Hierarchical Coordinated Control for Power System Voltage Using Linear Temporal Logic

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Abstract

The paper proposed an approach to study the power system voltage coordinated control using Linear Temporal Logic (LTL). First, the hybrid Automata model for power system voltage control was given, and a hierarchical coordinated voltage control framework was described in detail. In the hierarchical control structure, the high layer is the coordinated layer for global voltage control, and the low layer is the power system controlled. Then, the paper introduced the LTL language, its specification formula and basic method for control. In the high layer, global voltage coordinated control specification was defined by LTL specification formula. In order to implement system voltage coordinated control, the LTL specification formula was transformed into hybrid Automata model by the proposed algorithms. The hybrid Automata in high layer could coordinate the different distributed voltage controller, and have constituted a closed loop global voltage control system satisfied the LTL specification formula. Finally, a simple example of power system voltage control include the OLTC controller, the switched capacitor controller and the under-voltage shedding load controller was given for simulating analysis and verification by the proposed approach for power system coordinated voltage control. The results of simulation showed that the proposed method in the paper is feasible.

Keywords: Power Systems Voltage Control, Linear Temporal Logic, Hierarchical Coordinated Control, Hybrid Automata

1. Introduction

Power systems voltage control involves many distributed continuous controllers such as the generator excitation controller and discrete controllers such as the OLTC, the capacitor banks switching and load shedding, so power system is a classical hybrid dynamic control system. At present, the common methods of power system voltage control are the optimal control method based on optimization theory [1-3], the VQC method [4,5] and the Multi-Agent control method [6-8]. Substation is the main node of power system voltage control, particularly most voltage controllers in substation present the discrete dynamic. How to coordinate these controllers that have different functions is crucial to power system voltage control. In order to ensure the voltage security control, it is necessary to prevent redundancy and disorderly action and regulation, moreover the disturbances exacerbated the power system operation should be avoided [9].

In the light of the hybrid characteristics of power system voltage control, a method using the Linear Temporal Logic (LTL) is proposed to study the coordinated control problem of the multiple discrete voltage controllers in substation [10-12]. The main ideas: A hierarchical method is adopted for voltage control. The upper layer is voltage coordinated controller and the lower layer is composed by the physics equipments and their local controllers. In the high layer, Linear Temporal Logic (LTL) is used to describe power system coordinated voltage control specification [13], and then the LTL specification formula is converted into hybrid automata [14]. The hybrid automata effectively imple-
ment the coordinated voltage control with multiple specifications and multiple controllers. The most important feature of this approach is that hybrid automata of the coordinated controller can be designed automatically though LTL specification formula. If the detailed LTL specification formula is given, the hybrid automata model can automatically be derived using the algorithms in [14]. In particular, for complex systems, this method greatly reduced the miscellaneous design and deductive inference of the complexity control logic. Moreover, it is easy to be extended to large-scale power system coordinated voltage control.

2. Hierarchical Control Structure of Power System

2.1. Hybrid Dynamic of Power System

Power system hybrid dynamics can be described by the following equations:

\[
\dot{x} = f(x,q,v,t), \quad s_j(x,q,v,t) \neq 0, \quad j = 1, \ldots, n \tag{1}
\]

\[
\varsigma(t') = \varphi(x,q,v,t), \quad s_j(x,q,v,t) = 0, \quad j = 1, \ldots, n \tag{2}
\]

\[
z = h(x,q,v,t) \tag{3}
\]

where Equation (1) describes the continuous dynamics of power system, which are differential equations.

When the system continuous dynamics trajectory passes through discontinuous plane \( S_j(\cdot) = 0 \), a discrete event will occur. That is to say, \( S_j(\cdot) = 0 \) is the condition of events occurred. Equation (2) describes the subsequence change of continuous state vector when events occurred. Equation (3) describes the output of hybrid power system.

In order to facilitate modeling and analysis, we express the mathematical description of the hybrid dynamics system by nine-tuple a hybrid automata model [16],

\[
\mathcal{H} = (X, Q, V, \text{inv}, f, \varphi, x, I, F) \tag{4}
\]

where \( X \subseteq \mathbb{R}^n \) is the continuous state space of the system, \( x(t) \in X \); \( Q \subseteq \mathbb{N}^m \) is the set of discrete state, \( q \in Q \); \( V \subseteq \mathbb{N}^l \) is the set of discrete event input, \( v(t) \in V \); \( l \subseteq X \times Q \) is the system initial state, \( (x(t_0), q(t_0)) \in l \); \( Z \subseteq X \times Q \) include \( p \) dimensions continuous state output \( z_s \) and \( r \) dimensions discrete state output \( z_q \), that is,

\[
z(t) = \begin{bmatrix} z_s \\ z_q \end{bmatrix} \in Z \subseteq \mathbb{R}^p \times \mathbb{N}^r \tag{5}
\]

and \( z(t) \) is produced by function \( h : \mathbb{X} \times \mathbb{Q} \times \mathbb{V} \times \mathbb{R} \rightarrow \mathbb{R}^p \times \mathbb{N}^r \).

The vector field \( f : \mathbb{Q} \times \mathbb{X} \times \mathbb{V} \times \mathbb{R} \rightarrow \mathbb{R}^n \) describes continuous dynamics, and \( \text{inv} : \mathbb{V} \rightarrow 2^q \) assigns an invariant set to each location \( q \), the continuous part of the state.

The function \( s_j : \mathbb{Q} \times \mathbb{Q} \times \mathbb{V} \times \mathbb{R} \rightarrow \mathbb{R} \), \( j = 1, \ldots, n \) describes the condition of events occurred. As long as the discontinuous plane function \( s_j(x, y, u, q,v,t) \neq 0 \) is satisfied, the system trajectory makes the continuous dynamic evolve according to Equation (1).

The function \( \varphi : \mathbb{Q} \times \mathbb{Q} \times \mathbb{V} \times \mathbb{R} \rightarrow \mathbb{X} \times \mathbb{Q} \) is the reset function, describes the change of continuous state vector after discrete events occurred, that is, subsequence state \( \varsigma(t') \).

\[
\varsigma(t') = \begin{bmatrix} x(t') \\ q(t') \end{bmatrix} \in \mathbb{X} \times \mathbb{Q} \subseteq \mathbb{R}^e \times \mathbb{N}^j \tag{6}
\]

Note that in the hybrid automata that we use in this paper all the reset maps are defined to be the identify function. We assume that the switching conditions and the location invariants are connected sets. Also we let \( H = \mathbb{X} \times \mathbb{Q} \) to denote the state space of hybrid automata \( H \).

The trajectory of the hybrid automata \( H \) consist of combinations of the continuous state and discrete transitions. A trajectory of \( H \) can start at a location \( q(1) \), then it evolves under the gradient of vector field whose values is constraint by the set \( f(q(\cdot)) \) while the state \( x(t) \) remain always within the invariant set \( inv(q(\cdot)) \). When continuous state of trajectory satisfies the switching conditions, the system instantaneously switches to the new location \( q(t) \). The new state of the system will be \( (q', x) \).

Formally, the semantics of hybrid automata are given in term of generalized transition systems. A generalized transition system is a tuple \( T = (H, H_0, \rightarrow) \), where \( H_0 \) is the set of initial condition and \( \rightarrow \) is a transition relation. We define a trajectory \( \eta : R_e \rightarrow \mathbb{X} \) of the transition system \( T \). The set of all trajectories \( \eta \) of \( T \) that start from a state in \( H_0 \) is the language \( L(T) \) of the generalized transition system \( T \).

2.2. Hierarchical Voltage Control Structure

From the hybrid dynamics above, we know that it needs complex logic analysis and effective coordination among the dispersed controllers to implement global voltage safety control for the power system with both continuous control input and discrete control input.

We adopted hierarchical method to research the voltage control problem, as shown in Fig.1. The upper layer is the voltage coordinated control model, and a global control specification in this layer is defined by the LTL formula to coordinate the action of multiple voltage controllers to ensure the global voltage control safety.
lower layer is local closed loop control system composed by the physics equipments and their continuous controllers or discrete controllers. Moreover, the coordinated controller in upper layer and the physics system in lower layer also consist of a global closed loop control system satisfied LTL specification formula.

For the power system hybrid voltage control, how to carry on logic analysis and coordination based on the system running status is the main content of this paper. The aim is mainly focused on:
- The control inputs should ensure the security and stability of the system voltage;
- The results of coordination control should ensure that the actions of the multiple discrete controllers are reasonable, and the number of action is minimum;
- Avoid aggravating the deterioration of the power system state due to disorder regulation of controllers.

3. Linear Temporal Logic and Controller Synthesis

3.1. Linear Temporal Logic

LTL is a mathematical language based on the set of propositions  \( \Pi = \{ \pi_0, \pi_1, \ldots, \pi_n \} \) and provides a succinct expression to describe the temporal and logic identity of dynamic control system. The denotation \( \llbracket \cdot \rrbracket : \Pi \rightarrow \mathbb{P}(\mathbb{R}^n) \) is a mapping function and represents a subset of \( \mathbb{R}^n \). For any \( \pi \in \Pi \), it is \( \llbracket \pi \rrbracket \subseteq \mathbb{R}^n \). \( \mathbb{P}(\Gamma) \) denotes the power set of a set \( \Gamma \).

LTL includes traditional logic operators, such as conjunction (\( \land \)), disjunction (\( \lor \)) and negation (\( \lnot \)), and temporal operators such as eventually (\( \Diamond \)), always (\( \square \)) and until (\( \mathcal{U} \)). For \( \pi \in \Pi \), the set \( \Phi_\pi \) of all well formed LTL over \( \Pi \) is constructed using the grammar.

\[
\phi := \pi | \lnot \pi | \phi \lor \phi | \phi \land \phi | \phi \mathcal{U} \psi
\]

Let \( y(t) \) be a function from \( \mathbb{R}_+ \) to \( \mathbb{R}^n \) and \( \Pi \) be the set of atoms. For \( t, s \in \mathbb{R}_+ \), the semantics of any formula \( \phi \in \Phi_\Pi \) can be recursively defined as

- \( (y, \llbracket \cdot \rrbracket) = \pi \), iff \( y(0) \in \llbracket \pi \rrbracket \).
- \( (y, \llbracket \cdot \rrbracket) = \lnot \pi \), iff \( y(0) \notin \llbracket \pi \rrbracket \).
- \( (y, \llbracket \cdot \rrbracket) = \phi \lor \psi \), if \( (y, \llbracket \cdot \rrbracket) = \phi \) or \( (y, \llbracket \cdot \rrbracket) = \psi \).
- \( (y, \llbracket \cdot \rrbracket) = \phi \land \psi \), if \( (y, \llbracket \cdot \rrbracket) = \phi \) and \( (y, \llbracket \cdot \rrbracket) = \psi \).
- \( (y, \llbracket \cdot \rrbracket) = \phi \mathcal{U} \psi \), if there exists \( t \geq 0 \) such that \( (y, \llbracket \cdot \rrbracket) = \psi \) and for all \( s \) such that \( 0 \leq s \leq t \) we have \( (y, \llbracket \cdot \rrbracket) = \phi \).

Note that the path formula \( \phi \mathcal{U} \psi \) intuitively expresses the property that over the trajectory \( y(t) \), \( \phi \) is true until \( \psi \) becomes true. Here the semantics of until requires that \( \phi \) holds when \( \psi \) becomes true. The formula \( \Diamond \phi \) indicates that over the trajectory \( y(t) \) the subformula \( \phi \) becomes eventually true, that is, it describes the reachability properties for control problems, whereas the formula \( \Box \pi \) or \( \Box \lnot \pi \) denotes that \( \phi \) is always true over \( y(t) \), and it describes the safety properties for control problems.

Beyond the usual properties, LTL can capture sequences of events and certain infinite behaviors. For example,

- Coverage: The formula \( \phi = \Diamond \pi_1 \land \Diamond \pi_2 \land \cdots \land \Diamond \pi_n \) reads as the system will eventually reach \( \llbracket \pi_1 \rrbracket \) and eventually \( \llbracket \pi_2 \rrbracket \) and ... eventually \( \llbracket \pi_n \rrbracket \), requiring the system to eventually visit all regions of interest without any particular ordering.
- Reachability while avoiding regions: The formula \( \phi = \Box (\pi_1 \lor \pi_2 \lor \cdots \lor \pi_n) \mathcal{U} \pi_{n+1} \) expresses the property that eventually \( \pi_{n+1} \) will be true, and until \( \pi_{n+1} \) is reached, we must avoid all unsafe sets \( \llbracket \pi_i \rrbracket \), \( i = 1, \ldots, n \).
- Sequencing: The requirement that we must visit \( \llbracket \pi_1 \rrbracket \), \( \llbracket \pi_2 \rrbracket \) and \( \llbracket \pi_3 \rrbracket \) in that order is naturally captured by the formula \( \phi = \Diamond (\Diamond \pi_1 \land \Diamond (\Diamond \pi_2 \land \Diamond \pi_3)) \).
- Recurrence: The formula \( \phi = \Box (\Diamond \pi_1 \land \Diamond \pi_2 \land \cdots \land \Diamond \pi_m) \mathcal{U} \pi_{n+1} \) requires that the trajectory does whatever the coverage does and, in addition, will force the system to repeat the desired objective infinitely often.

More complicated control specification can be composed from more basic specifications using the logic operators.

For a hybrid control system, we can define LTL semantics over abstractions of the output trajectories of discrete set \( \Pi \). Let \( (y, \llbracket \cdot \rrbracket) = \phi \) to denote the satisfaction of the
LTL formula $\phi$ over the output trajectory $y(t)$ starting at time $t = 0$ with respect to the atom mapping $\Xi$. If all the output trajectories $y(t)$ of system $\Sigma$ driven by a controller $C$ are such that $((\Xi, \Sigma)|C|=\phi$, then we write $((\Sigma, H), |\Xi|=\phi$ and we say that $[(\Sigma, H)$ satisfies LTL formula $\phi$.

3.2. From LTL to Hybrid Automata

In this section, we describe an algorithmic procedure for deriving a hybrid automata whose transition system generates the models of certain fragments of LTL using the framework presented in [15]. In the following, we introduce the algorithm for the LTL$(\mathcal{U}, \wedge, \lor)$, LTL$(\exists, \wedge, \lor)$ and LTL$(\forall, \wedge, \lor)$ fragments of the logic.

The fragment LTL $(\mathcal{U}, \wedge, \lor)$ contains the Boolean operators of conjunction and disjunction and until temporal operator. According to the three propositions 1-3 in [15], the algorithm of LTL $(\mathcal{U}, \wedge, \lor)$ can be described as follows:

**Algorithm 1:** the LTL $(\mathcal{U}, \wedge, \lor)$ fragment

**Input:** A formula $\phi \in \text{LTL}(\mathcal{U}, \wedge, \lor)$

**Output:** the Hybrid Automata $H_{t}$

**procedure** LTL$_{\mathcal{U}}$toHA($\phi$)

if $\phi = \pi$ then
    return $H_{\pi}$
else if $\phi = \phi_1 \wedge \phi_2$ then
    return LTL$_{\mathcal{U}}$toHA($\phi_1$) $\cap$ LTL$_{\mathcal{U}}$toHA($\phi_2$)
else if $\phi = \phi_1 \lor \phi_2$ then
    return LTL$_{\mathcal{U}}$toHA($\phi_1$) $\cup$ LTL$_{\mathcal{U}}$toHA($\phi_2$)
else if $\phi = \pi \mathcal{U} \psi$ then
    $H_{t} \leftarrow$ LTL$_{\mathcal{U}}$toHA($\psi$)
    return $H_{t}$
end if

**end procedure**

Algorithm 1 presents the procedure for the synthesis of hybrid automata that generate the models of a specification $\phi$ in LTL$(\mathcal{U}, \wedge, \lor)$, hence we have the following the proposition:

Let $\phi \in \text{LTL}(\mathcal{U}, \wedge, \lor)$ and let $H_{t}$ be the output of algorithm 1, then $\eta \in \mathcal{L}(\mathcal{T})$ implies $\eta \models \phi$.

For the fragment $\phi \in \text{LTL}(\exists, \wedge, \lor)$, its algorithm is similar to algorithm 1 of LTL$(\mathcal{U}, \wedge, \lor)$. The algorithm of the LTL$_{\exists}$ captures both reachability and safety properties, that is, it is combinations of LTL$(\mathcal{U}, \wedge, \lor)$ and LTL$(\exists, \wedge, \lor)$. Therefore, we can take advantage of these algorithms to synthesize the controller satisfied the reachability and safety properties.

3.3. Coordinated Controller Synthesis Based on LTL

The problem of synthesizing a coordinated controller can be described by the following:

If there is a dynamic system $\Sigma$ and LTL formula $\Phi$ on set $\Pi$, we construct a coordinated controller $C$ for the system $\Sigma$, such that its trajectories generated by the close-loop control system should satisfy the LTL specification $\Phi$.

Coordinated controller synthesis includes two parts: (a) define LTL specification formula; (b) the design of coordinated controller satisfied LTL formula.

The LTL specification formula described the global control behavior, through coordinating the lower layer controller to achieve the global system stability control. The step of coordinated controller design is as follows:

First, transform the LTL formulas into hybrid automata by using these algorithms mentioned above. Then, construct a closed-loop control system combined the objects controlled in lower layer with their coordinated hybrid automata in top layer.

Hybrid automata can satisfy the requirements of reachability and safety from any state driving system trajectory. In fact, this control behavior is to simplify the entire system to combinations of a series of control controllers, that continuous trajectory produced by these controllers should satisfy the LTL formula.

4. Coordinated Controller Synthesis to Power System Substation

4.1. Hybrid Model of Power System

We make use of a substation which including OLTC controller, load shedding relay and capacitor bank switching to research the coordinated voltage control. The generator bus is modeled as an ideal voltage source. The load is modeled as a dynamic exponential recovery load, as shown in Figure 2. The voltage safe operating region is $\pm10\%$ of the rating voltage.

The hybrid dynamic model of system above power system is,

$$\dot{x}_r = \frac{1}{r}(\omega + k_1(Q_0V_r^2 - V_r^2))$$

(8)

$$\dot{x}_e = \frac{1}{r}(\omega + k_1Q_0(V_e^2 - V_e^2))$$

(9)
The control behavior of OLTC can be described by the following mathematical model:

\[ k_r(i) = k_r(i-1) + d \cdot f(\Delta V) \]  \hspace{1cm} (12)

where \( k_r(i) \) is the OLTC ratio of the \( i \)-th regulation; \( d \) is the OLTC regulation step, \( \Delta V = V - V_r \) is the voltage deviation, \( V_r \) is reference voltage; \( f(\Delta V) \) denotes up or down of OLTC regulation, its expression is

\[
f(\Delta V) = \begin{cases} 
1 & (\Delta V > \frac{1}{2}D_B) \land (t_r > T_{rd}) \land (k_r < n_{max}) \\
-1 & (\Delta V < -\frac{1}{2}D_B) \land (t_r > T_{rd}) \land (k_r > n_{min}) \\
0 & \text{others}
\end{cases}
\]  \hspace{1cm} (13)

where, \( T_{rd} \) is the sum of OLTC timer delay and mechanical delay, \( n_{max}, n_{min} \) are the maximum and minimum regulation tap respectively.

The OLTC control behavior described by model (12) can be described by a hybrid automata model, as shown Figure 3. The regulation condition of up or down of OLTC regulation is as follows

\[ \phi_{up} = \pi_{r1} \land \pi_{r3} \land \pi_{r4} \]  \hspace{1cm} (14)

4.2. The Automata Model of OLTC Controller

The control behavior of OLTC can be described by the hybrid automata model, as shown Figure 4. The automata model of capacitor banks switching is as follows:

\[ \phi_{dn} = \pi_{c2} \land \pi_{c3} \land \pi_{c5} \]  \hspace{1cm} (15)

\[ \phi_{rt} = \pi_{c6} \]  \hspace{1cm} (16)

where, atomic proposition \( \pi_{r1} = (\Delta V - \frac{1}{2}D_B) > 0 \) denotes the regulation condition when voltage is larger than the set value; \( \pi_{r2} = -(\Delta V + \frac{1}{2}D_B) > 0 \) denotes the regulation condition when voltage is lower than the set value; \( \pi_{r3} = (t_r - T_{rd}) > 0 \) denotes OLTC delay of tap regulation; \( \pi_{r4} = -(k_r(i) - k_{r_{max}}) > 0 \), \( \pi_{r5} = (k_r(i) - k_{r_{min}}) > 0 \), \( \pi_{r6} = (t_r - T_{rd}) > 0 \).

4.3. The Automata Model of Capacitor Switching Controller

Switching capacitors can produce or reduce system reactive power. The term \( K_cB_rV^2 \) in Equation (11) is the reactive power produced by the capacitor banks switched. The switching conditions are as follows: when power factor is lower than the setting value and at the same time the voltage increase slowly, we switch on the capacitor; when power factor is larger than the setting value and the bus voltage is higher than the setting value requested, the capacitor is switched off.

The condition of switching capacitor is described as follows,

\[ \phi_{cm} = \pi_{c1} \land \pi_{c3} \land \pi_{c5} \]  \hspace{1cm} (17)

\[ \phi_{rm} = \pi_{c2} \land \pi_{c4} \land \pi_{c5} \]  \hspace{1cm} (18)

\[ \phi_{rc} = \pi_{c6} \]  \hspace{1cm} (19)

The atomic propositions of the switching condition are

\[ \pi_{c1} = -(\cos \phi - f_{min}) > 0 \] , \( \pi_{c2} = (\cos \phi - f_{max}) > 0 \) , \( \pi_{c3} = -(\dot{\phi} - V_{crw}) > 0 \) , \( \pi_{c4} = (\dot{\phi} - V_{csw}) > 0 \) , \( \pi_{c5} = (t_r - T_c) > 0 \) , \( \pi_{c6} = (t_r - T_{rc}) > 0 \).

The control behavior is similar to the OLTC controller, its automata model is as shown in Figure 4.
4.4. The Automata Model of Load Shedding Controller

Load shedding is the final measure used to avoid a wide area voltage instability and voltage collapse when all other effective measures are exhausted. The condition of load shedding is: (i) The system active power safety margin is less than the setting, that is $S_{set} - \Delta S > 0$; (ii) The voltage falls to 85~95% of normal for a minimum of 5 seconds. The automatic recovery of load isn’t considered in this paper. The conditions mentioned above can be written as follow,

\[
\phi_{sh} = \pi_{s1} \land \pi_{s2} \land \pi_{s3}
\]

(20)

\[
\phi_{rh} = \pi_{s4}
\]

(21)

The atomic propositions are 1) \( \pi_{s1} = (\Delta S - S_{set}) > 0 \), 2) \( \pi_{s2} = (V - 0.90) > 0 \), 3) \( \pi_{s3} = (t_r - T_m) > 0 \), 4) \( \pi_{s4} = (t_r - T_m) > 0 \).

The automata model of load shedding is shown in Figure 5.

4.5. The Coordinated Controller on Substation

In order to avoid the voltage instability or collapse, the OLTC regulation, capacitor banks switching and load shedding in substation have to coordinate with their action each other, otherwise, would lead to control disorder and even aggravate the deterioration of the voltage.

a) The coordinated control LTL specification formula

The action principle of coordinated controller: if power system is lack of reactive power or in heavy load or power safety margin close to its settings, the capacitor should be switched on; if all capacitor banks are switched on, and the safety margin of power is still outside its settings, some load should be shed. At the same time, in order to avoid system voltage instability or collapse, lock the OLTC controller.

For the OLTC controller, its LTL formula of the coordinated adjustment is as follows

\[
\phi_r = \Box(\pi_{s1} \lor \pi_{s2})
\]

(22)

For capacitor banks switching, the coordinated action LTL formula is

\[
\phi_C = \Box(\pi_{s1} \lor \pi_{s2})
\]

(23)

\[
\phi_{sh} = \pi_{s1} \land \pi_{s2} \land \pi_{s3}
\]

\[
\phi_{rh} = \pi_{s4}
\]

Figure 5. Automata model of load shedding.

For load shedding, the coordinated action LTL formula is

\[
\phi_S = \Box(\pi_{s1} \land \pi_{s2} \land \pi_{s3} \land \neg \phi_T)
\]

(24)

where, \( \pi_c = (k_C - k_{C_{max}}) = 0 \) denotes that all capacitor banks are switched on, \( \neg \phi_T \) denotes to lock the OLTC operation during the load shedding.

The final LTL formula of coordinated controller \( \Phi_H \) is

\[
\Phi_H = \Box(\neg \pi_{s1} \land \neg \pi_{s2}) \land \{\phi_r \lor \phi_C \lor \phi_S\}
\]

(25)

where \( \Box(\neg \pi_{s1} \land \neg \pi_{s2}) \) denotes that the system is in the steady-state and has not any control action.

b) Transform the LTL formula into the Hybrid Automata

In order to implement the LTL specification formula of coordinated controller, the formula \( \Phi_H \) will be converted to hybrid automata by those algorithms introduced above. The hybrid automata model of LTL formula is shown in Figure 6.

In Figure 6, \( \pi_0 = \neg \pi_{s1} \land \neg \pi_{s2} \), and the symbol \( \llbracket \pi_0 \rrbracket \) denotes that the system is in the steady-state and has not any control. \( \pi_1 = \pi_{s1} \lor \pi_{s2} \), and \( \llbracket \pi_1 \rrbracket \) denotes that the coordinated controller allow the OLTC controller to regulate. \( \pi_2 = \pi_{s3} \lor \pi_{s2} \), and \( \llbracket \pi_2 \rrbracket \) denotes allowing the capacitor banks switching. \( \pi_3 = \pi_{s1} \land \pi_{s2} \), \( \llbracket \pi_3 \rrbracket \) denotes allowing load shedding. \( \llbracket \pi_4 \rrbracket \) denotes allowing the OLTC to be regulated after capacitor banks switching. \( \llbracket \pi_5 \rrbracket \) denotes allowing the OLTC to be regulated after load shedding.

5. Numerical Simulation

In order to verify the validity of power system voltage hierarchical coordinated control based on LTL formula, the operating process of the coordinated controller \( \Phi_H \) and the dynamic behavior of power system under several disturbances are simulated on the platform of Dymola.
regulating OLTC, can make the voltage to satisfy system requirements. This shows that the reactive power is adequate under normal conditions, so don’t need input capacitors and only depending on LOTC regulation would be able to meet the requirements of voltage. As can be seen from Figure 7 without any coordination, the input capacitor led to the OLTC regulation up-regulated and down-regulated repeatedly.

5.2. Fault Occurred under Reactive Power Deficiency

A permanent short-circuit fault occurred under reactive power deficiency state at 20 seconds and it was cleared after 0.1 second. Some cases involved in discrete controllers are discussed in the following.

1) Only the OLTC regulated
For the system under the reactive power deficiency in Figure 2, if only OLTC regulated, the voltage collapsed finally. Shown as Figure 9, the system voltage collapsed near 710 seconds. This is because the reactive power is deficiency, so the adjustment of OLTC not only can’t make voltage satisfy system requirements, but will made system further deteriorating.

2) The OLTC locked
If locked OLTC, the system collapse could be avoid and the voltage eventually be stable at low value 0.78 p.u., shown as Figure 10. However, the level of voltage is far from the system requirements.

Figure 7. The voltage curve without coordination on bus 2 and the actions of discrete controllers.

Figure 8. The voltage curve with coordination on bus 2 and the actions of discrete controllers.

5.1. Fault Occurred under Normal State

A permanent short-circuit fault occurred under normal state at 20 seconds and it was cleared after 0.1 second.

1) Without any coordination
The voltage simulating curve without any coordination on the low voltage side bus2 is shown as Figure 7(a) and the actions of the discrete controllers are shown as Figure 7(b) and Figure 7(c). We can know that one bank of capacitor is switched on, at the same time, the OLTC controller has been up-regulated 3 times, then down-regulated 3 times. But in practice the operation of OLTC controller repeatedly is not desired since it reduces the lifetime of contact of executer.

2) The operating process with coordinated controller
The voltage simulating curve and the actions of discrete controllers with coordination are shown as Fig.8. We can know that the results of action of controller under the coordination: the capacitors needn’t to be put, only the OLTC controller has been up-regulated 7 times, and the voltage finally stabilized at its allowed level.

It can thus be seen that in such circumstances, only by
3) Without any coordination

The voltage simulating curve without any coordination on the low voltage side bus 2 is shown as Figure 11(a) and the actions of the discrete controllers are shown as Figure 11(b) and Figure 11(c). We can know that three banks of capacitor are switched on and the OLTC controller has been up-regulated four times, then down-regulated three times. Although the final voltage satisfied the system requirements, but all banks of capacitors are switched on and OLTC has been up-regulated and down-regulated repeatedly.

4) The operating process with coordinated controller

The voltage simulating curve and the actions of the discrete controllers with coordination are shown as Figure 12. Two banks of capacitors were switched on and the OLTC is only up-regulated 6 times, then the power system finally stabilized at the allowed level of voltage. From the simulating results, the coordinated controller can significantly avoid the adjustment of OLTC repeatedly, at the same time, reduce one bank of capacitor switching on.

5.3. Fault Occurred under the Heavy Load

When system is under the heavy load, a permanent short-circuit fault is assumed at 20s and the fault was cleared after 0.1s.

1) Without coordination

Due to power system operating under the condition of heavy load, the system power margin is deficient when the disturbance occurred, and the controllers of OLTC and capacitor banks would operate respectively. The Figure 13 shows the operating result of multi-controller without coordination. The system voltage collapsed near 380 seconds. This shows that under the heavy load, the operation only depended on capacitor banks and OLTC is not enough.
Figure 12. The voltage curve with coordination on bus 2 and the actions of discrete controllers.

Figure 13. The voltage curve without coordination on bus 2 and the actions of discrete controllers.

Figure 14. The voltage curve with coordination on bus 2 and the actions of discrete controllers.

2) The operating process with coordinated controller

The Figure 14 is shown the action result under the coordination of the LTL specification formula, and the system voltage is finally stabled at the level of system requirements. Two groups of load are shed, and finally make the voltage satisfy the system requirements by OLTC adjustment. Through the analysis can be aware that when fault occurred under heavy load, due to overloading, the input of capacitor banks will not achieve all well. Therefore, the final measures to shed loads should be made to avoid the system collapse.
6. Conclusions

According to the hybrid characteristics of power system voltage control, a hierarchical method is adopted for the power system voltage control. The upper layer mainly completes the coordination function, and the low layer is system or equipment and the corresponding physical system controller.

The coordinated controller synthesis problem includes two parts: the global specification formula and design of the coordinated controller. We use the LTL formula to describe the global stable specification of voltage control. The LTL is a math language that can be able to flexibly describe the real-time and logic functions, and can be able to succinctly describe the coordination and logic. For the design of the coordinated controller, the proposed approach was to transform the LTL formula into the hybrid automata model, and the hybrid automata coordinated the all the low layer distributed controllers, and implement the global voltage control with them together.

Finally, a simple example of the power system is given, some cases using the proposed hierarchy coordinated control method were simulated, and the results show that the proposed method is feasible. The further work is that we continue to study the wide-area power system voltage coordinated control using the method proposed in this paper.

7. References


