Direct Torque Control Strategy of an Induction-Machine-Based Flywheel Energy Storage System Associated to a Variable-Speed Wind Generator

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ABSTRACT
The flywheel energy storage systems (FESSs) are suitable for improving the quality of the electric power delivered by the wind generators and for helping these generators to contribute to the ancillary services. Presently, FESSs containing a flux-oriented controlled (FOC) induction machine (IM) are mainly considered for this kind of application. This paper proposes the direct torque control (DTC) for an IM-based FESS associated to a variable speed wind generator (VSWG), and proves through simulation results that it could be a better alternative.

Keywords: VSWG; FESS; IM; DTC; DC Bus Voltage Control; Power Flow

1. Introduction
The actual decentralized electricity sources cannot participate in the ancillary services of the power grid (voltage and frequency control, black start, and islanding operation). From the viewpoint of the power grid, these sources are like negative charges, i.e., they do not consume the electric energy but generate it, without participating in the ancillary services [1]. The mains voltage and frequency control is always reported to the classical generators. Hence, the penetration rate of the decentralized electricity production is restricted in order to keep the power grid’s stability. This is particularly right for the renewable energy sources, whose primary energy source is very fluctuant and unpredictable. The wind generators belong to this category of energy sources, and to give them the possibility to participate in the ancillary services, a generating system, which is able to feed isolated loads or to be integrated in the network, has to be considered.

In order to reach these objectives, an Energy Storage System (ESS) is needed for controlling the power flow between the wind generator and the power grid [2,3]. In fact, the ESS can contribute to the energy balance between the production and the consumption. It provides the energy in case of consumption deficiency and accumulates it at high wind speeds for which the energy request is reduced [4].

Due to the important fluctuation of the wind, conventional electrochemical batteries are not suitable [5]. They cannot support the number of required cycles nor to store a significant quantity of energy in a restricted volume [6]. The storage system must have a high dynamics in order to operate in real time, in function of the generated and consumed power fluctuations, respectively. In the last years, flywheel energy storage systems (FESSs) have been rediscovered by the industrials due to their advantages in comparison with other ESSs [7,8]. They are well appropriated because of their characteristics: high dynamics, good efficiency, long lifetime (similar to the wind generators) and ecological system [7]. The FESSs constitute short-term storage systems, which are generally sufficient to improve the electric power quality. [9, 10] show that the FESS offers an interesting solution to adapt the production to the consumption. In this paper, a FESS associated to a variable-speed wind generator (VSWG) is studied. By means of power electronic converters, the energy generation and storage systems can be connected to the DC bus in order to control the power flow from the VSWG to the isolated loads. In such a configuration, the FESS ensures the DC bus voltage control [11,12], thus contributing to the generation/consumption balance of energy.

The FESS considered for this application contains a low-speed flywheel and a classical squirrel-cage induc-
tion machine (IM). The IM operates in the flux-weakening region, thus allowing operation at the rated power. Until the present time, only the field-oriented control (FOC) has been considered for this type of FESS [2,11,13]. In this paper, we propose a different control method of the FESS i.e. the direct torque control (DTC). In [14-16], good comparisons between FOC and DTC are given, but only the motoring operation mode at the rated flux is considered. The application of the DTC to the IM of the FESS involves two aspects: 1) the IM must operate in the flux-weakening region and 2) it must change rapidly and many times between the motoring and generating operation modes. In other words, the IM is always operating in the transient conditions. The steady-state operation is inexistant in this application. This paper will show that the DTC can satisfy these requests.

The proposed control system is then simulated using MATLAB-SIMULINK. The obtained results are presented and discussed to demonstrate the performance of the global system.

2. Studied System

The system studied is constituted of a permanent-magnet synchronous generator (PMSG)-based VSWG, an IM-based FESS, power converters (rectifiers/inverters), as shown in the Figure 1. The FESS is controlled by DTC Technique. The goal of the system is to provide a constant power and voltage to the isolated load connected even if the flywheel speed varies. This can be achieved mainly by the control of the DC bus voltage at a constant value and the flywheel energy storage system participate to maintain the power of the load constant as long as the wind power is sufficient.

The study focuses on the control strategy, efficiency and dynamic performance of the FESS associated to a VSWG.

3. Modeling of the FESS

The FESS, as shown in Figure 1, comprises a flywheel, an IM and a converter 2 (rectifier/inverter), which controls the speed of the flywheel and therefore the exchanged power.

3.1. Flywheel Modeling

The energy stored in the flywheel depends on the square of the rotational speed [7], for a given inertia, as represented as follow:

$$E_f = \frac{1}{2} J_f \Omega_f^2$$

(1)

with $J_f$ (kg·m²) and $\Omega_f$ (rad/s) are the inertia moment and the speed of the flywheel, respectively.

To calculate the wheel inertia, we consider a power required during $\Delta t$ time. In fact, to store the rated power of the IM $P_{n-IM}$ during $\Delta t$, the energy $\Delta E$ is then necessary such as:

$$\Delta E_f = P_{n-IM} \Delta t$$

(2)

Combining Equations (1) and (2), we define the necessary value of the wheel inertia as:

$$J_f = \frac{2 P_{n-IM} \Delta t}{\Omega_f^2} = \frac{2 P_{n-IM} \Delta t}{\Omega_{f_{max}}^2 - \Omega_{f_{min}}^2}$$

(3)

$\Omega_{f_{max}}$ and $\Omega_{f_{min}}$ represent the maximal speed limit and the minimal speed limit of the flywheel, respectively. $\Delta t$ is then the storage period. This limit must be respected otherwise we risk to deteriorate the flywheel energy storage operation [17].

3.2. Mechanical Shaft Modeling

The evolution of the mechanical speed of the IM-based FESS can be easily determined using the dynamic equation. The simplified model of this equation is given by:

$$J_f \frac{d\Omega_f}{dt} = T_{em} - f \Omega_f$$

(4)

where $T_{em}$ (N·m) is the electromagnetic torque and $f$ (N·m·s·rad⁻¹) is a viscous friction coefficient.

![Figure 1. Configuration of the studied generation system.](image)
3.3. IM Modeling

The model generally used in the cage IM is the model of Park [18]. In our approach, we adopt the d-q model of the IM expressed in the stator frame noted by ($\alpha\beta$). The currents and the flux and are given by the following equations:

$$\frac{d i_{sa}}{dt} = -\frac{R_s}{\sigma L_s} i_{sa} + \frac{M}{\sigma L_s L_r} \phi_{s\alpha} + \frac{M}{\sigma L_s} \Omega \phi_{s\beta} + \frac{1}{\sigma L_s} V_{sa}$$

$$\frac{d i_{sb}}{dt} = -\frac{R_s}{\sigma L_s} i_{sb} - \frac{M}{\sigma L_s L_r} \Omega \phi_{s\alpha} + \frac{M}{\sigma L_s} \phi_{s\beta} + \frac{1}{\sigma L_s} V_{sb}$$

$$\frac{d\phi_{s\alpha}}{dt} = \frac{M}{T_r} i_{sa} - \frac{1}{T_r} \phi_{s\alpha} - p\Omega \phi_{s\beta}$$

$$\frac{d\phi_{s\beta}}{dt} = \frac{M}{T_r} i_{sb} + p\Omega \phi_{s\alpha} - \frac{1}{T_r} \phi_{s\beta}$$

where:
- $L_s$, $L_r$: are the cyclique-propre inductances of the stator and of the rotor (H);
- $M$: is the mutual inductance between the stator and the rotor (H);
- $\sigma = 1 - \frac{M^2}{L_s L_r}$: is the dispersion coefficient of the machine;
- $R_s$, $R_r$: are the resistances of the stator and rotor (Ω),
- $R_s = R_r = \frac{M^2}{L_s L_r}$ (Ω);
- $T_r = \frac{L_s}{R_s}$: is the rotor speed constant;
- $\phi_{s\alpha}$, $\phi_{s\beta}$: are the $\alpha$-$\beta$ components of the rotor flux respectively (Wb);
- $i_{sa}$, $i_{sb}$: are the $\alpha$-$\beta$ components of the stator currents respectively (A);
- $V_{sa}$, $V_{sb}$: are the $\alpha$-$\beta$ components of the stator voltages respectively (V);
- $p$: is the number of pairs of poles.

The electromagnetic torque is given by:

$$T_{em} = p \frac{M}{L_s} (i_{sa}\phi_{s\alpha} - i_{sb}\phi_{s\beta})$$

(6)

4. Control of the FESS Associated to a VSWG

4.1. Control Strategy for the FESS

The wind generators are considered as negative charges for the power grid, because they do not consume the electric energy but generate it without participating to the ancillary services. It is well known that the wind speed is very fluctuant, and for this reason, the wind generator will deliver a variable electric power [9].

To overcome this drawback, two methods are available:

1) Acting on the mechanical system, using the pitch or stall-controlled wind turbines in order to deliver a constant power to the wind generator [19,20];

2) Acting on the electric system, associating an energy storage system with the wind generator in order to regulate the electric power delivered into the power grid [2,11].

The first method gives acceptable results when connecting the wind generators at a strong power grid, but if the wind generator supplies a weak grid or an isolated load, the power fluctuations can still be questionable. That is the reason for choosing the second method in the power regulation. An energy buffer is needed in order to make a good power regulation [2,11].

Figure 2 gives a graphic explanation of the control principle of the FESS. The FESS has two functions: to regulate the DC bus voltage and to regulate the power flow toward the load [21].

From Figure 1, the evolution of the DC bus voltage can be deduced:

$$\frac{dv_{dc}}{dt} = \frac{1}{C} (i_1 + i_2 - i_3)$$

(7)

To regulate the DC bus voltage, a PI voltage controller is used and gives the value of the power $\Delta P$ required for maintaining this voltage at the reference value $v_{dc-ref}$. To control the speed of the flywheel energy storage system we must find reference speed which with the system must turn to ensure the energy transfer required at each time. The reference speed can be determinate by the reference energy. The power assessment of the overall system is given by [21]:

$$P_{f-ref} = P_{load} - P_{sg} + \Delta P$$

(8)

where $P_{f-ref}$ is the reference value of the active power exchanged between the FESS and the load, $P_{load}$ is the
load demand power and \( P_{eg} \) is the optimal active power generated by the VSWG.

If \( P_{eg} \) is positive, means that exists energy in excess which can be stored. If \( P_{eg} \) is negative, a lack in energy exists and it will be replaced by the stored energy.

4.2. DTC for the FESS IM

4.2.1. DTC Principle

The IM is controlled by DTC Technique. DTC method has been first proposed for induction machines. DTC technique introduced by Takahashi and Noguchi [22] for low and medium power application and DTC technique introduced by Depenbrock [23] for high power application are popular in industry. DTC strategy is quite different from that of the FOC or vector control, which does not need complicated coordination transformations and decoupling calculation [24].

The DTC technique is based on the direct control of the stator flux and torque. In this technique, the supply voltage and stator current are sampled. In order to control the stator flux and torque, the supply voltage to apply based on the position of the stator flux and the required changes in stator flux magnitude and torque [25]. The selected voltage vector will be applied to the IM at the end of the sample time. In voltage source converter, there are six equally spaced voltage vectors having the same amplitude and two zero voltage vectors. Figure 5 illustrates the voltage vectors in every sector, which are selected from the eight possible switches configurations, using the look-up table given in Table 1.

In DTC, torque and flux are controlled independently by selecting the optimum voltage space vector for entire switching period and the errors are maintained within the hysteresis band [26]. In conventional DTC, only one vector is applied for the entire sampling period. So for small errors, the machine torque may exceed the upper/lower torque limit. Instead by using more than one vector with in the sampling period torque ripple can be reduced. The slip frequency can be controlled precisely by inserting zero vectors [27]. For the small the hysteresis band, frequency of operation of PWM converter could be very

\[ S_i = 0 \] the phase \( i \) is connected to the supply negative polarity

The stator-current space vector \( \mathbf{i}_s \) derived from the measured currents \( i_a, i_b, \) and \( i_c \):

\[
\begin{align*}
\mathbf{i}_s &= \sqrt{3} \left( \frac{1}{2} (i_a + j i_b) \right) \\
\mathbf{i}_s &= \sqrt{2} \left( i_b - i_a \right)
\end{align*}
\]  

The electromagnetic torque \( T_{em} \) of the motor can be evaluated as follows:

\[
T_{em} = p (\varphi_{\alpha} i_{\beta} - \varphi_{\beta} i_{\alpha})
\]

The basic model of the conventional DTC IM scheme is shown in Figure 3. The magnitude of stator flux and electric torque calculated are compared with their reference values in the hysteresis comparators shown in Figure 4 and then the outputs of the comparators are fed to a switching table to select an appropriate converter voltage vector. The switching table shown as Table 1 determine the voltage vector to apply based on the position of the stator flux and the required changes in stator flux magnitude and torque [25]. The selected voltage vector will be applied to the IM at the end of the sample time. In voltage source converter, there are six equally spaced voltage vectors having the same amplitude and two zero voltage vectors. Figure 5 illustrates the voltage vectors in every sector, which are selected from the eight possible switches configurations, using the look-up table given in Table 1.

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Table 1. Switching table.

<table>
<thead>
<tr>
<th>( C_P )</th>
<th>( C_T )</th>
<th>Sector I</th>
<th>Sector II</th>
<th>Sector III</th>
<th>Sector IV</th>
<th>Sector V</th>
<th>Sector VI</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0</td>
<td>V_d(110)</td>
<td>V_d(010)</td>
<td>V_d(011)</td>
<td>V_d(001)</td>
<td>V_d(101)</td>
<td>V_d(100)</td>
</tr>
<tr>
<td>0</td>
<td>1</td>
<td>V_d(111)</td>
<td>V_d(000)</td>
<td>V_d(111)</td>
<td>V_d(000)</td>
<td>V_d(111)</td>
<td>V_d(001)</td>
</tr>
<tr>
<td>0</td>
<td>-1</td>
<td>V_d(101)</td>
<td>V_d(100)</td>
<td>V_d(010)</td>
<td>V_d(011)</td>
<td>V_d(000)</td>
<td>V_d(111)</td>
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<tr>
<td>0</td>
<td>0</td>
<td>V_d(000)</td>
<td>V_d(111)</td>
<td>V_d(000)</td>
<td>V_d(111)</td>
<td>V_d(010)</td>
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<tr>
<td>-1</td>
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<td>V_d(011)</td>
<td>V_d(011)</td>
<td>V_d(011)</td>
</tr>
</tbody>
</table>
Electromagnetic Torque and Stator Flux Estimators is an important aspect of the system. The electromagnetic torque \( \mathbf{T}_{em} \) and stator flux \( \mathbf{\Phi} \) are calculated based on the current and voltage measurements. The stator flux \( \mathbf{\Phi} \) is estimated using the following expressions:

\[
\mathbf{\Phi} = \mathbf{L}^{-1} \mathbf{v} - \mathbf{R} \mathbf{i}
\]

where \( \mathbf{L} \) is the inductance matrix, \( \mathbf{v} \) is the voltage vector, and \( \mathbf{i} \) is the current vector.

The electromagnetic torque \( \mathbf{T}_{em} \) is calculated as:

\[
\mathbf{T}_{em} = \mathbf{L} \mathbf{\dot{\Phi}} - \mathbf{R} \mathbf{\dot{i}}
\]

The control scheme involves the use of a PI controller to determine the reference torque, based on the difference between the reference and instantaneous speeds of the motor.

4.2.2. Flux Reference Determination

Since the maximum speed of the flywheel is 3000 rpm, whereas the base speed of the IM is 1500 rpm, the FESS IM must operate in its flux-weakening region in order to reach the maximum speed of the flywheel. In this region, the rated power of the IM is still available from 1500 to 3000 rpm.

Flux-weakening control of the IM is usually accomplished by regulating the stator flux according to the following control law [28]:

\[
\phi_{s-ref} (\Omega_f) = \begin{cases} 
  \phi_{s-rated} & \text{if } \Omega_f \leq \Omega_b \\
  \phi_{s-rated} \frac{\Omega_b}{\Omega_f} & \text{if } \Omega_f > \Omega_b
\end{cases}
\]

where \( \Omega_b \) is the IM base speed and \( \phi_{s-rated} \) is the IM-

Figure 3. FESS control scheme using DTC for the IM.

Figure 4. Hysteresis comparator (a) Stator flux; (b) Torque.

Figure 5. Voltage vectors.

The energy reference value \( E_{f-ref} \) is determined from the power reference value:

\[
E_{f-ref} = E_{f0} + \int P_{f-ref} dt
\]

\( E_{f0} \): is the initially flywheel stored energy.

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The switching frequency always varies according to the width of hysteresis band.

The power reference value \( P_{f-ref} \) allows us to determine the flywheel speed reference value controlled via converter 2 (Figure 1). The flywheel reference rotational speed can be deduced from (1):

\[
\Omega_{f-ref} = \sqrt{\frac{2E_{f-ref}}{J_f}}
\]

The energy reference value \( E_{f-ref} \) is determined from the power reference value:

\[
E_{f-ref} = E_{f0} + \int P_{f-ref} dt
\]

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The control scheme of the FESS IM is presented in Figure 3.

5. Simulation Results and Discussions

We present the simulations results, using numerical simulations carried under the Matlab-SIMULINK, of the FESS associated to a VSWG. Simulation is made with a wind power profile which provides power continuously required by the load through the FESS. Figure 6 shows the VSWG power $P_{\text{wg}}$ and the load demand power $P_{\text{load}}$ which equal to $-1$ kW.

Initially, the speed of the flywheel is 235.6 rad/s (2250 rpm).

Figure 7 shows the FESS power and its reference power. It depicts the power stored (positive) or generated (negative) by the FESS. We note that the power exchanged between the FESS and the isolated load, is very fluctuant, as the VSWG power is, which causes the flywheel to slow down/accelerate.

Flywheel speed and the reference speed are plotted in Figure 8. The rotational speed increases when the energy is transferred to the flywheel, and decreases when the flywheel is unloaded. Figure 9 gives the IM electromagnetic torque which is fluctuant, like the VSWG power, and entails the flywheel speed variations.

The FESS regulates the DC bus voltage which is well maintained at 400 V (Figure 10). Thus, the simulation results prove that a DTC-IM can satisfactorily be used in FESS associated to a VSWG.

6. Conclusion

A contribution to improvement of the performances for
wind energy conversion systems of VSWG associated to a FESS has been presented in this paper. A low-speed FESS, whose electric machine is a classical squirrel-cage IM, has been considered. A new DTC control strategy has been applied to the IM. This application involves two main constraints on the IM: it must operate in the flux-weakening region and it must change rapidly and many times between motoring and generating operation modes. Simulation results have shown that DTC can fulfil these requirements and proved that the DTC IM-based FESS can control the DC bus voltage and the power flow from the VSWG to the isolated load.

As compared to FOC, DTC is simpler in experimental implementation and needs less demanding controllers. It has also been proved that DTC can operate with constant switching frequency by using discrete hysteresis controllers, which are appropriate to DSP control boards.

REFERENCES


Appendix

**IM and Flywheel**

Nominal power: $P_{n,IM} = 1.5 \text{ kW}$
Nominal voltage: $V_a = 220/380 \text{ V}$
Nominal rotational speed: $\Omega_{n,IM} = 157 \text{ rad/s}$
Pole pairs: $p = 2$
Stator resistance: $R_s = 5.72 \Omega$
Rotor resistance: $R_r = 4.2 \Omega$
Stator inductance: $L_s = 0.462 \text{ H}$

Rotor inductance: $L_r = 0.462 \text{ H}$
Mutual inductance: $M = 0.44 \text{ H}$
FESS inertia (Flywheel + IM): $J_f = 2.43 \text{ kg} \cdot \text{m}^2$
Viscous friction coefficient: $f = 0.0656 \text{ Nm} \cdot \text{rad} \cdot \text{s}^{-1}$

**DC Bus and Filter**

DC bus voltage: $v_{dc} = 400 \text{ V}$
Equivalent capacitance: $C = 2200 \mu\text{F}$