A General Approach for Direct Conversion of Single Phase AC to AC Converter for Induction Heating System

Dr. P. Umasankar¹, Dr. S. Senthil Kumar²

¹Department of EEE, AVS Engineering College, Salem, India
²Department of EEE, Government College of Engineering, Salem, India

Email: nagaraj2k1@gmail.com

Abstract

This paper signifies the study of modeling and simulation of a single phase matrix converter for induction heating system. The working principle and the control method, using PID are revealing in detail. The performance of the system is carried out in MATLAB/Simulink environment with pulse width modulation switching strategy by varying the duty cycle. PID control is employed to obtain the better performance for a specified input supply for various output frequencies. The proposed control strategy of AC to AC converter has been discussed with a wide range of operating frequencies and results in low Total Harmonic Distortion.

Keywords

Single Phase Matrix Converter, PID Control, Induction Heating, Pulse Width Modulation Total Harmonic Distortion

1. Introduction

In recent days, Induction Heating (IH) systems have broad industrial coverage [1] and widely use in domestic and industrial applications [2] such as melting forging, hardening, tempering, annealing, brazing, bonding, welding, specialty heating, plastic injection molding, etc., and in domestic applications such as cooking, boiling, and super heating applications. A typical induction heating [3] system necessitates high frequency AC supply for which inverters or AC-AC converters or AC-DC-AC converters were being employed. It has higher throughput, efficiency, faster and non-polluting system. A typical induction heating system requires high frequency AC supply for which transformers or motor-generator sets or AC-AC converters or AC-DC-AC converters were be-
The direct AC-AC converters also termed as Matrix Converters (MC) when compared to DC link converters such as Voltage Source Inverters (VSI) and Current Source Inverters (CSI) possess more advantage such as wide range of operating frequency, variable output voltage magnitude for a given fixed frequency and fixed voltage input supply without any intermediary DC link due to direct conversion of AC-AC, which is highly advantages for these type of converters over other conventional converter and the development of fast and efficient switching devices such as SCR, GTO, MOSFET and IGBT’s paved way for using these AC-AC converters in practice effectively. In this article a Single Phase Matrix Converter (SPMC) controlled by a PID controller is employed to supply an Induction Heating (IH) system. The operation of the proposed controlled SPMC and the performance of the system over different operating frequencies is revealed in detail.

2. Single Phase Matrix Converter

Gola and Idrish experimented the SPMC with AC source having four bidirectional switches namely S1a, S1b, S2a, S2b, S3a, S3b, S4a and S4b, with the Induction Heating load is shown in Figure 2. Zuckerberger proposed the Single Phase Matrix Converter (SPMC) and consists of four bidirectional switches, such as S1a, S1b, S2a and S2b are connecting the input lines to output lines directly through the intersections discussed in detail in the block diagram.

The commutation of these switches is difficult than the VSI and CSI AC-DC-AC converters due to the absence of freewheeling path in bidirectional switch configuration. As a result commutation of switches has to be actively controlled at any time instant with respect to two basic rules. Modes of Operation of the Single Phase Matrix Converter (SPMC) consisting of eight switches is designed in a matrix form of four switching blocks in a bidirectional switching pattern as shown in Figure 1. Each switching block consists of two switches connected in anti-parallel direction as shown in Figure 2 with a recovery diode for each switch. The output of the matrix converter is connected to the inductive heating system which is indicated by load as shown in Figure 1.

The switching pattern of the Matrix Converter switches for a constant input supply frequency of 50 Hz is given in Table 1 for various output frequencies of the Matrix Converter fed Induction Heating system. Table 1 gives switching pattern for output frequencies 25 Hz, 50 Hz and 100 Hz whereas output frequencies 1 kHz, 10 kHz and 100 kHz switching pattern have 40, 400 and 4000 time intervals respectively for a single cycle of input and hence not represented in Table 1.

The switches S1, S3 and S2, S4 can be switched ON simultaneously as they will short circuit the input lines which will destroy the converter due to over current is shown in Figure 2. Similarly any switches S1, S3 and S2, S4 should not be switched OFF simultaneously at any instant as it will open circuit the output phase which leads to the absence of path for the flow of inductive current leading to over voltages. This leads to a
Table 1. Power flow switching sequence of the single phase matrix converter.

<table>
<thead>
<tr>
<th>Input frequency</th>
<th>50 Hz</th>
<th>25 Hz</th>
<th>50 Hz</th>
<th>100 Hz</th>
</tr>
</thead>
<tbody>
<tr>
<td>Output frequency</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Time interval</td>
<td>1</td>
<td>2</td>
<td>3</td>
<td>4</td>
</tr>
<tr>
<td>Switching mode</td>
<td>S_{1a}-S_{4a}</td>
<td>S_{1b}-S_{2b}</td>
<td>S_{2a}-S_{3a}</td>
<td>S_{3b}-S_{4b}</td>
</tr>
</tbody>
</table>
Figure 3. Power flow in mode 1 operation (S1a and S4a: ON).

signal to conduct the positive half-cycle in reverse direction to the load as shown in Figure 4.

In mode 3 switching operation, switches S2b and S3b are switched ON by the PWM signal to conduct the negative half-cycle in forward direction to the load as shown in Figure 5.

In mode 4 switching operation, switches S4b and S1b are switched ON by the PWM signal to conduct the negative half-cycle in reverse direction to the load as shown in Figure 6.

Based on the four operating sequences the Matrix Converter output frequency can be varied by varying the combination of the operating sequence of the switches and the switches describe the switching sequence of the Matrix Converter switches for an input voltage source frequency of 50 Hz to obtain variable frequency ranges.

Figure 7 shows the various output voltage waveform of the Single Phase Matrix Converter for various output frequency to a corresponding input frequency of 50 Hz.

a) Modeling of Single Phase to Single Phase Matrix Converter for Induction Heating

The Single Phase to Single Phase Matrix Converter module shown in Figure 8 which is designed with four modules of single bidirectional switches as shown in Figure 9. The designed Single Phase to Single Phase Matrix Converter is connected to an AC supply in the input and the output of the Matrix Converter is connected to an Induction Heating load [16]. The Single Phase to Single Phase Matrix Converter modeling in MATLAB/Simulink environment is carried out starting with the modeling of bidirectional switches. The common emitter connected bidirectional switch arrangement of Single Matrix Converter switch module designed with MATLAB/Simulink environment [17].

The modelling of the instantaneous input voltage is given by the Equation (1)

\[ V_i(t) = V_m \cos(\omega t) \]  \hspace{1cm} (1)

The instantaneous input current \( i(t) \) is given by the Equation (2.2)
Figure 4. Power flow in mode 2 operation (S2a and S3a: ON).

Figure 5. Power flow in mode 3 operation (S2b and S3b: ON).

Figure 6. Power flow in mode 4 operation (S4b and S1b: ON).
Figure 7. Output frequencies of single phase matrix converter various output waveforms for 25 Hz, 50 Hz and 100 Hz corresponding to an input frequency of 50 Hz.

Figure 8. Circuit diagram of single phase to single phase matrix converter induction heating.
The instantaneous output voltage $v_o(t)$ is given by the Equation (3)

$$
v_o(t) = \begin{cases} 
    v_i(t); & \text{if } i_o(t) > 0; \\
    -v_i(t); & \text{if } i_o(t) < 0; \\
    0; & \text{if } i_o(t) = 0.
\end{cases}
$$

The output voltage during any cycle is given by the Equation (4)

$$
v_o^k(t) = \left(m_1^k - m_2^k\right) v_i^k(t)
$$

where

- $v_o^k(t)$ = output voltage during any $k^{th}$ cycle;
- $v_i^k(t)$ = input voltage during any $k^{th}$ cycle.

The modulation index of any switch during any switching time is given by the Equations (5)-(8)

$$
m_i^k(t) = \frac{\Delta_i^k}{T_s}
$$

$$
\sum_{j=1}^{2} \Delta_j = T_s
$$

$$
m_1^k + m_2^k = 1
$$
where
\[ m_k^j = \begin{pmatrix} m_{11}^k & m_{12}^k \\ m_{21}^k & m_{22}^k \end{pmatrix} \] (8)

- \( m_{11}, m_{22} \) = the modulation index of PWM signals during any \( k^{th} \) cycle;
- \( \Delta_j^k \) = the time interval when the circuit is in mode \( j \), during any \( k^{th} \) cycle; \( (j = 1, 2) \);
- \( T_s = \frac{1}{f_s} \) = switching cycle time.

**b) Simulink Model of Single Phase to Single Phase Matrix Converter for Induction Heating**

The simulation of Single Phase Matrix Converter is built up with four bidirectional IGBT switches connected in Common Emmitter Mode shows in Figure 8. The model of Single Phase to Single Phase Matrix Converter is consisting of single phase voltage source, Single Phase Matrix Converter and Single Phase Induction Heating load. Figure 9 shows the basic simulation circuit of Single Phase Matrix Converter switching arrangement [18]. Switching arrangement as a sub system which is connected with two IGBT back to back connection with two anti-parallel diodes as shown in Figure 10.

**3. PID Controller for the Proposed Converter**

The control signal from the PID controller output is fed to the PWM signal generator which acts as modulation index for the PWM generator to generate pulse width modulated signals for energising the Matrix Converter switches to produce Single phase output from the Matrix Converter.

![Figure 10. Simulation of common emitter bidirectional single module of matrix converter switch.](image-url)
The input AC supply is fed to the Matrix Converter which energizes the Induction heating system shown in Figure 11. The Matrix Converter switching pattern generates nine switching pulse sequence in PWM mode block diagram stated in Figure 12. The load current or the output current of the Matrix Converter is compared with the reference value to produce the error (e) in output current. The change in error (ce) is calibrated and the error (e) and change in error (ce) are fed as inputs to the PID Controller. The PID controller produces a corresponding output signal for this input which is the control signal or modulation index for the pulse width modulation generator [19]. The pulse width modulation signal generator produces corresponding PWM signals for energizing the Matrix Converter through the bidirectional switches [20].

4. Results and Discussions

The results obtained from PID controlled Single Phase to Single Phase Matrix Converter for Induction Heating for various operating frequencies from 25 Hz to 100 kHz is presented in following figures. Figure 13(a) shows the input voltage and output voltage for operating frequency of 25 Hz and Figure 13(b) shows the corresponding output current for the Single Phase Induction Heating load rated for 230 V, 2.25 A. Figure 13(c) shows the THD measured for the corresponding operating frequency output. A THD of 42.06 is being measured for 25 Hz output frequency.

![Figure 11. Block diagram of PID controller for single phase to single phase matrix converter.](image1)

![Figure 12. Simulation of PID controller for single phase to single phase matrix converter.](image2)
Figure 13. (a) PID control of single phase to single phase matrix converter input and output voltage waveform for $f_o = 25$ Hz; (b) PID control of single phase to single phase matrix converter output current waveform for $f_o = 25$ Hz; (c) PID control of single phase to single phase matrix converter total harmonic distortion for $f_o = 25$ Hz.
**Figure 14(a)** shows the input voltage and output voltage for operating frequency of 50 Hz and **Figure 14(b)** shows the corresponding output current for the Single Phase Matrix Converter for Induction Heating system load. **Figure 14(c)** depicts the Total Harmonic Distortion for the same operating frequency.

**Figure 14.** (a) PID Control of single phase to single phase matrix converter input and output voltage waveform for \( f_o = 50 \) Hz; (b) PID control of single phase to single phase matrix converter output current waveform for \( f_o = 50 \) Hz; (c) PID control of single phase to single phase matrix converter total harmonic distortion for \( f_o = 50 \) Hz.
Harmonic Distortion (THD) measured for the corresponding operating frequency output. A THD of 37.52 is being measured for 50 Hz output frequency. Moreover the current and voltage waveforms are in phase which shows the unity power factor.

Figure 15(a) shows the input voltage and output voltage for operating frequency of 100 Hz and Figure 15(b) shows the corresponding output current for the Single Phase Induction Heating system load.

![Diagram](image)

**Figure 15.** (a) PID control of single phase to single phase matrix Hz converter output current waveform for $f_o = 25$; (b) PID control of single phase to single phase matrix converter input and output voltage waveform for $f_o = 100$ Hz; (c) PID control of single phase to single phase matrix converter total harmonic distortion for $f_o = 100$ Hz.
Figure 15(c) depicts the THD measured for the corresponding operating frequency output. A THD of 27.14 is being measured for 100 Hz output frequency.

Hence the frequency study of the described input and the corresponding output plotted and discussed. Table 2 represents the THD measured for the various operating frequencies in the PID controller based Single Phase Matrix Converter for Induction Heating.

Figure 16 shows the graph for Total Harmonic Distortion vs various operating frequencies for the proposed system.

As stated frequency and the Total Harmonic Distortion and different frequency relationship of PID Controller based Single Phase Matrix Converter for Induction Heating are compared.

5. Conclusion

The single phase matrix converter powered by single phase source is modeled in MATLAB/Simulink and performance analysis of the converter is carried out with linear proposed PID controller. The PID controller based single phase to single phase matrix converter results were explained and discussed. Simulation is carried out for specified frequencies such as 25 Hz, 50 Hz and 100 Hz. The output of the converter presented and comparison of total harmonic distortion of the PID controller based single phase matrix converter is also presented. The performance of single phase matrix converter

![Figure 16](image1)

Figure 16. Total Harmonic distortion vs frequency plot for PID control of single phase to single phase matrix converter for induction heating.

Table 2. Measurement of THD for various operating frequencies of PID controlled single phase to single phase matrix converter.

<table>
<thead>
<tr>
<th>S. No</th>
<th>Frequency in Hz</th>
<th>THD in %</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>25</td>
<td>42.06</td>
</tr>
<tr>
<td>2</td>
<td>50</td>
<td>37.52</td>
</tr>
<tr>
<td>3</td>
<td>100</td>
<td>27.14</td>
</tr>
</tbody>
</table>
controlled by PID controller is analyzed and they exhibit low Total Harmonic Distortion (THD). The proposed PID controller based matrix converters demonstrate the robust operation for induction heating load.

**References**


**Nomenclatures**

\[ V^k_i(t) \]: Input Voltage during any cycle \(k^{th}\)

\[ V^k_o(t) \]: Output Voltage during any cycle \(k^{th}\)

\[ \Delta^j_k \]: Time interval in mode \(j\) during the \(k^{th}\) cycle

\[ m_1, m_2 \]: Modulation index of PWM signals

\[ f_s \]: Switching frequency

\[ T_s \]: Switching cycle time

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