Drug dispersion for single- and multi-lumen catheters

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ABSTRACT
This study presents a comparison of the drug dispersion capability of various catheters which can be used to inject medication or stem cells into the arterial system. The study was carried out by the use of numerical simulation so that various geometric and physical operating parameters could be investigated. The blood was modeled with a power-law viscosity and the medication had two levels of viscosity to represent upper and lower bounds expected in practice. Two different medication flowrates were also incorporated into the study. Finally, the impact of an inflated balloon upstream of the injection was studied. The artery was simply modeled as a straight circular tube with the catheters concentrically positioned. It was found that in some cases, dispersion was improved by use of a multi-lumen device, particularly when an upstream balloon was employed to regulate blood flow and drug residence time. In other cases, the dispersion from the single-lumen device was superior. Another finding was that the multi-lumen device had a reduced hydraulic resistance to blood flow, compared to the single-lumen device when an upstream balloon was inflated.

Keywords: Catheter Injection; Catheter Hemodynamics; Intracoronary Injections; Stem Cell Treatment of Infarction; Heart Disease; ND Infusion Catheter

1. INTRODUCTION
Numerous medical situations call for direct injection or infusion of medication or other fluids that can be used for patient treatment. Some examples include the intracoronary injection of Adenosine or Nitroglycerin for transient occlusions or spasm or the infusion of stem cells for regenerative therapy following myocardial infarction (MI). For any case of intravascular infusion, it is important to characterize the distribution of the injectant across the cross section of the artery. Well-distributed injectant is more capable of contacting the artery lumen and entering into the tissue for therapy. As an example of this area of active investigation, comparisons of direct injection and intracoronary injections of stem cells are well represented in the literature, for instance [1-9]. Some of these studies compared various injection methods [4,6,8]; others were overviews of the emerging technology of stem cell use for treating MI (for instance [2,3]); while others compared the impact of injection on the hemodynamics of the neighboring arteries in bench-top tests (but not on distribution of medication or cells within the artery) [9].

Figure 1 has been prepared to describe the qualitative difference between a rapid and slowly dispersing injectant. In the upper part of the figure, the injectant, shown in grey, is seen to rapidly spread across the artery cross section. In the second part of the figure, the injectant is confined to a small central region that transits a significant distance in the artery before dispersion. The figure is intended to be illustrative rather than quantitative.

2. NUMERICAL MODELING
The numerical model was laminar, justified by the low-
Reynolds numbers in the system. Blood velocities were based on a cardiac-cycle average flowrate. The equations of motion are listed below.

Conservation of mass of species \( k \):
\[
\rho \frac{\partial C_i}{\partial t} + \rho u_i \frac{\partial C_i}{\partial x_i} = D \frac{\partial^2 C_i}{\partial x_i^2}
\]

Conservation of momentum:
\[
\rho \frac{\partial u_j}{\partial t} + \rho u_i \frac{\partial u_j}{\partial x_i} = -\frac{\partial p}{\partial x_j} + \mu \frac{\partial^2 u_j}{\partial x_i^2} \quad j = 1, 2, 3
\]

In these expressions, \( k \) designates the species, \( j \) indicates Cartesian direction, and \( i \) is a tensor variable. The term \( D \) is the diffusivity of the binary fluid mixture. All equations are expressed in transient form to reflect the solution strategy of the software (CFX Version 14.0) that was used to complete the calculations; the ultimate solutions are steady state, a situation which is achieved when the flow field is no longer changing in time.

The artery is straight with a diameter of 3.5 mm for all cases. A total of 16 cases were simulated, as listed in Table 1. The fluid densities were 1060 and 1000 kg/m³, respectively, for the medication and blood.

As seen from the table, a number of key parameters are investigated. The first is the single/multiple lumen injection catheter. Next, is the presence of a balloon upstream of the injection location which partially blocks the artery passageway. The third issue listed in the table is the inlet condition for the blood. For no balloon cases, the inlet condition is a pre-specified blood flowrate (60 cc/min) coronary artery blood flow of the anterior descending artery, which leads to an average blood velocity of 0.1039 m/s. For the cases with upstream balloons, the flowrate was not known apriori so an inlet pressure was applied that matched the inlet pressure for the no-balloon case. In this regard, an equivalent overall pressure drop was enforced.

The fourth item is the viscosity of the injectant which takes on high and low values that are expected to be upper and lower bounds on the actual medication viscosity used in the therapy. Finally, the medication flowrates are listed.

Blood was modeled as a non-Newtonian fluid with an Ostwald-de Waele constitutive model [10] that is
\[
\tau = K \gamma^n
\]

Here, \( K = 0.0147 \) (kg/m-s\(^{1.22}\)) and \( n = 0.78 \) [11]. The blood model is similar to that described in [12].

### Simulated Geometry

To facilitate the discussion of the modeling effort, attention is next turned to the geometric details. Figure 2 has been prepared to provide some dimensional detail. The figure shows a single-lumen catheter positioned in an artery. The figure is illustrative, in reality, the catheter is circular as is the artery. The image can be interpreted as a cut-view along the bisecting symmetry plane. The figure contains annotations which show key features, including the location of blood and medication inlets. The diameter of the artery is 3.5 mm and the length of the model is 11 cm so it was necessary to use cut lines to indicate the length of the model. The solution domain extends 3 cm upstream of the location where the medication exits the catheter and enters the bloodstream. The rationale for this was that such an extension allows natural development of the flow prior to the injection location.

<table>
<thead>
<tr>
<th>No</th>
<th>Lumens</th>
<th>Balloon</th>
<th>Inlet Cond.</th>
<th>Visc. (mPa*s)</th>
<th>Medic. Flow (ml/min)</th>
</tr>
</thead>
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<tr>
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<td>5</td>
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<td>4.7</td>
<td>5</td>
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<tr>
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<td>5</td>
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<tr>
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<tr>
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<tr>
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<td>10</td>
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<tr>
<td>9</td>
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<td>1.4</td>
<td>5</td>
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<tr>
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<tr>
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</table>
For the case with an inflated balloon, the bounding dimensions are maintained however a balloon is positioned upstream of the injection location. The balloon is symmetrically arranged around the catheter, as seen in Figure 3.

A multi-lumen catheter was modeled after the ND Infusion Catheter (Translational Research Institute, Gilbert, AZ). Instead of a single port for medication to enter the bloodstream, as commonly found in a single-lumen catheter, the ND Infusion Catheter has six ports. The injection plane of the catheter is shown in Figure 4. There, the injection ports can be seen near the periphery of the cross section.

Upstream of this injection plane, the multi-lumen catheter has a complex fluid flow pathway with multiple mixing regions and collection chambers. Figure 5 has been prepared to show the medication passageway in an oblique view. As with the single lumen case, the solution domain is extended upstream from the injection plane so that flow development can occur naturally.

From the figures, it is seen that the multi-lumen simulation encompasses a far more complex flow geometry than that of the single-lumen device. For instance, a single channel empties into a mixing chamber which then serves as a manifold for the six multiple injection lumens.

### 3. COMPUTATIONAL MESH

The completion of the simulation requires subdivision of the fluid space into regularly shaped computational elements. The quality and deployment of the computational elements are crucial for a successful and accurate solution. Inasmuch as the flow in this problem is deeply laminar, it is not necessary to expend extra elements in the near wall region to refine the boundary layer. On the other hand, experience suggests that such near-wall elements will aid in the predictions of flow separation. Consequently, the mesh shown in Figure 6 was used for the single-lumen case. The figure shows a series of magnifications which reveal the details of the mesh. It is seen that very near the wall, there are thin layers of elements which were described in the preceding text. Those thin elements follow the contour of the lumen and balloon, as evident in the lower part of the figure.

Similarly, the multi-lumen geometry was subdivided into elements and that deployment is displayed in Figure 7. As with Figure 6, this image shows a succession of increasing magnifications that allows identification of areas of fine mesh deployment.
4. RESULTS AND DISCUSSION

The primary results of interest are the distributions of the medication across the cross section of the artery. To help visualize the concentration results, Figure 8 has been prepared. This figure shows two instances after the medication injectant has emerged from the catheter. The top portion shows the medication shortly after emergence and the bottom shows the injectant at a later time. The bolus shown in the image is defined as the space which has medication concentrations greater than some arbitrarily selected threshold (1%, 10%, etc.) by volume. Areas outside the bolus have lower than the threshold concentration. The metric which will be used to characterize the performance of the devices is the percentage of a downstream cross section area that is occupied by volumetric concentrations that are greater than 1% or 10%. With the illustration of Figure 8 for context, attention will now be turned to quantification of the concentrations.

The following results will be focused on the region distal to the injectant port, within approximately 25 mm of that location. It is important to recall that the results to be presented here correspond to steady state conditions after the bolus has reached the outlet and results are no longer changing in time.

4.1. Single-Lumen Concentration Results

A global view of the injectant dispersion is provided by Figure 9. That figure, which corresponds to Case 1, is provided as a typical dispersion pattern. The top contour image shows the injectant along the entire length of the solution domain. The (b) and (c) parts are focused on the region near the injectant location. The (b) part is color coded to the legend on the left whereas (c) has two color regions which reflect zones that have <1% and >1% medication concentration. The last part of the figure, (d), shows the 1% region at the exit of the domain. It is seen that the injectant occupies the center of the artery.
Another feature of the flow is that the medication is constrained in the center portion of the artery by the blood flow which insulates it from the artery wall. The blood serves as a buffer against penetration to the wall. Much of the spreading occurs in the very near proximity to the injection ports; further downstream, the dispersion is gradual.

4.1.1. Impact of Kinematic Diffusivity Values

The first set of quantitative results shows the insensitivity of the results to the value of the kinematic diffusivity. Four variants of Case 1 were completed with values of kinematic diffusivity that were 0, $10^{-12}$, $10^{-9}$, and $2\times10^{-9}$ m$^2$/s. These values represent a range of diffusivity values that might be encountered with two liquid species. It was found that the results are virtually identical, as displayed in Figure 10. In fact, aside from the largest diffusion case, the results are indistinguishable. This finding confirms our expectations that the dispersion is primarily driven by advection rather than diffusion processes. As a consequence, the remaining results will all be presented for kinematic diffusivity values of 0 m$^2$/s without loss of generality.

4.1.2. Effects of Viscosity, Medication Flowrate, and Balloon

The next presentation will be for the distribution of injectant from the single-lumen catheter. The metric for evaluating performance will be the percent of downstream area that is occupied by fluid that is more than 1% injectant and more than 10% injectant by volume. The first image, Figure 11, shows the single-lumen situation, with no upstream balloon. Two sets of results are shown which correspond to Cases 1 and 3. It is quickly seen that the viscosity of the medication has very little impact on the dispersion rate of the medication. The results in the figure are representative of other comparisons that show insensitivity of viscosity.

While the medication viscosity is seen to have a small impact, the presence of the balloon is more apparent. Figure 12 shows the development of medication in the streamwise direction for Cases 3 and 4 which differ only by the presence of the balloon. For both the 1% and 10%...
regions, the presence of the balloon reduces the cross sectional coverage.

The last comparison to be made for the single-lumen case is for the injectant flowrate. For this comparison, Figure 13 has been prepared which shows that there is an impact on the dispersion by a doubling of the injectant flow. In the region very near the injectant port, the lower flowrate (Case 3) spreads slightly faster than the higher flowrate case (Case 7). On the other hand, further downstream, the situation reverses and the higher medication flowrate spreads significantly faster. Since there is more medication entering the stream, it is clear why the larger medication flowrate spreads faster. The very slight reduction in spreading near the injectant port is likely due to the stronger jet coherence as the medication emerges into the co-flowing blood stream. Nevertheless, the differences in this region are very small. Similar findings would be seen if other cases were compared, Cases 3 and 7 are representative samples.

4.2. Multi-Lumen Results

Medication that emerges from the multi-port injection lumen has a distinct dispersion pattern that is best illustrated qualitatively. Figure 14 has been prepared which shows an isosurface that demarks the surface on which medication concentrations of 10% exist. It can be seen that the medication emerges from the injection ports off-center and predisposed to the artery wall, compared to the symmetric emergence of medication from the single-lumen case.

More quantitative information is available by plotting the axial evolution of the dispersion of medication, in particular, counterparts of Figures 12 and 13. To this end, Figures 15 and 16 have been prepared. The first of the figures shows the effect of the balloon on medication dispersion. In contrast to the single-lumen case, it is seen that the presence of the balloon actually increases the...
dispersion of the medication slightly. This is believed to be due to the fact that the multiple injection ports are located near the periphery of the catheter where flow disturbances from the upstream balloon promote mixing of the two fluids.

With respect to the effect of mass flowrate, it is seen that the larger medication flowrates result in significantly more widespread dispersion of the medication across the artery cross section, as displayed in Figure 16. In fact, the impact of the larger medication flowrate for the multi-lumen geometry is very similar to that of the single-lumen case which was displayed in Figure 13.

The last issue to be addressed is the dispersion rates between the two geometries. It is seen that for some cases, the single-lumen device results in faster dispersion while in other cases, the situation reverses. In particular, it is interesting to compare the dispersion rates of the two devices in the presence of the upstream balloon. This situation is particularly relevant because the balloon impacted the two devices differently. Axial dispersion results are shown in Figure 17.

While this dispersion advantage of the multi-lumen device is not universal, in some situations the single-lumen dispersion rate is faster, it suggests that for injection of therapeutic cells into arteries in the presence of balloons, enhancement is achieved with multiple lumens.

It also should be noted that while the axial patterns of medication dispersion are similar, the cross sectional distributions differ. As exhibited in Figures 9 and 14, the distribution from the multi-lumen geometry lies closer to the artery wall and thereby enhances blood-artery wall mass transfer. This enhancement is important for mass transfer into arterial tissue [13-20].

Another enhancement with the multi-lumen device is that the hydraulic resistance for blood flow is reduced. In the presence of an inflated balloon, the flow resistance was notably smaller than that for the single lumen device.

The differences were in the 8% - 12% range over the length of the flow region, as depicted in Figure 2.

It is also clear that further improvements of dispersion could be achieved by spreading the positions of the multi-lumen ports at the injection plane, or by creating some radial flow direction at the port location. Not only would such an arrangement increase dispersion, but it would result in medication being projected toward the arterial wall.

5. CONCLUDING REMARKS

A detailed numerical study of the dispersion processes associated with injection lumina was performed. To the best knowledge of the authors, this is the first study of its kind. The study encompassed single-lumen and multi-lumen catheters and modeled a binary fluid mixture (blood and medication). The simulation incorporated a range of medication viscosities, flowrates, catheter geometries, and the presence or absence of an upstream balloon. It was found that viscosity had little impact on the dispersion, however, the presence of a balloon reduced dispersion for the single-lumen device and increased dispersion for the multi-lumen device.

For both devices, increased medication flowrates improved the spread of medication throughout the artery cross section. Further, it was found that in some instances, the multi-lumen device led to increased dispersion of medication and in other instances, the performance was reversed. Finally, the multi-lumen device was found to reduce hydraulic resistance to blood flow by approximately 8% - 12% when an upstream balloon was employed.

It is expected that further dispersion could be achieved by the utilization of a radial velocity component at the injection ports.
6. ACKNOWLEDGEMENTS

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REFERENCES


