Review of Modeling Methods of Distributed Energy Supply System Connected to the Grid

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Received March, 2013

ABSTRACT
At present, the development of distribution network can’t meet the requirements of rapid economic development. The traditional single energy supply is difficult to meet the request, and distributed energy supply has a lot of advantages compared to it, particularly it's close to the end users, and they have been developed well and applied widely in recent years. This paper summarizes the features and current development of the distributed energy supply, and mainly describes the grid-connection model of distributed energy supply. Base on the mathematic grid-connection model of distributed power sources with different generation principles as well as that energy storage, the treatment of these models in distribution network power flow analysis is also presented.

Keywords: Modeling; Distributed Energy Supply; Grid-connection

1. Introduction
Recently, centralized power generation, long-distance transmission and grid interconnection constitute the main way of electricity production, transmission and distribution. Long-distance transmission has its advantages, but there are also some drawbacks, including: Cannot agilely tracking load changes, local accident easy to expand to a major accident. In addition, centralized power generation consume a large number of fossil fuels, produce large amounts of greenhouse gases and substances harmful to the environment. For the purpose of environmental protection, it is necessary to use more wind, solar and other renewable energy. Therefore, the interest in using renewable energy and small/medium-sized generators are increasing, especially in the increasingly rapid development of wind power and photovoltaic power generation. A lot of research and practice in this area have been done. At the same time, the new technology of using conventional fossil fuels, fuel cells and microturbines is also object of the study. They can reduce the emission of pollutants greatly. Most experts agree that combination of large power grid and distributed power generation, together with the appropriate energy storage equipment, so as to save investment, reduce energy consumption, improve power system reliability and flexibility, and are the keys to the development of the electric power industry.

2. Research Status of Distributed Power and Energy Storage Battery
Currently, the exact definition of distributed power supply is not recognized. The common definition is that generated power from 1 kW to 50 MW of small independent power module. They are typically installed near the user, in order to meet the specific needs of the user or to support the economic operation of the existing distribution network [1].

At present, the widely use of distributed power supply system mainly contain wind power, photovoltaic cells, fuel cells, micro turbines and storage batteries. The distribution network is generally designed to radiate, user side does not have any power supply. Penetration of distributed power makes the network have more than one power supply node. This will create difficulties for the operation of the power grid, will seriously affect the distribution network power flow, increase short-circuit current of the power distribution network, and make voltage regulation becomes difficult. In order to improve the power quality and operational reliability, its install location and capacity must be optimized.

Thus, in order to apply to the distributed power access, the original method of power flow calculation applied to traditional radial distribution network planning and optimization must be improved [2].

[3] Proposed an object-oriented modeling method and a reconfiguration algorithm for radial distribution network which take into account the distributed power...
access. The method has strong scalability and applicability that it can easily connect a variety of different interfaces of distributed power.

A power flow calculation method based on the compensation method presented in [4]. The whole model includes the three-phase unbalanced load, circuitries, capacitors, transformers and a distributed power supply. This model’s rapidity has been verified in case of ensuring accuracy. At present, the research literature on distributed power mainly concentrated in a radial network with a single distributed power source, seldom consider the characteristics of the distributed power itself. Interaction between distributed power and energy storage device may affect distribution network planning, power quality and voltage stability. The above study of the distribution network cannot be separated from the flow calculation. Different distributed power and energy storage device access to distribution networks will have different effects on the distribution power flow. Therefore, the establishment of mathematical models of different types of distributed power source/energy storage device connected to the grid, has important significance on the topological analysis, power flow calculation, relay protection, and the planning and configuration distribution network.

3. The Mathematical Grid-connection Model of the Distributed Energy Supply System

3.1. Wind power

The biggest difference between wind power and conventional power generation mode is the fluctuation of output power caused by the uncertainty of the input (wind speed). Accordingly the accurate prediction of power output of wind turbine is the key to establish wind generator model.

A stochastic model of wind turbine has been established, which is based on Weibull model [5]. Weibull model is considered to be the most suitable model for statistical description of the probability density function of wind speed. Under normal circumstances, the wind speed estimates range between the cut-in speed and cut-out speed. When the request for accuracy is not rigid, the output power of wind turbine was approximately linear with wind speed. Therefore, the probability density function of the wind generator output power can be written as:

\[ f(P_w) = \frac{k}{k_c}(\frac{P_w}{k_c})^{k-1}\exp[-(\frac{P_w}{k_c})^k] \]  \hspace{1cm} (1)

The parameters \( k, c \) in the equation can be figure out by using the mean \( \mu \) and standard deviation \( \sigma \):

\[ k = \left(\frac{\sigma}{\mu}\right)^{0.086} \]

\[ c = \frac{\mu}{\Gamma(1 + \frac{1}{k})} \]

\[ k_1 = \frac{P_r}{v_r - v_{ci}} \]

\[ k_2 = -k_1v_{ci} \]

where \( P_r \) is rated power of wind turbine, \( v_r \) and \( v_{ci} \) are cut-in wind speed and rated wind speed respectively.

The wind generator generally uses asynchronous motor, which does not produce reactive power and need to absorb reactive power from grid. Assume that the reactive power can be compensated and power factor keeps stable, then the wind generator can be seen as a PQ node. The node model of asynchronous wind generator is shown in Figure 1 [6].

The relation between the reactive power Q and P, V was obtained through the analysis of the circuit, as follows.

We can get equation associated with reactive power, P and V through the circuit analysis, as follows:

\[ Q = V^2 \left( \frac{X_c - X_m}{X_cX_m} + \frac{X}{V^2} \right)P^2 \]  \hspace{1cm} (2)

where \( X_c, X_m \) are the generator-side shunt capacitance and excitation reactance respectively. \( X_1, X_2 \) are stator leakage reactance and rotor leakage reactance respectively. \( X = X_1 + X_2 \).

Thus, the characteristic of the PQ node can be obtained, by calculating relation curve of P, Q node and input mechanical power.

[7] Put forward the positive and negative sequence circuit of wind turbines, it considered the influence of the fan slip, and use symmetrical component method to analyze the equivalent circuit of the wind generator. The function about the slip and the positive/negative sequence current of rotor can be determined, by calculation of the input impedance in the positive and negative sequence circuit. Then the input DC value can be calculated according to the positive and negative sequence voltage value. Base on neglecting the loss, linked the output of the wind turbine with wind input curve, the odd equation can be written as:

\[ \sum_{n=0}^{T} Q(x^i) = 0 \]  \hspace{1cm} (3)

Figure 1. The equivalent circuit of induction motor.
The slip $s$ can be calculated by Newton’s method, and then the node voltage and power distribution value which are need in power flow calculation.

A kind of RX model of wind turbine was suggested in [6,8].

The active power of the wind turbine output is derived as:

$$P_a = -I_r^2 \times R_s (1 - s) / s$$  \hspace{1cm} (4)

where $I_r$ and $R_s$ are rotor current and rotor resistance respectively.

This power and mechanical power that generated by wind turbine should be equal. When they are not equal, we can balance the wind turbine mechanical power and motor’s output power through the iterative correction of slip $s$.

According to the equivalent circuit of the induction motor, the expression of reactive power on the voltage can be launched [9].

$$Q = \frac{V^2}{X_p} + \frac{V^2 + \sqrt{V^4 - 4P^2X^2}}{2X}$$  \hspace{1cm} (5)

where $X_p = \frac{X_cX_m}{X_c - X_m}$. It is being used as a static voltage characteristic node in distribution network to deal with in power flow calculation.

The methods described above treat the power factor of wind turbine as a fixed value, but the actual value of power factor may not be kept constant.

Therefore, the P-Q-U model of asynchronous generator was proposed [10].

Based on considering the slip, it derived the expressions of wind turbine output power through analyzing the circuit diagram. The expressions of both the slip and the power factor are also obtained. In the case of a given wind speed, it is possible to get each moment the output of the active and reactive absorption, and accordingly calculate the power factor.

The power factor is confined within an allowable limit through the shunt capacitance sets real-time turned on/off.

### 3.2. Photovoltaic Cell Power Generation

Photovoltaic power generations are mainly divided into two types: off-grid photovoltaic power generation system and the grid-connected photovoltaic power generation system. And grid-connected photovoltaic power generation is the mainstream of the development of photovoltaic power generation. PV cells are connected to the grid, electricity generated directly deliver back to the grid. Thus, wind turbines can always run in the power factor 1, and it avoid the problems like that energy storage and additional facilities bring.

Similar to the modeling approaches of wind power random characteristics, the output of PV cell is the random output, which is proportional to the light intensity. In a certain period of time, the light intensity can be modeled as Beta distribution. Therefore, the output power of the battery also satisfies the Beta distribution. Its probability distribution function is as follows:

$$f(P_m) = \frac{\Gamma(\alpha + \beta)}{\Gamma(\alpha)\Gamma(\beta)} \frac{P_m^{\alpha-1}(1 - P_m)^{\beta-1}}{R_m}$$  \hspace{1cm} (6)

where $\alpha, \beta$ are the shape parameters of Beta distribution. $P_m$ is the total output power of Photovoltaic array. $R_m$ is the maximum output power of PV array.

Another model of random power flow is raised in [11]. The main factor affects the intensity of solar radiation is clouds.

It presents a clearness index $K_t$, used to indicate the ratio of the radiation intensity on ground plane and the total extraterrestrial radiation intensity. The output active power of PV system is:

$$P_{pv} = \eta A_c I_{ph} = \eta A_c (T \times K_t - T' K_t')$$  \hspace{1cm} (7)

where $A_c$ is the Photovoltaic array area and $\eta$ represents efficiency. $T$ and $T'$ are the parameters related to the location and inclination of the photovoltaic system. Probability density function of the real power output is:

$$f_{pp}(PV) = \begin{cases} e^{\frac{c[K_m - 0.5(a\alpha')]}{\pm K_m\eta T' A_c^{\alpha'}}}e^{0.5(a\alpha')} \frac{\alpha}{T'} & \text{if } P_{pp} \in [0, P_{pp}(K_m)] \\ 0, & \text{otherwise} \end{cases}$$  \hspace{1cm} (8)

where $\alpha = \frac{T}{T'}$, $\alpha' = \sqrt{\alpha^2 - 4 \frac{P_{pp}}{\eta T'A_c}}$, $K_m$ is the maximum value of $K_t$, $C$ is the parameter of probability density function.

The time distribution of active power output of these two random power flow model can be obtained by using the Monte Carlo method.

Another model of photovoltaic cells was given [12-14].
The mathematical model of a single photovoltaic cell can be derived through the circuit analysis. Its circuit diagram is as follows:

\[ I = I_{ph} - I_o \{ \exp[q(V + IR_x)/AkT] - 1 \} - (V + IR_x)/R_{sh} \]

\[ I_0 = I_{0r} \left( \frac{T}{T_r} \right) \exp \left[ \frac{qE_{cell}}{kA} \left( \frac{1}{T_r} - \frac{1}{T} \right) \right] \]

where \( T \) is the temperature of the battery and the parameter is relevant to the environment. The remaining parameters are fixed parameters associated with materials and design of photovoltaic cells.

Thus, suppose the number of photovoltaic cells is \( n \) and the number of parallel modules is \( m \), such a PV array output power is:

\[ P = V_{array} \times I_{array} = mV \times nI = mn[I_{ph} - I_o \{ \exp[q(V + IR_x)/AkT] - 1 \} - (V + IR_x)/R_{sh}] \]

The equation above can be solved by using Newton iteration. The PV cell connected to the grid through the inverter. The model above considers the efficiency of the rectifier as constant for simplicity. In fact, the efficiency of inverter will change with the input power. [15] Had proposed the correction relation equation of input power of the inverter.

\[ P_{inv,u} = -0.015 + 0.98P_{pr,a} - 0.09P_{pr,a}^2 \]

Variable is the P.U. value which relative to the rated capacity.

The input variable in the right hand side of equation is the output power of PV array. The output variable in left side of equation is the input power.

Generally, only the active power of photovoltaic cells can be used in distribution network. The possible maximum power of output can be achieved through tracking method of maximum power point. However, in the case of part of output active power lose; it can make the grid operating more stable and economic by controlling the inverter.

[16] Put forward the model which limits the output of inverter. It can be divided into a current control type and a voltage control type. In the current control type, it can be treat as the PI node and its output active power and the injection current is constant.

The reactive power injections can be calculated from the following formula.

\[ Q = \pm \sqrt{|P|^2 \left( e^2 + f^2 \right) - P^2} \]

where \( P \) is the constant node active power value, \( I \) is the constant current value, and \( e, f \) are the vectors of calculating voltage. If the model is of the type of a voltage control, inverter will be treating as a PV node, just like generator node. When the input current reaches to the borderline value, it will change into PI node.

### 3.3. Fuel Cell

Fuel cell has the characteristic of small volume and high efficiency. Its theoretical efficiency can reach to ninety percent. Its power supply is reliable, low noise, high power quality and more automatic. The efficiency of fuel cell which capacity ranges within 250kW to 5MW is similar to the efficiency of thermal power generator which capacity ranges within 300-500MW.

These fuel cell need to have fuel such as hydrogen, but it drive motor not by burning. In the presence of a catalyst, it reacts with oxygen directly. Therefore, the fuel cell is essentially a chemical energy generation.

With regard to the fuel cell accessing to distribution network, the first need to consider is the characteristics of its generating electricity.

The equation of output voltage of fuel cell power system is as follows [17, 18]:

\[ U_{cell} = N\left[ E_0 + \frac{RT}{2F} \ln \frac{x_{H_2}^2 x_{O_2}}{x_{H_2O}^2 x_{H_2}} \right] - E_{loss} \]

Where \( N \) is the number of series fuel cell, \( E_0 \) is the single battery standard potential, \( T \) is the temperature and \( x \) is the corresponding gas molar concentration. The last one is potential loss caused by system.

The output of fuel cell is DC, so it needs to be converted into AC before connected to the distribution network.

The active and reactive power generated by fuel cell can be derived from Figure 3 [19, 20].

\[ \begin{align*}
P &= \frac{mU_{cell}V_S}{X} \sin \delta \\
Q &= \frac{mU_{cell}V_S}{X} - \frac{V^2}{X}
\end{align*} \]

where \( X \) is the line impedance from the fuel to grid, \( V_S \) is the voltage of distribution network side. It controls the output of active and reactive power through control the parameters \( m \) and \( \delta \). This method is similar to the principle of conventional generator’s power regulator.

Therefore, fuel cells in power flow calculation can be treating as a PV node. But the reactive power output of inverter is limited. When reactive power limits are exceeded, it will be transformed into PQ node.

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3.4. Micro Gas Turbine

Gas turbine works like ordinary synchronous generator. It has a speed control system and excitation system. The speed control system adjusts active power output according to load level.

\[ P_r = \eta \times \left[ 1.3(W_f - 0.23) + \frac{1 - N}{2} \right] \]  \hspace{1cm} (16)

where \( \eta \) is the efficiency of turbine mechanical power into electric power, the fuel ratio required for no-load operating is 0.23, \( W_f \) is fuel flow, \( N \) is rotational speed.

Microturbine combines the traditional gas turbine with the recuperator, permanent magnet generator, variable frequency regulation technique and intelligent control technology.

The current generated by microturbine need to transform to power frequency current before import to distribution network. Whereas, just like centralized generators, its active power can still be adjusted:

\[ Q = \left| V'_{f,i} \right| \left| V'_{i} \right| \frac{1}{X'_{f,i}} \]  \hspace{1cm} (17)

\[ P_{m,in} - P_{m,out} = \frac{1}{R} \frac{w - w_r}{w_r} \]  \hspace{1cm} (18)

where \( V' \) is the engine power, \( X'_{f,i} \) is the motor output power, \( P_{m,in} \) and \( P_{m,out} \) are the input and output power of engine respectively, \( w \) and \( w_r \) are the angular velocity of the sending end and receiving end of power units, \( M \) and \( R \) are the torque and impedance of generator respectively.

Excitation device and power electronic device keep the output voltage of gas turbine stable. For this reason, gas turbine generator can be treating as a PV node. For the voltage deviation appear in process of iterative algorithm, the reactive power can be adjusted by sensitivity matrix. In the iterative process, the node type converts between PV node and PQ node once the reactive power or voltage exceeds the limit.

4. The Mathematical Model of Energy Storage Device Distributed Access grid

4.1. Battery Model

Battery model is the most studied storage way. Its unit energy storage cost is low. [21] Put forward with a model of battery cell access to distribution network.

The current of battery itself is DC. Hence, it need the converter help to access to grid. The active and reactive power through inverter and grid is as follow:

\[ \begin{align*}
P &= \frac{U_s U_R \sin \delta}{X} \\
Q &= \frac{U_s}{X} (U_R - U_s \cos \delta)
\end{align*} \]  \hspace{1cm} (19)

where \( X \) is impedance, \( U_s \) and \( U \) are the output voltage of Distribution network and storage battery respectively. The exchange of active and reactive power between battery and grid can be adjusted through controlling the phase shift and the output amplitude of inverter.

4.2. The Charge/Discharge Process of Battery

The charge/discharge process of battery is divided into three stages: main charge mode (constant current), float charge mode (liminary-voltage) and even charge mode (constant voltage).

4.2.1. Main Charge Mode

The system will charge battery if it detect that battery lack of electricity. To prevent violent reaction affect the battery life, it uses constant current charging mode. The current rating is commonly 0.1C. Where, \( C \) is the capacity of battery pack. The battery can be topped up in 10 hours if it has been charging in this way. For constant current charge, the voltage of battery pack will continue to rise. When it rises to nominal voltage of single battery, float charge mode will displace main charge mode.

4.2.2. Even Charge Mode

Experiments show that charging in constant current mode need eight hours to get back to 80 percent. After this, it adopts to even charge mode automatically. The limit voltage is 24n, where \( n \) represent the number of a pack. This process takes almost 10 hours, and the charging current reduces gradually. When the current is 0.01 C, the battery is fully charge. At this point, the float charge mode begins.
4.2.3. Float Charge Mode
The float charge mode is the main way of long-running. The voltage of float charging is 235n. The system changes it into main charge mode when the capacity is shortage cause by outage.

The battery can discharge with constant current. It can keep the output power constant for a considerable time.

5. Summary and Prospect
This article summarizes numerous model of different electric-generation principle of distributed energy supply access grid. They include distributed power supply and distributed storage system. For the study of distributed energy supply system attract more and more attention. Distributed energy access to distribution network is the future trend of the development of the power system.

Wind power generator mainly use asynchronous generator model, generally considered as accessing to distribution network directly. According to the needs of the calculation accuracy, they can be handled as PQ or PQU nodes. For photovoltaic power generation, the main consideration is modeling of the relationship between the output active power and sunshine intensity. In the case of special requirements, it can adjust the reactive power by using power electronic device. The modeling of the fuel cell is that connect the battery to grid through the switching of electric power electronic device, which control the output active and reactive power. The modeling of microturbine is similar to the general synchronization generator, but need to consider the effects produced by power electronic control unit. Storage battery also need power electronic device to access to distribution network, and to take reasonable charge and discharge model according to the different stages of charge and discharge. According to the need of analysis and control of distributed energy supply system accessing to grid, we need to build a unified mathematical model which consider different power generation principle. This model will provide a basis for power flow analysis, short-circuit current calculation as well as a variety of advanced analysis software for transmission and distribution network.

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