Numerical Modeling of Electromagnetic Scattering from Sea Surface Covered by Oil

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ABSTRACT

The aim of this work is to study the impacts of the oil spills on the electromagnetic scattering of the ocean surfaces in bistatic and monostatic configurations. Therefore, in this paper, we will study the influence of the pollutants (oil spills) on the physical and geometrical properties of sea surface. In recent literature, the study of the electromagnetic scattering from contaminated sea surface (sea surface covered by oil spill) was limited in monostatic case. In this paper, we will study this effect in bistatic configuration, which is interested in presence of pollution in sea surface. Indeed, we will start the numerical analysis of the bistatic scattering coefficients of a clean sea surface. Then, we will study the electromagnetic signature from sea surface covered by oil spills in bistatic case using the numerical Forward-Backward Method (FBM). The obtained numerical simulation of bistatic scattering coefficients of clean and contaminated sea surface is studied as a function of various parameters (frequency, incident angle, sea state, type of pollutant…). And the obtained results are also compared with those published in the literature, including those using asymptotic methods.

KEYWORDS

Sea Surface; Oil Spills; Forward-Backward Method; Asymptotic Methods; Electromagnetic Scattering Coefficients; Bistatic Configuration

1. Introduction

In the maritime environment, the presence of objects, ship wake and pollutants changes the physical and geometrical properties of sea surface. In this paper, a spatial focus is given to analyze the electromagnetic signature of pollutants such as organic films, petrol and oil slicks. To date, many systems have been developed such as SAR (Synthetic Aperture Radar) to detect the presence of the oil spill on the sea surface (Figure 1). To improve the performance of existing systems, it becomes very important to analyze in greater detail the information contained in the electromagnetic field scattered by the sea surface [1-3]. In this context, modeling the interaction of electromagnetic waves with polluted seas or not takes all its importance. In particular, the estimation of the electromagnetic scattering based on geometric (roughness) and physical (dielectric properties of sea water with or without pollutant) properties of the ocean surface is an essential tool in the design of detection systems, in particular for pollutant [4].

In recent years, many research works have focused on modelling the electromagnetic scattering from ocean surface. Indeed, on one hand, different models based on the geometric description of the sea surface (Elfouhaily spectrum and Pierson-Moskowitz spectrum) [5,6] and on the other hand, different electromagnetic models have been developed for studying the electromagnetic scattering from sea surface. The existing electromagnetic models are classified into: approximate methods like the Kirchhoff Approximation (KA), Small Perturbation Method (SPM), Two Scale Model (TSM), Small Slope Approximation (SSA) [7-9] and exact methods such as the finite difference time domain (FDTD) [10], Finite Element Method (FEM) [11], Method of Moment (MoM) [12], Forward-Backward Method (FBM), Forward-
Backward Method with Spectral Accelerate Algorithm (FBM/SAA) [13-17].

In our study, the numerical FBM method is used to calculate the bistatic scattering coefficients from a clean and a polluted sea surface. Recently in [4], the study of the electromagnetic scattering from ocean surface covered by oil spills was performed in monostatic case by using the numerical method of moment and Monte-Carlo simulation. The contribution of this paper is the study of this effect in bistatic case (Forward propagation configuration), which is interested in presence of pollution in sea surface. We will start the numerical simulation of the oil spills effect on the sea surface. Then, we represent our numerical results of the bistatic scattering coefficients from a clean and polluted sea surface by using the numerical Forward-Backward method.

This paper is organized as follows: in the first part, we present the impact of the oil spills on the surface height spectrum of a rough sea surface. To characterize the clean sea surface, the model of Elfouhaily et al. [6] is used, and for the contaminated sea surface we use the Lombardini et al. model [18]. In the second part, we discuss the calculation method of electromagnetic scattering coefficients (FBM). In the last part, by using the FBM method, we present the numerical results of electromagnetic scattering coefficients obtained for non-polluted and polluted sea surface.

2. Formulations

2.1. Sea Surface Description

In our simulation, we use the Elfouhaily model for sea roughness spectrum [6]. This sea spectrum formulation is given in the form:

\[ S(k, \phi) = M(k) f(k, \phi) \]  

(1)

\( M(k) \) represents the isotropic part of the Elfouhaily spectrum modulated by the angular function \( f(k, \phi) \). \( k \) is the sea wave number and \( \phi \) is the wind direction. Figure 2 illustrates the omnidirectional spectrum and the angular function for different values of the wind speed.

In this section, we study the effect of the oil spills on the geometrical properties of the sea surface (ocean spectrum). We will focus on the oil from a layer up the sea surface (contaminated sea surface). Then we present its influence on the ocean spectrum using a damping model [18], and we compared the obtained results with the representation of clean sea surface spectrum.

According to Lombardini et al., the influence of the pollution is introduced in the form of an attenuation coefficient applied to the clean sea spectrum:

\[ S_{po} = \frac{S_{cl}}{y_s(f, E_0, \omega_o)} \]  

(2)

This damping effect is expressed by the attenuation coefficient explicitly given by the following equation:

\[ y_s(f, E_0, \omega_o) = \frac{1 \pm 2 \tau + 2 \tau^2 - X + Y(X + \tau)}{1 \pm 2 \tau + 2 \tau^2 - 2X + 2X^2} \]  

(3)

where

\[ X = \frac{E_0 K^2}{\rho 2 \omega_o^3} \quad Y = \frac{E_0 K}{4 \rho \nu \omega} \quad \tau = \left( \frac{\omega_o}{2 \omega} \right)^{1/2} \]  

(4)

A dimensional quantities and

\[ f = \frac{\omega}{2\pi} = \left( \frac{\sigma K^3}{\rho + g K} \right)^{1/2} \]  

(5)

The dispersion law, \( S_{cl} \) denotes the clean sea spectrum, \( S_{po} \) the polluted sea spectrum, \( \rho \) the sea water density, \( \nu \) the kinematic viscosity, \( \sigma \) the surface tension, \( g \) acceleration of gravity, \( K \) the wave number,
Figure 2. Elfouhaily spectrum with different values of the wind speed: (a) Omnidirectional spectrum (b) Angular function.

In this paper we will focus on one-dimensional rough sea surface covered by insoluble films. In this work, the presented simulations of electromagnetic scattering coefficients of clean and contaminated sea surface are mainly based on a Forward-Backward Method. The FBM method split the surface current into contributions; one is the forward component (the courant contribution due to the waves propagating forwards) and another is the backward component (the current contribution due to the waves propagating backwards). This method has been developed to calculate the scattering coefficients from dielectric rough surface [16]. Furthermore, to accelerate this method and to treat a large problem, the FBM method was combined with Spectral Accelerate Algorithm (FBM/SAA) [15,17].

The FBM method has been well-discussed in [13-17]. The surface electric and magnetic fields can be evaluated by solving the following pair of integral equations:

\[ E_x(t, x) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \frac{\epsilon_0 \omega}{2 \pi} \frac{\partial}{\partial y} \left( \frac{1}{r} \right) \, dy \, dz \]

\[ H_y(t, x) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \frac{\mu_0 \omega}{2 \pi} \frac{\partial}{\partial y} \left( \frac{1}{r} \right) \, dy \, dz \]

where \( E_x \) and \( H_y \) are the electric and magnetic field components, \( \epsilon_0 \) is the permittivity of free space, \( \mu_0 \) is the permeability of free space, \( \omega \) is the angular frequency, and \( \partial \) is the partial derivative.

In the next section we will present the numerical FBM method used to calculate the electromagnetic scattering coefficients of clean and polluted ocean surface.

2.2. Numerical Forward-Backward Method

Many approaches were developed to estimate the electromagnetic scattering from sea surface (The asymptotic models and the numerical exact methods). Each of asymptotic methods is an approximation and is based on particular conditions (SPM covers the small-scale roughness; KA is valid for a surface with wide-scale roughness). However, the numerical exact methods are valid for all scale of roughness and give more precise results. Among the exact methods, in our study the numerical FBM method is used to calculate the bistatic scattering coefficients from a clean and a polluted sea surface. It should be noted that the chosen method (FBM) in this paper has already been applied, in particular to calculate the electromagnetic signature of a breaking wave, and the results obtained in this context were compared with measurements made in the anechoic chamber with profiles of breaking waves in aluminum [19,20].

In this paper we will focus on one-dimensional rough sea surface covered by of insoluble films (fully covered sea, \( F = 1 \)). Figure 4 shows the comparison between the height spectrum of clean sea surface and the polluted sea surface. The normalized height spectrum of contaminated sea surface (sea surface covered by oil film) is plotted for different parameters of oil film [18]. It was observed that the attenuation due to pollutant film is essentially located at the high frequencies, which corresponds to the capillary waves.

In the next section we will present the numerical FBM method used to calculate the electromagnetic scattering coefficients of clean and polluted ocean surface.
\[ E_{\text{inc}}(r) = \frac{1}{2} E(r) + \int_{S} j \omega \mu_{0} G_{0}(r,r') \hat{J}_{s}(r') dS' + E(r') \left[ \hat{n} \cdot \nabla G_{0}(r,r') \right] dS' \]

\[ 0 = \frac{1}{2} E_{i}(r) - \int_{S} j \omega \mu_{1} G_{1}(r,r') \hat{J}_{s}(r') dS' + E_{i}(r') \left[ \hat{n} \cdot \nabla G_{1}(r,r') \right] dS' \]  

Figure 3. Damping ratio for different fractional filling factors. 

Figure 4. Comparaison between a clean and oil spilled sea surface. 

where \( E_{\text{inc}} \) is the incident wave, \( J_{s} \) is the induced current in the surface, the fields \( E \) in the upper medium (free space) and \( E_{i} \) in the lower medium, \( \mu_{0} \) and \( \mu_{1} \) are respectively the permeability of the free space and the lower medium, \( \omega \) is the radian frequency, \( r \) and \( r' \) are the source and observation points respectively, \( \hat{n} \) the outgoing normal to the surface, \( G_{0}(r,r') \) and \( G_{1}(r,r') \) are respectively, the two dimensional Green function in the free space and in the lower medium.

The integral Equation (7) are discrete under a matrix…
form (8) by using rectangular pulse basis functions and the point matching technique:

\[ Z \cdot I = V \]  

where \( Z \) is the impedence matrix, \( V \) is the wave incidence and \( I \) is the induced current along the rough surface. In the FBM approach, the matrix of Equation (8) is decomposed as:

\[ I = I_f + I_b \]  
\[ Z = Z_f + Z_s + Z_h \]  

Equation (8) can be now decomposed into forward propagation and backward propagation of matrix equations, respectively as follows:

\[
\begin{align*}
Z \cdot I_f & = V - Z_f \cdot (I_f + I_b) \\
Z \cdot I_b & = -Z_s \cdot (I_f + I_b)
\end{align*}
\]

This system of equation can be solved iteratively; indeed the currents \( I_f^{(i)} \), \( I_b^{(i)} \) at the i-th iteration can be obtained as

\[
\begin{align*}
(Z_s + Z_f) \cdot I_f^{(i)} & = V - Z_f \cdot I_b^{(i-1)} \\
(Z_s + Z_b) \cdot I_b^{(i)} & = -Z_s \cdot I_f^{(i)}
\end{align*}
\]

The algorithm begins with \( I_b^{(0)} = 0 \).

After competition of the surface current, so that we can calculate the scattered field from the non-polluted and polluted sea surface. Using the Monte Carlo technique, we calculate the average of the bistatic scattering coefficients.

Finally, the algorithm of FBM method used in this paper is adapted to estimate the electromagnetic scattering coefficients from clean or polluted rough sea surface.

In the next part, first we study the electromagnetic scattering from non-polluted sea surface and we will present the outcomes of the pollutant film on the electromagnetic sea surface scattering.

### 3. Numerical Analysis of Bistatic Scattering Of Contaminated Rough Sea Surface by Using The Forward-Backward Method

Many works [21-23] show that the FBM method and the accelerated version FBM-SAA is interesting for maritime applications (ship target, electromagnetic scattering from braking wave). However, there are not research works, which analyze the oil spills effect on the electromagnetic signature of sea surface observed in bistatic configuration and by using the numerical FBM method. This is the object of this section.

In this section, we will focus on electromagnetic scattering coefficients of ocean surface covered by oil spills. First, we study the case of one-dimensional rough sea surface (clean sea surface without pollutants). By using the numerical FBM method, we realize the numerical simulation of the bistatic scattering coefficients (in forward propagation configuration) of clean rough sea surface, and we compare the numerical results with those obtained by using the asymptotic models such as small perturbation method (SPM) [7,24]. This step will allow to validate the results obtained by the developed model, and to have a reference on an ocean surface without oil spills.

#### 3.1. Comparison with Asymptotic Methods

In this part, by using the FBM method, we present numerical simulations of bistatic scattering coefficients (in forward propagation configuration) of clean rough sea surface, and we compare the numerical results with those obtained by using the asymptotic methods, especially with those given by the small perturbation method (SPM). In this simulation the sea surface is assumed to be dielectric rough surface. Figure 5 compares the results obtained using the numerical FBM method with those given by using SPM model in the forward propagation configuration. The parameters are fixed as follows: The electromagnetic wave frequency is 10 GHz (X band), the relative dielectric constant of sea is \((55.5 + i38)\), the incident angle is fixed to \(\theta_i = 60^\circ\), and the wind speed \(U_{10} = 5\) m/s.

Using the Monte-Carlo technique, we calculate the average of the bistatic scattering coefficients (60 realizations).

We compared the results obtained by FBM with those given by SPM method; we can notice that the results obtained by using the numerical FBM method are in good agreements with those given by the asymptotic approach SPM. It should be noted that the SPM method is accurate for the rough sea surfaces with the small roughness conditions (valid for a slightly rough sea surface). In our future works we will compared the numerical FBM method with other asymptotic models such as (TSM, SSA, WCA...) which have a wider application domain than the SPM method.

#### 3.2. Bistatic Scattering Coefficients of Sea Surface Contaminated by Oil

To analyze the influence of the oil pollutants on the electromagnetic signature from sea surface, we represented the variation of the bistatic scattering coefficients (in forward propagation configuration) under different conditions of sea state, frequencies, type of pollutant, and incidence angles. Figure 6 gives the bistatic scattering coefficients for both clean and polluted surface by using the FBM method. The sea surface is described by using the Elfouhaily spectrum, the wind speed \(U_{10} = 5\) m/s, the
sea temperature and salinity are respectively $T = 20\, ^\circ C$ and $S = 35$ ppt the frequency is $3$ GHz ($S$ band), the incident angle is fixed to $\theta_0 = 0^\circ$, HH polarizations, and the scattering angle in vary from $-90^\circ$ to $90^\circ$. The pollutant is considered insoluble film and its relative dielectric constant is $(2.25 + i0.01)$ [22], and the relative dielectric constant of the sea water is equal to $(70.5 + i40)$ [21].

Figures 7-9 show the bistatic scattering coefficients of the clean and the contaminated rough sea surface obtained for incidence angle equal to $40^\circ$, $70^\circ$ and $80^\circ$ respectively. The other parameters are the same as those given in Figure 6.

From Figures 6-9 it may be noted the differences between the scattering coefficients of the clean and the polluted sea surface. Indeed, for the incidence angle equal to $0^\circ$ (Figure 6) the differences exist for both negative and positive scatterings angles, whereas for the incidence angles $40^\circ$, $70^\circ$ and $80^\circ$ (Figures 7-9) the differences appear at negative scattering angles, more precisely in the range $[-90^\circ, \theta_s]$. The deviation between the scattering coefficients is essentially due to both the influence of pollutant in surface height spectrum and relative dielectric constant of the pollutant.

In order to obtain more information about the deviation between the scattering coefficients of oil spilled sea surface and the non polluted surface, we present in Figures 10 and 11 another comparison at Ku band (frequency is $14$ GHz).

In Figures 10 and 11 the electromagnetic wave frequency is $14$ GHz (Ku band), the dielectric constant of
Figure 7. Bistatic scattering coefficients of clean and contaminated sea surface: frequency (3 GHz) and incidence angle (40°).

Figure 8. Bistatic scattering coefficients of clean and contaminated sea surface: frequency (3 GHz) and incidence angle (70°).

Figure 9. Bistatic scattering coefficients of clean and contaminated sea surface: frequency (3 GHz) and incidence angle (80°).
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Figure 10. Bistatic scattering coefficients from clean and contaminated sea surface: frequency (14 GHz) and incidence angle (40°).

Figure 11. Bistatic scattering coefficients from clean and contaminated sea surface: frequency (14 GHz) and incidence angle (50°).

sea surface is $(45.75 + i39)$, the incident angle is equal to 40° in Figure 10 and to 50° in Figure 11 and the other parameter are the same as in Figure 6.

By comparing Figures 7 and 10, we notice that for Ku band (frequency is fixed to 14 GHz) the difference between the electromagnetic scattering coefficients of the clean and polluted sea surface is greater than S band (frequency 3 GHz). From these analyses, we can conclude the influence of the oil spills on the electromagnetic signature of ocean surface is more important at a higher frequency.

In our study, the numerical simulations of electromagnetic scattering coefficients from both clean and polluted sea surface are limited to the problem of one dimensional surface (1D) and only the cross-polarization scattering coefficients can be evaluated by using the numerical FBM method. The main purpose of our future works is to evaluate the co-polarization and cross-polarization scattering by tow-dimensional rough sea surface (clean and oil-spilled sea surface) in bistatic configuration.

4. Conclusions

In this paper, by using the numerical FBM method, the EM scattering by clean and polluted rough sea surface observed in bistatic case (forward propagation configuration) is investigated. For clean rough sea surface, the numerical results obtained by using FBM were compared
with those given by using the asymptotic methods (small perturbation method-SPM). The pollutant effect on sea surface spectrum and in the electromagnetic scattering coefficients was described and modeled for various conditions of sea surface, frequencies and incidence angles.

Comparing the scattering coefficients of the clean sea surface with those of polluted sea surface, it may be noted the differences between the scattering coefficients. These results demonstrate the influence of the pollution on the electromagnetic signature of the sea surface.

The objective of future work is to compare the performance of the FBM method with other asymptotic models such as (TSM, SSA, WCA…) which have a large validity domain than the small perturbation method (SPM). And we will study the electromagnetic scattering from other geometric configurations of observation and other types of surface (including 2D dielectric rough sea surface).

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