multi-component propulsor, and the hydrodynamic performance is done in both 2D and 3D with numerical method. Long Yu et al. [3] investigated the open water performance of Ka-series propeller combined with 19A duct by the panel method and the numerical method, and a 3D-geometry generate method is proposed. H. Haimov et al. [4] combined the calculation methods and model tests to calculate the hydrodynamic problem of the Ka4-60-19A, and the RANSE solution has sufficient precision.

Yet, the finite element meshes in the numeral calculation of propeller mentioned above are regular grid, and the calculation models are limited to the two-equation model, such as the standard k-ε model, which may affect the precision and speed of calculation to some extent. Considering the complexity of the geometry, flow field characteristics and the precision of calculation, a kind of multi-block hybrid mesh combined with the RSM is put forward in this paper. The convection and diffusion effect of Reynolds stress is fully considered, and the Reynolds stress is directly solved with transport equation. Finally a good result is achieved.

2. Meshing and Boundary Conditions Set

Grid quality is one of the most important factors which affect the numerical precision and work efficiency in numerical calculation. Considering the complexity of the thruster structure and the advantages of structured and unstructured grids, multi-block hybrid meshing method is presented.

The ducted propeller is placed in a cylindrical flow field, as shown in Figure 1, the diameter of the column is 5D, the distance between the fluid entrance and front of the duct is 4D, the distance between the fluid outlet and back of the duct is 6D, the axis of the flow field coincides with the axis of the duct. The flow region of the thrust is divided into four parts. Unstructured meshes are used in the complex area adjacent to the propeller-area 1, and local crowded meshes are used near the propeller blade and hub position, and structured meshes are used in the area 2, area 3 and area 4; the grid density in area 2 is a little bigger than that in area 3 and area 4.

The grids on the surface of the propeller and the hub is generated with type of map and elements of quad, afterwards, the grids inside the duct is generated with type of TGrid and elements of Tet/Hybrid, which is shown in Figure 2. The mesh in area 2 area 3 and area 4 is generated with cooper and Hex/Wedge, which is shown in Figure 3.

Among them, TGrid and Tet/Hybrid means that the volume is divided mainly by tetrahedral cell, Hex/Wedge means that the mesh generated is hexahedral mesh, and some of them is wedge mesh, cooper means that the volume is divided according to the appointed source face.

The unstructured grid has good adaptability, reduced the difficulty in the mesh generation around the propeller, and the structured grid has good quality. The grid division method mentioned above not only reduces the grid number and improves the quality of mesh, but also improves the efficiency of the subsequent simulation.

In general, the flow region in the boundary is almost uniform mixture in numerical calculation. For the numerical calculation only need to obtain the time averaged data of the interaction between the propeller and the
catheter, so the Moving Reference Frame (MRF) model is selected. And the flow field is divided into the internal catheter flow area and the external one, the interior area is defined as a rotation domain, the external one is defined as static domain. Inlet boundary is set as velocity inlet, the magnitude is constant and the direction is perpendicular to the entrance. Outlet boundary is set as pressure-outlet; the gauge pressure is given as 0. Interfaces between the rotation domain and the static domain are set as interface. The propeller and the duct are set as solid wall with no slip conditions. Considering that the RSM is effective under fully developed turbulent condition, turbulence around the near wall region is not stable, the non-equilibrium wall function is adopted.

3. Selection of RSM Model and Open Water Performance of the Ducted Propeller

In order to use the experimental data of the JD7704 catheter + Ka4-55 propeller provided by Shanghai Jiao Tong University to verify the correct of our method and model, a matched propeller is designed. The structure is as shown in Figure 4 and its dimension in Table 1.

In the rotation of the propeller, the flow around the propeller is considered to be strong rotational flow, thus the turbulent flow is anisotropic. RSM considered the convection and diffusion of the Reynolds stress, and used the transport equation to solve the stress, avoided the viscosity hypothesis. RSM is a transport equation to solve the Reynolds stress tensor [5], the equation is:

$$\frac{\partial}{\partial t} \left( \rho u_i \right) + \frac{\partial}{\partial x_j} \left( \rho U_i u_j \right) = -\frac{\partial}{\partial x_k} \left[ \rho u_i u_j + p \left( \delta_{ij} u_i + \delta_{ij} u_j \right) \right]$$

$$+ \frac{\partial}{\partial x_k} \left( \mu \frac{\partial U_i}{\partial x_k} \right) - \rho \left( \frac{\partial U_i}{\partial x_j} + \frac{\partial U_j}{\partial x_i} \right) - \rho \beta \left( g_{ij} \frac{\partial u}{\partial x} + g_{ij} \frac{\partial u}{\partial x} \right)$$

$$+ \rho \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) - 2 \mu \frac{\partial u_i}{\partial x_j} \frac{\partial u_j}{\partial x_i} - 2 \rho \beta \left( u_i u_j \varepsilon_{ik} + u_i u_j \varepsilon_{jk} \right)$$

(1)

To simulate the effect of the wall to the distribution of Reynolds stress, the SSG model is chosen, which import the quadratic component of Reynolds stress anisotropic tensor to pressure and strain term. Thus the pressure and strain term is:
To study the mesh dependency of the calculation, the open water performance of the ducted propeller under 200 thousands, 300 thousands, 500 thousands grids are calculated with RSM used. Through the simulation, the propeller thrust $T_p$, duct thrust $T_n$ and the total torque $Q$ under different advance coefficient is achieved, and the total thrust coefficient $K_T$, the duct thrust coefficient $K_{TN}$, the torque coefficient $K_Q$ and the open-water efficiency $\eta_0$ is calculated. Among them, the advance coefficient $J = \frac{V_n}{nD}$, the total thrust coefficient $K_T = T/\rho n^2 D^4$, the duct thrust coefficient $K_{TN} = T_n/\rho n^2 D^4$, the torque coefficient $K_Q = Q/\rho n^2 D^5$, the open-water efficiency $\eta_0 = \frac{K_T}{K_Q \pi}$. In the equation, $\rho$ means the fluid density; $T$ means the total force generated by the ducted propeller.

The comparison of results under different grids is shown as Figure 5; we can see that the result with higher grid density is closer to the experimental result, but the results are stable in general. Considering the calculation efficiency and computational accuracy, the 300 thousands grid is chosen for later calculations.

In the calculation, the advance coefficient is defined from 0.1 to 0.8, the interval is 0.1. The simulation data and the error of the data are shown in Table 2. From the table, we can learn that the maximum error of torque coefficient $K_Q$ is 1.46%, the maximum error of duct thrust coefficient $K_{TN}$ is 4.01%, the maximum error of the total thrust coefficient $K_T$ is 2.98%, and the maximum error of the open water efficiency $\eta_0$ is 0.89%. The conformity between numerical calculation and experimental data is very good, so we can conclude that the method proposed is feasible.

### Table 1. Geometry parameters of the propeller.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Diameter(m)</th>
<th>Pitch ratio $P/D$</th>
<th>Disc ratio $A_s/A$</th>
<th>Hub diameter ratio $d_1/D$</th>
<th>Number of blades</th>
<th>Clearance between the blade and duct (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Value</td>
<td>0.06</td>
<td>1.03</td>
<td>0.55</td>
<td>0.2</td>
<td>4</td>
<td>2</td>
</tr>
</tbody>
</table>

\[
\phi_q = -C_1 e a_q + C_2 e \left( a_u a_q - \frac{1}{3} a_u a_u \delta_q \right) + C_3 k \left( S_q - \frac{1}{3} \{S\} \delta_q \right)
\]

\[
+ C_4 k \left( a_u S_{jk} - \frac{2}{3} a_u a_{jk} \delta_q \right) + C_5 k \left( a_u \omega_{jk} + a_{jk} \omega_a \right)
\]

(2)

4. Pressure Nephogram Analyses on the Surface of the Blades of the Propeller

Thrust and torque of the propeller are the two macroscopic stresses. If we want to study the force of the propelle-
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Figure 5. Grid dependency of the calculation.

Table 2. The simulation data and the error.

<table>
<thead>
<tr>
<th>$J$</th>
<th>$K_{TN}$ Simulation</th>
<th>$K_{TN}$ Error (%)</th>
<th>$K_T$ Simulation</th>
<th>$K_T$ Error (%)</th>
<th>$10^2K_0$ Simulation</th>
<th>$10^2K_0$ Error (%)</th>
<th>$\eta_0$ Simulation</th>
<th>$\eta_0$ Error (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.1</td>
<td>0.2286</td>
<td>0.69</td>
<td>0.5001</td>
<td>2.89</td>
<td>0.4576</td>
<td>0.47</td>
<td>0.1740</td>
<td>0.41</td>
</tr>
<tr>
<td>0.2</td>
<td>0.1785</td>
<td>1.96</td>
<td>0.4293</td>
<td>1.55</td>
<td>0.4443</td>
<td>0.96</td>
<td>0.3077</td>
<td>0.18</td>
</tr>
<tr>
<td>0.3</td>
<td>0.1349</td>
<td>3.01</td>
<td>0.3617</td>
<td>0.69</td>
<td>0.4137</td>
<td>0.11</td>
<td>0.4177</td>
<td>0.24</td>
</tr>
<tr>
<td>0.4</td>
<td>0.0962</td>
<td>3.67</td>
<td>0.3002</td>
<td>1.71</td>
<td>0.3747</td>
<td>-0.07</td>
<td>0.5104</td>
<td>0.89</td>
</tr>
<tr>
<td>0.5</td>
<td>0.0618</td>
<td>3.91</td>
<td>0.2351</td>
<td>2.11</td>
<td>0.3314</td>
<td>1.44</td>
<td>0.5647</td>
<td>0.37</td>
</tr>
<tr>
<td>0.6</td>
<td>0.0303</td>
<td>4.01</td>
<td>0.1688</td>
<td>2.98</td>
<td>0.2757</td>
<td>1.46</td>
<td>0.5849</td>
<td>0.86</td>
</tr>
<tr>
<td>0.7</td>
<td>0.0034</td>
<td>3.77</td>
<td>0.0958</td>
<td>0.26</td>
<td>0.2154</td>
<td>1.17</td>
<td>0.4959</td>
<td>-0.45</td>
</tr>
<tr>
<td>0.8</td>
<td>-0.0257</td>
<td>-9.94</td>
<td>0.0244</td>
<td>-0.56</td>
<td>0.1572</td>
<td>3.76</td>
<td>0.1979</td>
<td>-0.86</td>
</tr>
</tbody>
</table>

**5. Working Flow Analysis of the Propeller**

From Figure 6, we can learn that: 1) on the pressure surface, the pressure decreases gradually from the leading edge to the trailing edge, whereas the pressure increases gradually from root to tip. Because of the mutual interference between the catheter and blade, the leading edge of the blade and the blade tip appears pressure drop; 2) on the back surface, the suction decreases gradually from the leading edge to the trailing edge, and yet the suction increases gradually from root to tip, and reaches the maximum in the leaf tip. There are large differences between the catheter propeller blade and ordinary propeller in pressure distribution characteristics [6] [7].
Figure 6. Pressure distribution of the blade surface of the catheter propeller. (a) Pressure distribution of the blade surface; (b) Pressure distribution of the back surface of the blade.

Figure 7. The pressure distribution of the flow field.

site direction of the flow, which explains the working mechanism of ducted propeller.

Figure 8 shows the velocity vector of the ducted propeller at surface $x = 0$, we can see that the fluid velocity at both sides of the blade increases gradually from root to tip and a tip vortex forms at the blade tip.

6. Comparison of Computational Accuracy under Different Turbulent Models

At present, the two-equation models are also used to calculate swirling flow with high Reynolds number. To verify the advantage of RSM, the standard $k-\varepsilon$ model is used to simulate the open water performance of the ducted propeller. The open water performance calculated by RSM and standard $k-\varepsilon$ model is shown in Figure 9; we can see that RSM has better accuracy and RSM is more applicable to calculate the open water performance of the ducted propeller.
7. Conclusions

This paper proposes a new method—the combination of the multi-block hybrid mesh and RSM, then it is used to analyze the flow field of ducted propeller, including the numerical calculation on the open water performance; finally, we draw conclusions:

1) Compared with the experimental data of JD7704 catheter + Ka4-55 propeller, the calculation results based on this method are in good agreement with experimental results in the thrust coefficient, torque coefficient and open water efficiency, so the method proposed in this paper is effective and feasible.

2) The flow field distribution characteristics of the ducted propeller are analyzed in this paper; the catheter can adjust the pressure distribution on the blade surface, which reduces the pressure difference in the blade tip, but cannot completely eliminate the tip vortex.

3) In the calculation of open water performance of ducted propeller, RSM has better accuracy than standard k-ε model; the method proposed provides reference for simulation of viscous flow around the complex rotating machine.

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References


